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Ingersoll-

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SCHOLAB'S ARITHMETIC,

OR

Federal Accountant.

CONTAINING,

- I. COMMON ARITHMETIC, THE RULES AND ILLUSTRATIONS.
- II. Examples and Answers with Blank Spaces, sufficient for their operations by the SCHOLAR.
- III. To Each Rule a Supplement, comprehending, 1. QUESTIONS on the nature of the Rule, its use, and the manner of its operations, 2. EXERCISES.
- IV. Federal Money, with rules for all the various operations in it—to reduce Federal to Old Lawful, and Old Lawful to Federal Money.
- V. Interest cast in Federal Money, with Compound Multiplication, Compound Division and Practice, wrought in Old Lawful and in Federal Money, the fame questions being put, in separate columns on the same page, in each kind of money, by which these two modes of account become contrasted, and the great advantage gained by reckoning in Federal Money easily discerned.
- VI. DEMONSTRATIONS, BY ENGRAVINGS, OF THE REASON AND NATURE OF THE NATIOUS STEPS IN THE EXTRACTION OF THE SQUARE AND CUBE ROOTS,
 NOT TO BE FOUND IN ANY OTHER TREATISE ON ARITHMETIC.
- VII. FORMS OF NOTES, DEEDS, BONDS, AND OTHER INSTRUMENTS OF WRITING.
 THE WHOLE IN A FORM AND METHOD ALTOGETHER NEW,
 FOR THE EASE OF THE MASTER AND THE GREATER PROGRESS OF THE SCHOLAR.

BY DANIEL ADAMS, M. B.

SEVENTH EDITION.

PUBLISHED ACCORDING TO ACT OF CONGRESS.

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1812.

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District of Massachusetts District, To wir :

(25) BE IT REMEMBERED, that on the Ninth day of September, in the 26th Year of the Independence of the United States of America, DANIEL ADAMS, of the faid Diffrict, hath deposited in this office the Title of a book, the right whereof he claims as AUTHOR, in the following words, to wit: "The Scholar's Arithmetic: or Federal Accountant. Containing, I. Common Arithmetic, the rules and illustrations.—IL Examples and answers, with Blank spaces sufficient for their operation by the Scholar.—III. To each rule a Supplement, comprehending, 1. Questions on the nature of the rule, its use, and the manner of its operations.—2 Exercises.—IV. Federal Money, with rules for all the various operations in it, to reduce Federal to Old Lawful and Old Lawful to Federal Money.—V. Interest cast in Federal Money, with Compound Multiplication, Compound Division, and Practice wrought in Old Lawful and in Federal Money, the same questions being put in separate columns on the same page, in each kind of money, by which thefe two modes of account become contrasted and the great advantage gained by reckoning in Federal Money eafily differred. VI. Demonstrations by engravsings of the reason and nature of the various. Reps. in the extraction of the Square and Cube Roots, not to be found in any other treatife on Arithmetic. -VII. Forms of Notes, Deeds, Bonds and other infiruments in writing:-The whole in a form and method altogether new, for the ease of the Maker and the greater progress of the Scholar.

By DANIEL ADAMS, M. B."

IN conformity to the act of the Congress of the United States, entitled, "An act for the encouragement of Learning, by securing the Copies of Maps, Charts and Books, to the Authors and Proprietors of such Copies, during the times therein mentioned."

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A true Copy of Record.]

RECOMMENDATIONS.

New-Salem, Sept. 14th, 1801.

HAVING attentively examined "The Scholar's Arithmetic," I cheerfully give it as my opinion, that it is well calculated for the instruction of youth; and that it will abridge much of the time now necessary to be spent in the communication and attainment of such Arithmetical knowledge, as is proper for the discharge of business.

WARREN PIERCE.

Preceptor of New-Solem Academy.

Groton Academy, Sept. 2, 1801.

I HAVE perused with attention "The Scholar's Arithmetic," which you transmitted to me some time since. It is, in my opinion, better calculated to lead students in our Schools and Academies into a complete knowledge of all that is useful in that branch of literature, than any other work of the kind I have seen. With great sincerity I wish you success in your exertions for the promotion of useful learning; and I am confident, that to be generally approved, your work needs only to be generally known.

WILLIAM M. RICHARDSON.

Preceptor of the Academy,

EXTRACT

Of a letter from the Hon. JOHN WHEELOCK, L. L. D. President of Dartmouth College, to the AUTHOR.

"THE Scholar's Arithmetic is an improvement on former productions of the same nature. Its distinctive order and supplement will help the learner in his progress; the part on Federal Money makes it more useful; and I have no doubt but the whole will be a new fund of profit in our country."

Sept. 7th, 1807.

THE Scholar's Arithmetic contains most of the important Rules of the Art, and something, also, of the curious and entertaining kind.

The subjects are handled in a simple and concise manner.

While the Questions are few, they exhibit a considerable variety. While they are, generally, easy, some of them afford scope for the exercise of the Scholar's Judgment.

It is a good quality of the Book, that it has so much to do

with Federal Money.

The plan of showing the reasons of the operations in the extraction of the Square and Cube Roots is good.

DANIEL HARDY, Jun.
Preceptor of Chesterfield Academy.

Extract of a letter from the Rev. LABAN AINSWORTH, of Jaffrey, to the publisher of the 4th Edition, dated Aug. 3, 1807.

"THE Superiority of the Scholar's Arithmetic to any book of the kind in my knowledge, clearly appears from its good effect in the Schools I annually visit. Previous to its introduction, Arithmetic was learned and performed mechanically; since, scholars are able to give a rational account of the several operations in Arithmetic, which is the best proof of their having learned to good purpose."

PREFACE [TO THE 2d EDITION] DEDICATORY

TO

SCHOOL MASTERS.

χ

GENTLEMEN,

AFTER expressing my sincere thanks for your kind and very ready acceptance of the first Edition of the SCHOLAR'S ARITHMETIC, permit me now to offer for your further consideration and favor, the Second Edition, which, with its Corrections and Additions, it is hoped, will be found still

more deserving of your approbation.

The testimony of many respectable Teachers has inspired a confidence to believe, that this work, where it has been introduced into Schools, has proved a kind assistant towards a more speedy and thorough improvement of Scholars in Numbers, and at the same time, has relieved masters of a heavy burden of writing out Rules and Questions, under which they have so long laboured, to the manifest neglect of other parts of their Schools.

To answer the several intentions of this work, it will be necessary that it should be put into the hands of every Arithmetician; the blank after each example is designed for the operation by the Scholar, which being first wrought upon a slate, or waste paper, he may afterwards transcribe into his book.

The Supplement to each Rule in this work is a novelty. I have often seen books with questions and answers, but in my humble opinion, it is no evidence that the Scholar comprehends the principles of that science which is his study, because that he may be able to repeat, verbatim from his book, the answer to a question on which his attention has been exercised, two or three hours, to commit to memory. Study is of but little advantage to the human mind without reflection. To force the Scholar into reflections of his own, is the object of those Questions unanswered, at the beginning of each Supplement. The Exercises are designed, tests of his judgment. The Supplements may be omitted the first time going through the book, if thought proper, and taken up afterwards as a review.

Through the whole it has been my greatest care to make myself intelligible to the Scholar; such rules and remarks as have been compiled from other authors are included in quotations; the *Examples*, many of them, are extracted. This I have not hesitated to do, when I found them suited to my purpose.

Demonstrations of the reason and nature of the operations in the extraction of the Square and Cube Roots have never been attempted, in any work of the kind before, to my knowl-

edge. It is hoped these will be found satisfactory.

I have only to add, that any intimation of amendments or defects by the candid and experienced of your order, will be thankfully received by

Gentlemen,

Your most humble, and

most obedient servant,
DANIEL ADAMS.

Leominster, Mass. Oct. 1, 1802.

SEVENTH EDITION.

The Seventh edition is printed, page for page, from the Sixth.

CONTENTS.

Introduction.

NOTATION AND NUMERATION.

SECTION I.

FUNDAMENTAL RULES OF ARITHMETIC.	
	PAGR.
Simple Addition	. 13
do. Subtraction	. 19
do. Multiplication	. 23
do Division	. 33
Compound Addition	. 42
do Division	. 53
SECTION II.	
RULES ESSENTIALLY NECESSARY FOR EVERY PERSON TO FIT AND QU	ALIFY
THEM FOR THE TRANSACTION OF BUSINESS.	
	. 58
Fractions	. 75
Reduction Fractions Decimel Fractions	. 76
Federal Manay	. 87
Federal Money Table to reduce Shillings and Pence to Conts and Mills	. 94
Tables of suchanas	. 95
Tables of exchange	. 93
Therest	. 90 . 100
Method of Casting Interest on Notes and Bonds when partial payment	S
at different times have been made	. 102
	. 104
	. 107
do. Division	. 112
Single Rule of Three	. 119
Single Rule of Three	. 138
Practice	. 143
SECTION III.	
RULES OCCASIONALLY USEFUL TO MEE IN PARTICULAR EMPLOYMEN	TS OF
LIFE.	
Involution	159
Evolution	159
Extraction of the Square Root	160
Demonstration of the Reason and Nature of the various steps in the op	
eration of extracting the Square Root	161
Extraction of the Cube Root	169
Demonstration of the Reason and Nature of the various steps in the op	
eration of extracting the Cube Root	170
Single Fellowship	179
Single Fellowship	1 (3

170

CONTENTS.

Double Fellowship	-	•		-		•		•	•	•	-	•	•	181
Barter								-	-	-	-	-	-	184
Loss and Gain -				-					_	-		-	-	187
Duodecimals, or C	ross N	Aul ti	olica	tion		_	· ^ 4)	_	_		_			190
								_	_	-		-		191
do.		Boar	ds			<u>.</u> .		_	_	_		-	٠,	192
				_				_		_		_		
				_				_	_				_	
								-	-	_	_	_	_	
			_	_			_	_	_		_	_		
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1st. To find the	circu	mfer	ence	of a	ı circl	e, the	e dia	met	er b	ein	g g	ŗive	n	
2d. To find the	area	of a	circl	e, th	e dia	meter	bei	ng g	zive	n	-	-	-	206
3d. To measure	the s	olidi	ty of	an	irregı	ılar b	ody	-	•	-	-	-	-	206
		`			_					×				
			OL	UI.	\mathbf{r}	17.								
	MISC	CEL	LAI	NEC				ON	s.	:				
	MISC	CEL			ous	QUE		ON	s.	•	•			
	MISC	CEL			ous	QUE		ON	s.	•	•			
	MISC		SE	CT	ous ION	QUE V.	STI	ON	s.	•	•			
	MISC		SE	CT	ous ION	QUE V.	STI	ON	s.	•		•		011
Notes	MISC		SE	CT	ous ION	QUE V.	STI	ON.	s.	•	•			211
Notes Bends	MISC		SE	CT	ous ION	QUE V.	STI	ON.	s.	•	•			212
Notes Bends Receipts	MISC		SE	CT	ous ION	QUE V.	STI	ON	s.	•				212 213
Notes Bends Receipts Orders	MISC		SE	CT	ous ION	QUE V.	STI	ON	s. -					212 213 214
Notes Bends Corders Deeds	MISC		SE	CT	ous ION	QUE V.	STI	ON	s.					212 213 214 214
Notes Bonds Receipts Deeds Indenture	MISC		SE	CT	ous ION	QUE V.	STI	ON	s.					212 213 214 214 214 215
Notes Bends Corders Deeds	MISC		SE	CT	ous ION	QUE V.	STI	ON	S					212 213 214 214
Notes Bonds Receipts Deeds Indenture	MISC		SE	CT	ION NOTI	QUE V.	STI	ON	S.					212 213 214 214 214 215
Barter	212 213 214 214 215 216													
### Barter	212 213 214 214 215 216													
### Barter	212 213 214 214 215 216													
Barter														
### Barter	212 213 214 214 215 216													
## Barter														
Notes Bonds	OF Tequal	FOR THE	SE CHA	CT	OUS ON NOTE	QUE V. V. Sis, E	STI c. MAI lition	DE milio	US es ti	hat +	10 -	0 c	ent tha	212 213 214 214 215 216 THE
Notes Bonds	OF Tequal	FOR THE	SE CHA	CT	OUS ON NOTE	QUE V. V. Sis, E	STI c. MAI lition	DE milio	US es ti	hat +	10 -	0 c	ent tha	212 213 214 214 215 216 THE
Notes Bonds Receipts Orders Deeds Indenture Will FXPLANATION The sign of equal to 1 doll Saint Geo added to 4 is The fign of fubt	OF Tequal ar.	FOR THE Cross to 6 on; a	SE CH.	CT	OUS (NOTI ACTE RK. cts = gn of	QUE V. ss, & CRS	MAII figuition	DE mific	US to ses the	hat +	10 k=	0 c 6, 1e	ent tha ave	212 213 214 214 215 216 THE s are t is 2 s 4.
Notes Bonds Receipts Orders Orders Deeds Indenture Will FXPLANATION The sign of equal to 1 doll Saint GEO added to 4 is The fign of fubt Saint Andre	oF Tequal ar. RGE's equal raction are.	FOR THE Cross to 6 on ; as Cross Cro	SE CHA	CT AR WO 100 he fi	OUS (NOTI ACTE RK. cts = gn of	QUE V. ss, & CRS	MAII figuition	DE mific	US to ses the	hat +	10 k=	0 c 6, 1e	ent tha ave	212 213 214 214 215 216 THE s are t is 2 s 4.
Notes Bonds Receipts Orders Orders Deeds Indenture Will FXPLANATION The sign of equal to 1 doll Saint GEO added to 4 is The fign of fubt Saint Andre that is, 4 time	oF T equal ar. raction raction rew's s 6 is	FOR THE Crost to 6 on ; a Crost con con contract con contract cont	SE CHA	CT OF ARA WO 1 100 2= the : 24.	OUS (NOTI ACTE RK. cts = 4; 1	QUE V. ss, & CRS add	STI c. MAI lition s, 2 ultip	DE mific	US es ti	hat +	10 h=- n 6 as 4	6, 6, 1e	ent tha ave 6_	212 213 214 215 216 7HE s are t is 2 s 4.
Notes Bonds Receipts Orders Orders Deeds Indenture Will FXPLANATION The sign of equal to 1 doll Saint GEO added to 4 is The fign of fubt Saint Andre that is, 4 time	oF T equal ar. raction raction rew's s 6 is	FOR THE Crost to 6 on ; a Crost con con contract con contract cont	SE CHA	CT OF ARA WO 1 100 2= the : 24.	OUS (NOTI ACTE RK. cts = 4; 1	QUE V. ss, & CRS add	STI c. MAI lition s, 2 ultip	DE mific	US es ti	hat +	10 h=- n 6 as 4	6, 6, 1e	ent tha ave 6_	212 213 214 215 216 7HE s are t is 2 s 4.
Notes Bonds Receipts Orders Orders Deeds Indenture Will EXPLANATION The sign of equal to 1 doll Saint Geo added to 4 is The fign of fubt X Saint And that is, 4 time received a divided by	equal raction is so 6 is sed Party 3 is	Croo equarently	SE CH. as fs, t s 6— sss, t l to nefis, al to	CT of AR. WO. 100 he fi	OUS (NOT) ACTE RK. ds=-4;; sign of fign fign r6-+	V. SS, & CRS add hat i of m of d 3=2	MAII. figure	DE ; a tak licat	US es ti	hat ror;	10 h= n 6 as 4	6, 6, 6 le 1×	ent tha ave 6=	212 213 214 214 215 216 7HE s are t is 2 s 4. -24; is, 6
Notes Bonds Receipts Orders Deeds Indenture Will EXPLANATION The sign of equal to 1 doll Saint Geo added to 4 is The fign of fubt Saint And that is, 4 time	oF 7 equal ar. equal raction tew's s 6 is sed Pa y 3 is gn of	Cro to 6 or cequarently prop	SE CH. as fs, t s 6— sss, t l to nefis, al to	CT of AR. WO. 100 he fi	OUS (NOT) ACTE RK. ds=-4;; sign of fign fign r6-+	V. SS, & CRS add hat i of m of d 3=2	MAII. figure	DE ; a tak licat	US es ti	hat ror;	10 h= n 6 as 4	6, 6, 6 le 1×	ent tha ave 6=	212 213 214 214 215 216 7HE s are t is 2 s 4. -24; is, 6

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SCHOLAR'S ARITHMETIC.

INTRODUCTION.

ARITHMETIC is the art or science which treats of numbers.

It is of two kinds, theoretical and practical.

The THEORY of Arithmetic explains the nature and quality of numbers, and demonstrates the reason of practical operations. Considered in this sense Arithmetic is a Science.

PRACTICAL ARITHMETIC shews the method of working by numbers, so as to be most useful and expeditious for business. In this sense Arithmetic is an Art.

DIRECTIONS TO THE SCHOLAR.

Deeply impress your mind with a sense of the importance of arithmetical knowledge. The great concerns of life can in no way be conducted without Do not, therefore, think any pains too great to be bestowed for so noble an end. Drive far from you idleness and sloth; they are great enemies to improvement. Remember that youth, like the morning, will foon be past, and that opportunities once neglected, can never be regained. things, there must be implanted in your mind a fixed delight in study; make it your inclination; "A defire accomplished is sweet to the foul." Be not in a hurry to get through your book too foon. Much instruction may be given in these few words, understand every thing as you go along. Each rule is first to be committed to memory; afterwards, the examples in There is not a illustration, and every remark, are to be perused with care. word inserted in this Treatise, but with a design that it should be studied by the Scholar. As much as is possible, endeavor to do every thing of yourfelf; one thing found out by your own thought and reflection, will be of more real use to you, than twenty things told you by an Instructor. Be not overcome by little feeming difficulties, but rather strive to overcome fuch by patience and application; fo shall your progress be easy, and the object of your endeavors fure.

On entering upon this most useful study, the first thing which the Scholar has to regard is

NOTATION.

NOTATION is the art of expressing numbers by certain characters or figures; of which there are two methods.

1. The Roman method, by Letters.

2. The Arabic method, by figures. The latter is that of general use.

In the Arabic method all numbers are expressed by these ten characters or figures.

Unit, or; two; three; four; five; fix; feven; eight; nine; cypher, or one nothing.

The nine first are called fignificant figures, or digits, each of which standing by itself or alone, invariably expresses a particular and certain number; thus, I signifies one, 2 signifies two, 3 signifies three, and so of the rest until you come to nine, but for any number more than nine, it will always require two or more of those sigures set together in order to express that number.

This will be more particularly taught by

NUMERATION.

Numeration teaches how to read or write any fum or number by figures. In fetting down numbers for arithmetical operations, especially with beginners, it is usual to begin at the right hand, and proceed towards the left.

Example. If you wish to write the sum or number 537, begin by setting down the seven, or right hand sigure, thus, 7, next set down the three, at the left hand of the seven, thus, 37, and lastly the five, at the left hand of the

three, thus 537, which is the number proposed to be written.

In this fum thus written you are next to observe, that there are three places, meaning the situations of the three different sigures, and that each of these places has an appropriated name. The first place, or that of the right hand sigure, or the place of the 7, is called Unit's place; the second place, or that of the sigure standing next to the right hand sigure, in this case the place of the 3, is called ten's place; the third place, or next towards the less thand, or place of the 5, is called hundred's place; the next, or fourth place, for we may suppose more sigures to be connected, is thousand's place; the next to this, tens of thousand's place, and so on to what length we please, there being particular names for each place. Now every sigure signifies differently, accordingly as it may happen to occupy one or the other of these places.

The value of the first or right hand figure, or of the figure standing in the place of units, in any sum or number, is just what the figure expresses standing alone or by itself; but every other figure in the sum or number, or those to the lest hand of the first figure, have a different signification from their true or natural meaning, for the next figure from the right hand towards the lest, or that figure in the place of tens expresses so many times ten, as the same figure signifies units or ones when standing alone, that is, it is ten times its simple, primitive value; and so on, every removal from the right hand figure making the figure thus removed ten times the value of the same

figure when standing in the place immediately preceding it.

Hund. Tens. Units.

Example. Take the sum 3 3 3, made by the same figure three times repeated. The first or right hand sigure, or the sigure in the place of units, has its natural meaning or the same meaning as if standing alone, and signifies three units or ones; but the same figure again towards the lest hand in the second place, or place of tens, signifies not three units, but three tens, that is, thirty, its value being increased in a tenfold proportion; proceeding on still surther towards the lest hand, the next figure, or that in the third place, or place of bundreds, signifies neither three nor thirty, but three bundred, which is ten times the value of that sigure, in the place immediately preceding it, or that in the place of tens. So you might proceed and add the sigure 3, sifty or an hundred times, and every time the sigure was added, it would signify ten times more than it did the last time before.

A CYPHER standing alone is of no signification, yet placed at the right hand of another figure it increases the value of that figure in the same ten fold proportion, as if it had been preceded by any other figure. standing alone, signifies three; place a cypher before it, (30) and it no longer fignifies three but thirty; and another cypher (300) and it fignifies three

The value of figures in conjunction, and how to read any fum or number, agreeably to the foregoing observations, may be fully understood by the fol-

lowing

-Hund. of Thous. of Mil

*Hundreds of Thousand

8

2 1

2

3 4

7 0 3

1

3 6 7

7

4

0 6

6 3

9098

76 **54**

567

Hundreds of Million

7 6 2 1 6

1

7 Ó

> 6 2

Tens of Millions

TABLE.

The words at the head of the Table shew the fignification of the figures against which they itand; and the figures shew how many of that fignification are meant. Thus, units in the first place signifies ones, and 6 standing against it shew that fix ones, or individuals are here meant; tens in the second place shew that every figure in this place means so many tens, and 3 standing against it shews that three tens are here meant, equal to thirty, what the figure really fignifies. Hundreds in the third place shew the meaning of figures in this place to be Hundreds, and 8 shews that eight hundreds are meant. In the fame manner the value of each of the remaining figures in the Table is known. Having proceeded thro' in this way, the fum of the first line of figures or those immediately against the words, will be found to be Two billions, one hundred fixty seven thousands, two bundred and thirty five millions; four hundred / 123 twenty one thousands; eight hundred and thirty In like manner may be read all the remaining numbers in the Table.

Those words at the head of the Table are applicable to any sum or number, and must be committed perfectly to memory so as to be readily applied

on any occasion.

For the greater case in reckoning, it is convenient and often practised in public offices and by men of business, to divide any number into periods and half periods, as in the following manner:

TRILLIONS.

ed thousand of billions & Fen thousand of billions & Thousand billions & Hundred billions 9

Ten billions & Ten billions & Billions & Ten billions & Fen thousand of millions & Fen thousand of millions & Fen thousand millions & Fen tho Thoufand millions thundred millions to Ten millions 9 Millions 9 Hundred thoufands of Ten thoufands to Thoufands to Hundreds to Hundreds to Thoufands to Hundreds to Tens 9 red thousand of millions red thousand of

The first fix figures from the right hand are called the unit period, the next fix the million period, after which the trillion, quadrillion, quintillion, periods, &c. follow in their order.

Thus, by the use of ten figures may be reckoned every thing which can be numbered; things, the multitude of which far exceed the comprehension of

man.

"It may not be amiss to illustrate by a sew examples the extent of numbers, which are frequently named without being attended to. If a person employed in telling money, reckon an hundred pieces in a minute, and continue at work ten hours each day, he will take seventeen days to reckon a million; a thousand men would take 45 years to reckon a billion. If we fuppose the whole earth to be as well peopled as Britain, and to have been so from the creation, and that the whole race of mankind had constantly pent their time in telling from a heap consisting of a quadrillion of pieces, they would hardly have yet reckoned a thousandth part of that quantity."

After having been able to read correctly to his inftructor all the numbers in the foregoing Table, the learner may proceed to write the following num-

bers out in words.

6

9 8

4 3 7

6019

72845

149703

9783016

5372168**b**

SECTION I.

FUNDAMENTAL RULES OF ARITHMETIC.

THESE are four, Addition, Subtraction, Multiplication, and Division; they may be either simple or compound; simple, when the numbers are all of one sort or denomination; compound, when the numbers are of different denominations.

They are called, *Principal* or *Fundamental Rules*, because that all other rules and operations in Arithmetic are nothing more

than various uses and repetitions of these four rules.

The object of every arithmetical operation, is, by certain given quantities which are known, to find out others which are unknown. This cannot be done but by changes effected on the given numbers; and as the only way in which numbers can be changed is either by increasing or by diminishing their quantities, and as there can be no increase or diminution of numbers but by one or the other of the above operations, it consequently follows, that these four rules embrace the whole art of Arithmetic.

§ 1. Simple Addition.

SIMPLE ADDITION is the putting together of two or more numbers, of the fame denomination, so as to make them one whole or total number; as 3 dollars, 6 dollars, and 8 dollars added or put together, make 17 dollars.

RULE.

"Write the numbers to be added one under another, with units under units, tens under tens, and so on. Draw a line under the lower number, then add the right hand column; and if the sum be under ten, write it at the foot of the column; but if it be ten, or an exact number of tens, write a cypher; and if it be not an exact number of tens, write the excess above tens at the foot of the column; and for every ten the sum contains, carry one to the next column, and add it in the same manner as the former. Proceed in the like manner to add the other columns, carrying for the tens of each to the next, and mark down the full sum of the left hand column."

PROOF.

Reckon the figures from the top downwards, and if the work be right, this amount will be equal to the first;—or, what is often practised, "cut off the upper line of figures and find the amount of the rest; then if the amount and upper line, when added, be equal to the sum total, the work is supposed to be right."

EXAMPLES.

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dollars, and of 3 dollars, when added together?

Here are four sums given for addition; two of them contains units, tens, bundreds, thousands; another of them contains units, tens, hundreds; and a fourth contains units only. The first step to prepare these sums for the operation of addition, is to write them down, units under units, tens under tens, and so on as in the following manner.

The four given fums for addition placed as the rule directs.

8 0 4 3 dollars.

8 0 4 3 dollars.
6 5 1 dollars.
3 dollars.

Answer, or amount, 1 2 3 0 9 dollars.

Amount of the three lower lines, 8*6 9 7

Proof, 12309

To find the answer or amount of the sums given to be added, begin with the right hand column, and say 3 to 1 is 4, and 3 is 7, and 2 is 9; which sum (9) being less than ten, set down directly under the column you added. Then proceeding to the next column, say again, 5 to 4 is 9, and 1 is 10, being even ten, set down 0, and carry 1 to the next column, saying 1, which I carry to six is 7, and 0 is nothing, but 6 is 13; which sum (13) is an excess of 3 over even tens; therefore set down 3 and carry 1 for the 10 to 8 in the next column, saying 1 to 8 is 9, and 3 is 12; this being the last column, set down the whole number, (12) placing the 2, or unit sigure directly under the column, and carrying the other sigure, or the 1, forward to the next place on the lest hand, or to that of tens of thousands, and the work is done.

It may now be required to know if the whole be right. To exhibit the method of proof let the upper line of figures be cut off as feen in the example. Then adding the three lower lines which remain, place the amount (8697) under the amount first obtained by the addition of all the sums, observing carefully that each figure falls directly under the column which produced it; then add this last amount to the upper line which you cut off; thus, 7 to 2 is 9; 9 to 1 is 10; carry 1 to 6 is 7 and 6 is 13; 1 which I care

ry again to 8 is 9 and 3 is 12, all which being set down in their proper places, as seen in the example, compare the amount (12309) last obtained, with the first amount (12309) and if they agree, as it is seen in this case they do,

then the work is judged to be right.

Nors. The reason of carrying for ten in all simple numbers is evident from what has been taught in Notation. It is because 10 in an inferior column is just equal in value to 1 in a superior column. As if a man should be holding in his right hand half pistareens, and in his lest hand, dollars. If you should take 10 half pistareens from his right hand, and put one dollar into his lest hand, you would not rob the man of any of his money, because 1 of those pieces in his lest hand is just equal in value to 10 of those in his right hand.

1 7 4 4 4 0 Proof.

The Scholar who has given proper attention to his rule, and the foregoing examples, will of himself be able to work the following; always remembering to carry one for every 10, and at the last column to set down the whole

number.

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6 3 5 7 0 8 5 0 0 0 0 0 0 0 2 6 8 6 7 2 1 3 4 5 3 7 8 6 7 9 8 3 6 7 7 6 0 7 6 0

Supplement to Midition.

THE attentive Scholar who has understood, and still carries in his mind, what has already been taught him of Addition, will be able to answer his in-Aructor to the following

QUESTIONS.

- 1. What is simple addition?
- 2. How do you place numbers to be added?
- 3. Where do you begin the addition?
- 4. How is the fum or amount of each column to be fet down?
- 5. What do you observe in regard to setting down the sum of the last column?
- 6. Why do you carry for ten rather than any other number?
- 7. How is addition proved?
- 8. Of what use is addition?

Note 1. Should the Learner find any difficulty in giving an answer to the above questions, he is advised to turn back and consult his Rule, with its Illustrations.

Note. 2. In treating the Rules of Arithmetic the Scholar, in all instances, is not particularly instructed in the use and application of them to the purposes of life. This is a point, however, to which his thoughts should be called; therefore it is made a question here. A consideration of the Rule and of the questions, which it involves, naturally suggests an answer. To consideration, therefore, let the Scholar apply himself. The mind acquires strength by exercise; instruction ought ever to be plain, but never so full as to preclude a necessity that the Scholar should in some degree exercise his own thoughts; it should be given in such a manner as to force him into some reflections of his own.

EXERCISES.

1. What is the amount of 2801 dollars; 765 dollars; and of 397 dollars, when added together?

Ans. 3963 dollars.

2. Suppose you lend a neighbor £210 at one time, 176 at another, £17 at another, and £9 at another, what is the fum lent? Ans. 6312.

Note. The Scholar who looks at greatness in his class will not be discouraged by a little difficulty which may at first occur in stating his question, but will apply himself the more closely to his Rule, and to thinking that if possible, he may be able of himself to answer what another may be obliged to have taught him by his Instructor.

3. Washington was born in the year of our Lord 1732; he was 67 years old when he died; in what year of our Lord did he die?

1732

4. There are two numbers; the less number is 8761, the difference between the numbers is 597; what is the greatest number?

8761

5. From the creation to the departure of the Israelites from Egypt was 2513 years; to the siege of Troy, 307 years more; to the building of Solomon's Temple, 180 years; to the building of Rome, 251 years; to the expulsion of the kings from Rome, 244 years; to the destruction of Carthage, 363 years; to the death of Julius Cæsar, 102 years; to the Christian æra, 44 years; required the time from the Creation to the Christian æra?

Ans. 4004 years.

6. At the late Census, taken A. D. 1800, the number of Inhabitants in the New-England States was as follows, viz. Newhampshire 183858; Massachusetts, 422845; Maine, 151719; Rhode-Island, 69122; Connedicut, 251002; Vermont, 154465; what was the number of Inhabitants at that time in New-England?

Ans. 1233011 Inhabitants.

23000

183858 422845 151719 69122 251002 154465 1233011

§ 2. Simple Subtraction.

SIMPLE SUBTRACTION is the taking a less number from a greater of the same denomination, so as to show the difference or remainder; as 5 taken from 8, there remains 3.

The greater number (8) is called the Minuend, the less number (5) the Subtrahend, and the difference (3) or what is left after subtraction, the Remainder.

RULE.

"Place the less number under the greater, units under units, tens under tens, and so on. Draw a line below; then begin at the right hand, and fubtract each figure of the less number from the figure above it, and place the remainder directly below. When the figure in the lower line exceeds the figure above it, suppose 10 to be added to the upper figure; but in this case you must add 1 to the under figure in the next column before you subtract it. This is called borrowing ten."

PROOF.

Add the remainder and subtrahend together, and if the sum of them correspond with the minuend, the work is supposed to be right.

EXAMPLES.

Minuend 8 6 5 3

The numbers being placed with the larger uppermost, as the rule directs, I begin with the Subtrahend 5 2 7 1

Remainder 3 3 8 2

Remainder 3 3 8 2

Proof 8 6 5 3 to be added to the upper figure (5) which make 15, then I say, 7 from 15, and there remain 8, which I set down; then proceeding to the next place, I say, 1 which I borrowed to 2 is 3, and 3 from 6 and there remain 3; this I set down, and in the next place I say 5 from 8

and there remain 3, which I fet down, and the work is done.

Proof. I add the remainder to the fubtrahend; on finding the fum just

equal to the minuend, and suppose the work to be right.

Note. The reason of borrowing ten will appear if we consider, that, when two numbers are equally increased by adding the same to both, their difference will be equal. Thus, the difference between 3 and 5 is 2; add the number 10 to each of these figures (3 and 5) they become 13 and 15, still the difference is 2. When we proceed as above directed, we add or suppose to be added, 10 to the minuend, and we likewise add 1 to the next higher place of the subtrahend, which is just equal in value to 10 of the lower place.

2. From 3 2 7 8 6 5 3 2 1 4 6 5 the minuend,
Take 1 0 6 7 9 3 6 1 2 3 4 2 the fubtrahend.

22/0/1/09/23 Remainder.

3. From <u>3</u> Take <u>1</u>	1 0	<u>6</u> 7	_do do	llars llars	, ,		4.	Fro Tal	m ke	7_	0	<u>6</u>	<u>3</u> 8	5 g	gui ne as, uineas.
Remainder \overline{z}	0	9					Rer	nain	der	6/	F	3	2		
Proof 3	1	6		,				Pro	of	0	6	3	ž	-	
5. From Take	1	0 8	2 7	3 9	6 1	7 2	4 8	2 4	3 5	10	7 6	9	8	1 3	0 2
Remainder	7	4	3	4	4	1	/	· F	1	/	2	-/	> /	>	<i>F</i>

6. From 3 7 5 1 dollars, take 1 6 7 4 dollars.

Write the less number under the greater, with units under units, &c. as the rule directs.

Thus, 3 7 5 1 1 6 7 4

Remainder 207/

8. From 10000000

7. From 2673105, the minuend, Take 178932, the fubtrahend.

Minuend 2 67 8 10 5
Subtrahend

494173

The distance of time since any remarkable event, may be found by sub-tracking the date thereof from the present year.

How long since the American Independence, which was declared in 1776?

1 8 1 0 present time. 1 7 7 6 date of the Ind.

Ans. 3 4 years since.

So, likewise, the distance of time from the occurrence of one thing to that of another, may be found by subtracting the date of the thing first happening, from that of the last.

How long from the discovery of America, by Columbus, 1492, to the commencement of the war, 1775, which gained our Independence?

1 7 7 5 1 4 9 2 Ans. 2 8 3 years.

Supplement to Subtraction.

QUESTIONS.

- 1. What is Simple Subtraction?
- 2. How many numbers must there be given to perform that operation?
- 3. How must the given numbers be placed?
- 4. What are they called?
- 5. When the figure in the lower number is greater than that of the upper number, from which it is to be taken, what is to be done?
- 6. How does it appear, that in fubtracting a less number from a greater, the occasional borrowing of ten, does not affect the difference between these two numbers?
- 7. How is Subtraction proved?
- So When, and how may Subtraction be of use to a man engaged in the pursuits of life?

EXERCISES.

1. What is the difference between 78360 and 5841?

72419

2. From a piece of cloth that meafured 691 yards, there were fold 278 yards; how many yards should there remain?

Ant.

278

Nore. In case of borrowing ten, it is a matter of indifference, as it respects the operation, whether we suppose 10 to be added to the upper figure, and from the sum subtract the lower figure and set down the difference; or as Mr. Pike directs, first, subtract the lower figure from 10, and adding the difference to the figure above, set down the sum of this difference and the upper figure. The latter method may, perhaps, be thought more easy, but it is conceived, that it does not lead the understanding of youth so directly into the nature of the operation as the former.

3. There are two numbers whose difference is 3 7 5, the greater number is 8 6 2; I demand the less? Ans. 487.

862 375 487 4. What number is that, which taken from 1 7 5 leaves 96?

Ans. 79.

175

5. The capture of Gen. Burgovne and his army happened in the year 1 7 7 7, that of Cornwallis in 1 7 8 1; how many years between these events?

Ans. 4 years.

1781

6. Suppose you should lend a neighbor 2 7 6 5 dollars at a certain time, and he should pay you 973 at another; how much would remain due?

Ans. 1 7 9 2 dollars.

2765

7. Supposing a man to have been born in the year 1 7 4 5, how old was he in 1 7 9 9?

Ans. 5 4 years.

1799

8. What number is that to which if you add 7 8 9 it will become 6 3 5 0?

Ans. 5 5 6 1.

5561

9. Suppose a man to have been 63 years old in the year 1 8 0 1; in what year was he born?

Ans. In the year 1 7 3 8.

10. King Charles, the martyr, was beheaded, 1 6 8 4, how many years is it fince?

1674

8

8

8

8

§ 3. Simple Multiplication.

SIMPLE MULTIPLICATION teaches, having two numbers given of the same denomination, to find a third which shall contain either of the two given numbers as many times as the other contains a unit.-Thus, 8 multiplied by 5, or 5 times 8 is 40.—The given numbers (8 and 5) spoken of together are called *Fallors*. Spoken of separately, the first or largest number, (8) or number to be multiplied, is called the Multiplicand; the less number, (5) or number to multiply by, is called the Multiplier, and the amount, (40) the Product.

This operation is nothing else than the addition of the same number several times repeated. If we mark 8 five times underneath each other and add them, the fum is 40, equal to the product of 5 and 8 But as this kind of addition is of frequent multiplied together. and extensive use, in order to shorten the operation, we mark down the number only once, and conceive it to be repeated as often as there are units in the multiplier.

Before any progress can be made in this rule, the following Table

must be committed perfectly to memory.

MULTIPLICATION TABLE.

1 2 3 4 5 6 7 8	9	10	111	12
2 4 6 8 10 12 14 16	18	20	22	24
3 6 9 12 15 18 21 24	27	30	33	36
4 8 12 16 20 24 28 32	36	40	44	48
5 10 15 20 25 30 35 40	45	<i>5</i> 0	55	60
6 12 18 24 30 33 42 48	54	60	66	72
7 14 21 28 35 42 49 56	63	70	77]	84
8 16 24 32 40 48 56 64	72	80	88	96
9 18 27 36 45 54 63 72	81	90	99	108
10 20 30 40 50 60 70 80	90	100	110	120
11 22 33 44 55 66 77 88	99	110	121	132
12 24 36 48 60 72 84 96	108	120	132	144

By this Table the product of any two figures will be found in that square which is on a line with the one and directly under the other. Thus, 56, the product of 7 and 8, will be found on a line with 7 and under 8: so 2 times 2 is 4; 3 times 3 is 9, &c. In this way the table must be learned and remembered.

RULE.

1. Place the numbers as in Subtraction, the larger number uppermost with units under units, &c. then draw a line below.

2. When the multiplier does not exceed 12, begin at the right hand of the multiplicand, and multiply each figure contained in it by the multiplier, fetting

down all over even tens, and carrying as in addition.

3. When the multiplier exceeds 12, multiply by each figure separately, first by the units of the multiplier, as directed above, then by the tens, and the other figures in their order, remembering always, to place the first figure of each product directly under the figure by which you multiply; having gone through in this manner with each figure in the multiplier, add their several products together, and the sum of them will be the product required.

EXAMPLES.

1. Multiply 5 2 9 1 by 3

Operation.

5 2 9 1 Multiplicand.

3 Multiplier.

1 5 8 7 3 Product.

2. Multiply 3 6 0 2 by 12

Operation.
3 6 0 2
1 2

4 3 2 2 4

The numbers being placed as feen under the operation, fay—3 times 1 is 3; which fet down directly under the multiplier; then 3 times 9 is 27; fet down 7 and carry 2. Again, 3 times 2 is 6, and 2 I carry is 8; fet down 8; then lastly, 3 times 5 is 15, which fet down, and the work is done.

The numbers being properly placed, proceed thus, 12 times 2 is 24, fet down 4 and carry 2; 12 times 0 is nothing, but 2 I carried is 2, which fet down; then 12 times 6 is 72, fet down 2 and carry 7; lastly, 12 times 3 is 36, and 7 I carried is 43, set down the whole number.

5. What is the product of 4175 multiplied by 37?

Place the factors thus,

4 1 7 5 Multiplicand.

3 7 Multiplier.

2 9 2 2 5 Product by the units (7) of the multiplier.
2 5 2 5 Product by the tens (3)

1 5 4 4 7 5 Product or answer.

In this example, as the Multiplier exceeds 12, therefore, you must multiply by each figure separately. First, by the units (7) just in the manner of the other examples. Secondly, by the tens (3) in the same way excepting only, that the first figure of the product in the multiplication by 3, must be placed under the 3, that is, under the figure by which you multiply. Lastly, add these two products together, the sum of them is the answer.

PROOF.

Multiplication may be proved by Division, but a method more concise

and easy, often practised by accountants, and which I shall recommend, is called

Casting out the 9's.

Casting out the 9's from any sum or number, is the exhausting of that number by the figure 9, till there is nothing left of it but a remainder, or excess over even nines, which remainder or excess is the thing sought.

How to cast out the 9's.

Whatever method may be adopted, this in effect, is nothing else than dividing the number by 9. The operation, however, would be tedious, as naturally practised by division; besides, as yet, we do not suppose the learner acquainted with it. A shorter and more successful way is the following

METHOD.

Beginning at the right hand of the number, add the figures, and when the fum exceeds 9, drop the fum and begin anew by adding, first, the figures, which would express it. Pass by the nines, and when the sum comes out exactly 9, neglect it; what remains after the last addition will be the remainder sought.

EXAMPLES.

If it be required to cast the 9's out of 576894, proceed thus;—5 to 7 is 12; which sum (twelve) as it exceeds 9 you must drop, and begin anew, first add the figures (12) which would express twelve, saying 1 to 2 is 3, and (proceeding with the other figures, which remain to be added) 6 is 9, being

† This method of casting out the 9's succeds on a

PRINCIPLE,

That every § figure, in rifing from the place of units to that of tens, takes to itself the addition of 9 times its value. The same from tens to hundreds, &c.

Consequently, if any figure, for instance *4, be removed from units place and divided by 9, it will leave a remainder of 4; the same of any other ‡ figure, moved and divided by 9, it will leave a remainder of itself, and that only.

Therefore, if any †† number be divided by 9; or, the figures which express that number be added together, and the sum of them divided by 9, the remainder will be equal. § Made evident thus;—1 in the place of units is the expression of an individual or one, in the place of tens, (10) it is the expression of ten individuals or ones; therefore taking 1 (one) its signification in units place, from 10 (Tan) its signification in tens place, leaves 9, the increase of 1, or 9 times its value, in rising from the place of units to that of tens.

* 4 removed from units place by a cybber

* 4 removed from units place by a cypher is 40, which divided by 9 haves 4 (4 times 9 is 36.)

† 6 removed by a cypher is 60, which divided by 9 leaves a remainder of 6; or 600 divided by 9, fill the remainder is 6, the remainder always begins the same figure whatever may be the place of its removal if divided by 9.

†† Thus, 5683 divided by 9, the remainder is 4; let the figures which express the number 5683 be added together—5 to 6 is 11 and 8 is 19 and 8 is 22, which number (22) divided by 9 leaves a remainder of 4, the same as when the number 5683 was divided by 9.

These properties of the figure 2 belong to none other of the Digits, excepting to the figure 3, and this figure (3) possesses them in consequence only of being an even part of 9.

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exally nine, neglect it, and begin again; 3 to 9 is tweive; again, drop the fum (twelve) and add the figures (12) which would express it, 1 to 2 is 3 and 4 is 7, which fum (7) is the remainder after the last addition, or the thing fought, and is the remainder that would be left after dividing the fum 576394 by 9.

To prove Multiplication.

Cast the 9's out of the Multiplicand by the foregoing method, and mark down the remainder; cast the 9's out of the Multiplier, mark the remainder, then multiply the remainder first obtained by this last remainder, and cast the 9's out of the product; also, cast the 9's out of the unswer or product of the Multiplicand and Multiplier, then if these two last remainders correspond, the work is supposed to be right.

EXAMPLES.

Let 7 6 5 3 0 2 be multiplied by 65.

Cast out the 9's from 7 6 5 3 0 2 Remainder 5 Remainders multiplied together.

3 8 2 6 5 1 0 - 9's from 10 Rem. 1 Corresponding with each other.

9's out of 4 9 7 4 4 6 3 0;

Remainder 1

Proof

There is nothing more easy than proving multiplication by this method so soon as the scholar shall have given it such attention, as to make it a little familiar.

nnar. Note. Should the Multiplier or Multiplicand, either or both, be lefs than

9, they are to be taken as the remainders.

4. Multiply 6 2 3

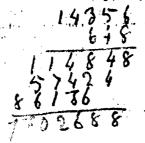
The examples which follow are to be wrought and proved according to the illustrations already given.

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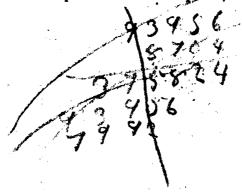
5. Mult. 3 7 8 4 67 By 2 3 5 Product, 8893910

SECT. I. 3. SIMPLE MULTIPLICATION.

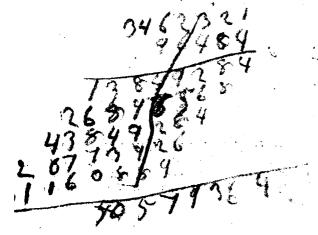
6. What is the product of 14356 multiplied by 648? Ans. 9302688



7. What is the product of 93956 multiplied by 8704? Ans. 817793024



8. Multiply 3 4 6 2 3 2 1 By 9 6 4 8 4 Product, 334058579364



Contractions and Varieties in Multiplication.

Any number which may be produced by the multiplication of two or more numbers, is called a composite number. Thus 15 which arises from the multiplication of 5 and 3 (3 times 5 is 15) is a composite number; and these numbers, 5 and 3, are called component parts. Therefore,

1. If the Multiplier be a composite number, multiply first by one of the component parts, and that product by the other; the last product will be the an-

` **fwe**r fought.

EXAMPLES.

I. Multiply 6 7 by 1 5.

6 7

5 one of the component parts.

3 3 5

3 the other component part.

1 0 0 5 Product of 67 multiplied by 15.

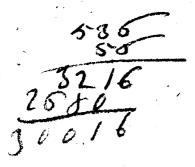
2: Multiply 367 by 48, Product, 17616.

OPERATION.

Confider first, what two numbers multiplied together will produce 48; that is, what are the component parts of 48? Answer, 6 and 8 (6 times 8 is 48) therefore, multiply 367 first by one of the component parts, and the product thence arising by the other; the last product will be the answer sought.

3. Mult. 583 by 56. Prod. 32648.

4. Mult. 1086 by 72. Prod. 78192. OPERATION.



^{2.} When there are cyphers on the right hand of either the Multiplicand or Mus"tiplier, or both, neglect those cyphers; then place the fignificant figures under one another, and multiply by them only; add them together, as before
directed, and place to the right hand as many cyphers as there are in both
factors."

EXAMPLES.

1. Multiply 65430 by 5200 OPERATION.

6 5 4 3 0 5 2 0 0

Here in the multiplication of 65430 by 5200, the cyphers are feen neglected, and regard paid only to the fignificant figures. To the product are prefixed 3 cyphers; equal to the number of cyphers neglected in the factors.

3 4 0 2 3 6 0 0 0

2. Mult. 3 6 5 0 0 By 7 3 0 3. Mult. 78000 by 600. Product, 46800000.

Prod. 2 6 6 4 5 0 0 0

3. When there are cyphers between the fignificant figures of the Multiplier, omit the cyphers, and multiply by the fignificant figures only, placing the first figure of each product directly under the figure by which you multiply, and adding the products together, the fum of them will be the product of the given numbers.

EXAMPLES.

T. Mult. 154326 by 3007.

1 5 4 3 2 6

3007

 $\begin{array}{c} \overline{1080282} \\ 462978 \end{array}$

464058282

In this example, the cyphers in the multiplier are neglected, and 154326 multiplied only by 7 and by 3, taking care to place the figure in each product directly under the figure from which it was obtained.

2. 3 4 5 7 3 0 2 3. 4 8 9 7 6 8 5 0 4 0 0 0 3 0

1 9 5 9 2 2 0 9 3 0 5 5 0 0

4. When the Multiplier is 9, 99, or any number of 9's, annex as many cyphers to the Multiplicand, and from the number thus produced, subtract the multiplicand, the remainder will be the product.

EXAMPLES.

1. Mult. 6547 by 999. OPERATION.

6 5 4 0 4 5 3

Write down the Multiplicand, place as many cyphers at the right hand as there are 9's in the multiplier for a minuend, underneath write again the multiplicand for a fubtrahend, subtract, and the remainder is the product of 6547 multiplied by 999.

2. 3, Product, 640827 7 0 2 1 7 Prod. 695079 9 9

5 5 8 4 9 7 6 Prod. 53844375024.

Supplement to Multiplication.

QUESTIONS.

- ▶ What is Simple Multiplication ?
- 2. How many numbers are required to perform that operation?
- 3. Collectively, or together, what are the given numbers called?
- 4. Separately, what are they called?
- 5. What is the refult, or number fought, called?
- 6. In what order must the given numbers be placed for multiplication?
- 7. How do you proceed when the multiplier is less than 12?
- 8. When the multiplier exceeds 12, what is the method of procedure?
- 9. What is a composite number?
- 10. What is to be understood by the component parts of any number?
- 11. How do you proceed when the multiplier is a composite number?
- 12. When there are cyphers on the right hand of the multiplier, multiplicand, either or both, what is to be done?
- 13. When there are cyphers between the fignificant figures of the multiplier how are they to be treated?
- 14. When the multiplier confifts of 9's, how may the operation be contracted?
- 15. How is Multiplication proved?
- 16. By what method do you proceed in casting out the 9's from any number?
- 17. How is, Multiplication proved by casting out the 9's?
- 18. Of what use is Multiplication?

EXERCISES.

1. What fum of money must be divided between 27 men so that each may receive 115 dollars?

Ans. 3105.

Note. The scholar's business in all questions for Arithmetical operations, is wholly with the numbers given; these are never less than two; they may be more; and these numbers, in one way or another, are always to be made use of to find the answer. To these therefore, he must direct his attention, and carefully consider what is proposed by the question, to be known.

er i destre titt dit itee e tel

- 2. An army of 10700 men having plundered a city, took so much money, that when it was shared among them, each man received 46 dollars; what was the sum of money taken?

 Ans. 492200
- 3. There were 175 men employed to finish a piece of work, for which each man was to receive 18 dollars; what did they all receive?

Ans. 2275

- 4. There is a certain town which contains 145 houses, each house two families, and each family 6 inhabitants; how many are the Inhabitants of that town.

 Ans. 1740
- 5. If a man earn 2 dollars per week, how much will he earn in 5 years, there being 52 weeks in a year?

 Ans. 520 dollars.

- 6. How much wheat will 36 men thrash in 37 days, at 5 bushels per day, each man? Ans. 6660 bushels.
- 7. If the price of wheat be 1 dollar per bushel and 4 bushels of wheat make 1 barrel of flour, what will be the price of 175 barrels of flour?

 Ans. 760 dollars.

§ 4. Simple Divigion.

SIMPLE DIVISION teaches, having two numbers given of the fame denomination, to find how many times one of the given numbers contains the other. Thus, it may be required to know how many times 21 contain 7, the answer is 3 times. The larger number (21) or number to be divided, is called the Dividend; the less number, (7) or number to divide by, is called the Divisor; and the answer obtained, (3) the Quotient.

After the operation, should there be any thing left of the dividend, it is called the *Remainder*. This part, however, is uncertain; sometimes there is no remainder. When it does happen, it will always be less than the divisor,

if the work be right, and the same name with the dividend.

RULE.

1. "Affume as many figures on the left hand of the dividend, as contain "the divifor once or oftener; find how many times they contain it, and "place the answer as the highest figure of the quotient.

2. "Multiply the divisor by the figure you have found, and place the

. " product under that part of the dividend from which it was obtained.

3. "Subtract the product from the figures above it.

4. "Bring down the next figure of the dividend to the remainder, and di-

" vide the number it makes up as before."

When you have brought down a figure to the remainder, if the number it makes up be still less than the divisor, a cypher must be placed in the quotient, and another figure brought down.

EXAMPLES.

1. Divide 127 by 5.

Divisor. Dividend. Quotient.

5) 127 (25

2 7 2 5 The parts in Division are to stand thus, the dividend in the middle, the divisor on the left hand, the quotient on the right, with a half parenthesis separating them from the dividend.

2 Remainder.

Proceed in this operation thus.—It being evident that the divisor (5) cannot be contained in the first figure (1) of the dividend, therefore, assume the two sirst figures (12) and inquire how often 5 is contained in 12, finding it to be 2 times, place 2 in the quotient, and multiply the divisor by it, saying 2 times 5 is 10, and place the sum (10) directly under 12 in the dividend. Subtract 10 from 12, and to the remainder (2) bring down the next figure (7) at the right hand, making with the remainder (2) 27. Again inquire how many times 5 in 27; 5 times; place 5 in the quotient, multiply the divisor; (5) by this last quotient figure (5) saying, 5 times 5 is 25, place the sum (25) under 27, subtract, and the work is done. Hence it appears that 127 contains 5, 25 times, with a remainder of 2, which was left after the last subtraction.

This Rule, perhaps, at first will appear intricate to the young student, although it is attended with no difficulty. His liability to errors will chiefly arise from the diversity of proceedings. To assist his recollection let him notice, that

The steps of Division are four

2. Multiply.

3. Subtract.

4. Bring down:

It is sometimes practised to make a point (.) under the figures in the Div-

idend, as they are brought down, in order to prevent mistakes.

When the divifor is a large number, it cannot always certainly be known how many times it may be taken in the figures which are assumed on the left hand of the dividend till after the first steps in division are gone over, but the learner must try so many times as his judgment may best distate, and after he has multiplied, if the product be greater than the number assumed, or that number in which the divisor is taken, then it may always be known that the quotient figure is too large, if after he has multiplied and subtracted, the remainder be greater than the divisor, then the quotient figure is not large enough, he must then suppose a greater number of times, and proceed again. This at first may occasion some perplexity, but the attentive learner after some practice, will generally hit on the right number.

2. Let it be required to divide 7012 by 52.

Remainder.

OPERATION.

Divifor. Dividend. Quotient.
5 2) 7 0 1 2 (1 3 4 5 2 1 8 1 1 5 6 2 2 0 8

In this operation it is left for the scholar to trace the steps of procedure without having them particularly pointed out to him by words.

PROOF.

Division may be proved by multiplication.

RULE.

"Multiply the Divisor and Quotient together, and add the remainder, if there be any, to the product; if the work be right, the sum will be equalto the Dividend."

Take the last example.

The Quotient was 1347
The Divisor 52

52 Multiply them together.

268 670

44 Remainder added.

7012 Equal to the Dividend.

Another and more expeditious way of proving division is

By casting out the 9's.

Cast out the 9's from the Divisor and the Quotient, multiply the results, and to the product add the remainder if any after division; from the sum of these cast out the 9's, also cast out the 9's from the Dividend, and if the two staff results agree, the work is right.

```
3. Divide 17354 by 86.

OPERATION.

PROOF.

15

Rem. 5 \ Multiplied to-

Quot.) 201. Rem. 3 \ gether.

15

Remainder 68 added.

9's out of 83 Rem. 2 \ Agreeing

9's out of (Divid.) 17354 Rem. 2 \ together.
```

4. Divide 153598 by 29. Quotient, 5296. Rem. 14 OPERATION. 29)153598(

5. Divide 30114 by 63. Quotient, 478

6. Divide 974932 by 365. Quotient, 2671. Remainder, 17.

7. Divide 3228242 dollars equally among 563 men; how many dollars must each man receive?

Am. 5734

From a view of the question it is evident, that the dollars must be divided into as many parts as there are men to receive them; consequently the number of dollars must be made the dividend, and the number of men the divisor; the quotient will then shew how many dollars each man must receive: 8. How many times does 1030603615 contain 3215? Ans. 320561 times.

Contractions and Varieties in Division.

1. When the Divisor does not exceed 12, the operation may be performed without setting down any figures excepting the quotient, by carrying the computation in the mind. The units which would remain after subtracting the product of the quotient figure and the divisor from the figures assumed of the dividend, must be accounted so many tens, and be supposed to stand at the left hand of the next figure in the dividend, then consider again how often the divisor may be had in the sum of them. Proceed in this way till all the figures in the dividend have been divided. This is called Short Division.

EXAMPLES.

1. Divide 732 by 3 OPERATION.

5) 7 3 2 (2 4 4

Here I say, how often 3 in 7; knowing it to be 2 times, I place 2 in the quotient, then considering that the quotient figure (2) and the divisor (3) multiplied together would be 6, and that this product (6) sub-

tracted from 7, in the dividend, would leave 1, I then consider this remainder (1) as standing at the left hand of the next figure (3) of the dividend, which together make 13. I now say, how many times 3 in 13—4 times, therefore I place 4 in the quotient, which multiplied into the divisor (3) would be 12, and 12 subtracted from 13 would leave 1, which considered as standing at the left hand of the next or last figure (2) of the dividend, would make 12; again, how many times 3 in 12—4 times—I then place 4 in the quotient, which multiplied into the divisor (3) is 12; this product (12) I consider as subtracted from 12, I find there will be no remainder, and the work is done.

Note. The quotient may stand as it is seen in the example, or it may be placed under the dividend, thus,

3) 7 3 2

2. Divide 37426 by 7.

OPERATION.
7) 3 7 4 2 6

Quotient, 5 3 4 6 Rem. 4.

Here I fay, how often 7 in 37? 5 times and 2 remain; then how often 7 in 24? 3 times, and 3 remain; how often 7 in 32? 4 times and 4 remain, lastly, how often 7 in 46? 6 times and 4 remain.

3. Divide 12363 by 5. Quot. 2472. Rem. 3.

4. Divide 602571 by 8. Quot. 75321. Rem. 3.

2. When there are typhers at the right hand of the Divisor, cut them off, also, cut off an equal number of figures from the right hand of the dividend, and place these figures at the right hand of the remainder.

EXAMPLES.

1. Divide 6203916 by 5700.

OPERATION.

57 | 00)62039 | 46(1088

57 ...

503

456

479

456

2346 Rem.

Here are two cyphers on the right hand of the divisor, which I cut off; also, I cut off two figures (46) from the dividend, and to the right hand of the remainder after the last division (23) I place the figures cut off from the dividend (46) which make the whole remainder 2346. 2. Divide 379432 by 6500. Quot. 58. Rem. 2432.

3. Divide 2764503721 by 83000. Quot. 83307. Rem. 22721.

3. When the divisor is 10, 100, 1000, or 1, with any number of cyphers annexed, cut off as many figures on the right hand of the dividend as there are cyphers in the divisor; the figures which remain of the dividend compose the quotient; those cut off, the remainder.

EXAMPLES.

- 1. Divide 1576 by 10. OPERATION.
 1 | 0 | 1 | 5 | 7 | 6
- 2. Divide 3217 by 100.

OPERATION.

Quot. Rem. 1 | 0 0)3 2 | 1 7

Here we have one cypher in the divifor; therefore, cut off one figure (6) from the dividend; what remains, (157) is the quotient, and the figure cut off (6) the remainder.

Supplement to Division.

QUESTIONS.

xxx: :: :xxx =

- 1. What is Simple Division?
- 2. How many numbers must there be given to perform that operation?
- 3. What are the given numbers called?
- 4. How are they to stand for Division?
- 5. How many steps are there in Division?
- 6. What is the first? the second? the third? the fourth?
- 7. What is the refult or answer called?
- 8. Is there any other, or uncertain part pertaining to Division? What is it called?
- 9. Of what name or kind is the remainder?
- 10. What is fhort Division?
- 11. When there are cyphers at the right hand of the Divisor, what is to be done?
- 12. What do you do with figures cut off from the Dividend when there are cyphers cut off from the Divifor?
- 13. When the Divisor is 10, 100, or 1 with any number of cyphers annexed, how may the operation be contracted?
- 14. How many ways may Division be proved?
- 15. How is Division proved by Multiplication?
- 16. How may Division be proved by casting out the 9's?
- 17. Of what use is Divition?

EXERCISES.

1. Suppose an estate of 36582 dollars to be divided among 13 sons, how much would each one receive?

Ans. 2814 dollars.

An army of 15000 men having plundered a city, and took 2825000 dollars? what was each man's share?
 Ans. 175 dollars.

- 3. A certain number of men were concerned in the payment of 18950 dollars, and each man paid 25 dollars, what was the number of men?

 Ans. 758.
- 4. If 7412 eggs be packed in 34 casks, how many in a cask?

 Ans. 218.

- 5. A farm of 375 acres is let for 1125 dollars, how much does it pay per acre?

 Ans. 3 dollars.
- 6. A field of 27 acres produces 675 bushels of wheat; how much is that per acre? Am. 25 bushels.

- 7. Supposing a man's income to be 2555 dollars a year; how much is that per day, there being 365 days in a year? Ans. 7 dollars.
- 8. What number must I multiply by 19, that the product may be \$713 Ans. 67.

§ § 5. Compound Addition.

COMPOUND ADDITION is the adding of numbers, which confift of articles of different value, as pounds, thillings, pence, and farthings, called different denominations; the operations are to be regulated by the value of the articles which must be learned from the Tables.

RULES FOR COMPOUND ADDITION.

1. Place the numbers fo that those of the same denomination may stand di-

really under each other.

2. Add the first column or denomination together, and carry for that number which it takes for the same denomination to make 1 of the next higher. Proceed in this manner with all the columns, till you come to the last, which must be added as in Simple Addition.

1. OF MONEY.

TABLE.

4 Farthings qr. make one Penny, marked d. Shilling, s. Pound, s.

EXAMPLES.

1. What is the fum of £61 17s. 5d.—£13 3s. 8d.—and of £5 16s. 11d. when added together?

OPERATION.

I begin with the right hand column or that of pence, and having added it, find the fum of the numbers therein contained to be 24; now as 12 of this denomination make one of the next higher, or in other words, 12 pence make one shilling, therefore in this, or in the column of pence I must carry for 12; I now inquire how often 12 is contained in 24, the sum of the first column or that of pence; knowing it to be 2 times and nothing over, I set down 0 under the column of pence, and carry 2 to that of shillings, to be added into the second column, saying 2 I carry to 6 is 8, and 3 is 11, and 7 is 18, and 10 to 18 is 28, and 10 again is 38 (for so each figure in ten place must be reckoned, I in that place being equal in value to 10 units.) Now as 20 shillings make one pound, therefore, in the column of shillings, I carry for 20; I then inquire how often 20 in 38? once, and 18 remains; therefore, I set down directly under the column of shillings 18, what 38 contains more than 20, and for the even 20 carry I to pounds or the last column, which is to be added after the manner of Simple Addition.

Note. The method of proof for Compound Addition is the same as that

of Simple Addition.

Z			· 3			
6. s. d. gr.		£.	s	d.	gr.	
		371	15	6	2	
6 1 5 3 0		5	7		0	
8 1 7 3		68	3	2	1	
		7	. 0	5	3	
t.						
•	•					
						
				`		
	•			`		
	•			•		

	_
1802. May 14, pays for a dinner 60 1	6
for oats for his horse - 0 0	6
for fling 0 1	2
15, for supper and lodging - 0 2	0
for horse keeping - 0 1 1	0
for bitters 0 1	6
for breakfast 0 2	0
to the barber for dreffing 0 1	6
for dinner again and other re-	
freshment 0 3	5

What were the gentleman's expenses?

5.	Suppo	ſe I	am	indebted	
----	-------	------	----	----------	--

1. s. d.

To A. Thirty two pounds, fourteen shillings and ten pence.

- B. Forty one pounds, fix shillings and eight pence.
- C. Seventy five pounds, eight shillings.
- D. Three pounds and nine pence.

How much is the debt?

	 _	-	
Ans.			

6. A man purchases cattle; one yoke of oxen for £14 11 6; four cows for £18 19 7; and other stock to the amount of £21 5; what was the amount of the cattle purchased?

Ans. £54 16 1

2. OF TROY WEIGHT.

By Troy Weight are weighed gold, filver, jewels, electuaries and liquors.

TABLE.

24	Grains grs.)	(Penny	weight,	marked	pwt.
. 2 0	Penny weights	- make	one <	Ounce,	, `.		OZ.
	Ounces .)		Pound	, ,		lb.

EXAMPLES.

	15	•	
l b.	OZ.	pwts.	grs.
70	10	I 3	grs. 4
3	9	7	16
28	0	0	- · 5
7	3	6	2
			
•			

Because 24 grains make a penny weight, you carry one to the penny weight column for every 24 in the sum of the column of grains; because 20 penny weights make 1 ounce, you carry for 20 in pennyweights, and because 12 ounces make one pound, you carry for 12 in the ounces. This is called carrying according to the value of the higher place.

				2,	
		lb.		QΖ.	pwts.
1	1	lb. 6	1	7	19
			6	5	6
		2	8	O	14
			,	3	`7
_					

	3.	
oz.	pwts.	grs.
7	1 4	23
2	0	6
1	13	5
0 .	12	7
	7 2 1	7 1 4 2 0 1 3

Note. The finencis of gold is tried by fire and is reckoned in carats, by which is understood the 24th part of any quantity; if it lose nothing in the trial, it is faid to be 24 carats fine; if it lose 2 carats, it is then 22 carats fine, which is the standard for gold.

ĺb.

Silver which abides the fire without loss is faid to be 12 ounces fine. The ftandard for filver coin is 11 oz. 2 pwts. of fine filver, and 18 pwts. of cop-

per melted together.

2

1 1

3. OF AVOIRDUPOIS WEIGHT.

By Avoirdupois weight are weighed all things of a coarse and drossy nature, as tea, sugar, bread, flour, tallow, hay, leather, and all kind of metals except gold and silver.

TABLE.

16 Drams dr.	1	Ounce,	mark	ed			oz.
16 Qunces		Pound,					lb.
28 Pounds	make one	Quarte	r of a	hundi	ed we	ight,	qr.
4 Quarters	1	100 we	ight,	or 112	poun	ď,	cwt.
20 Hund. weight	j	Ton,	_	-		—	T.
	EXAM	PLES.					
, ,	1						
T.	cwt.	qr.		lb.	. 0	z.	dr.
186	3 ·	2	2	5	1	1	. 8
4	1 7	0	2	3		7	6
9	8	3		7		2	5

1

16

	T.		ewt. 3	2 qr,	l b.	oz.	dr.
8	0	1	3	2	2 5	- 1 1 -	8
			19		14	5 ·	- 6
	8	6	2	O	6	0	15
		3	7		O	6	4

Note. "175 Troy Ounces are precifely equal to 192 Avoirdupois Ounces, and 175 Troy pounds are equal to 144 Avoirdupois. 1 lb. Troy=5760 grains and 1 lb. Avoirdupois=7000 grains."

4. OF TIME.

TABLE.

4 Weeks	make one	Minute, Hour, Day, Week, Month,	marked	m. h. d. w. mo.
13 Months, 1 d. & 1 h.		*Julian	Year,	mo. Y.

EXAMPLES.

Y.	mo.	w.	đ.	h.	m.	s.
16	10	. 3	6	2 3	57	43
28	7	2	5	16	28	3 2
39	6	1	3	1 7	38	11
8 7	4	0	1	14	1 5	17

			2			
Y.	mo.	w.	ď.	h.	m.	5.
89	1 1	3	6	2 2	4 5	36
3 6	1 0	2!	5	6	5 5	4 4
8 7	2	1	0	11	2 2	3 3
36	4	3	3	5	. 8	7

The number of days in each Calendar month may be remembered by the following verse.

Thirty days hath September, April, June and November; February twenty eight alone; all the rest have thirty one.

* "The civil Solar year of 365 days being short of the true by 5h. 48m. 57s. occasioned the beginning of the year to run forward through the season nearly one day in four years; on this account Julius Czsar ordained that one day should be added to February every fourth year, by causing the 24th day to be reckoned twice; and because this 24th day was the sixth (sextillis) before the kalends of March, there were, in this year, two of these sextiles, which gave the name of Bissextile to this year, which being thus corrected, was, from thence, called the Julian year."

5. OF MOTION.

				. <i>!</i>			
		•	LABLE	•			
60 Sec	conds	1	(Prin	ne Minute	, marked	" 1	
60 Mi	nutes	i	Deg		•	0	
30 De	grees	make o				S.	
12 Sig	gns, or 36		Γ_{i}	he whole	great cir	cle of th	ne Zo-
de	grees		Ιį	diac.	•	•	
	_	EX.	AMPLES	S.			
Q			· s	•	,	"	
25	17	1.8	9	8	5 5	44	
17	49	. 5 6	1	26	44	5 5	
6	3 5	24	8	18	36	12	
10	17	16	1	9	33	22	
·					, 		

6. OF CLOTH MEASURE.

•		T.	ABLE.	· ·		
2 Inches, and on 4 Nails, or 9 inc 4 Quarters of a 3 Quarters of a 5 Quarters of a 6 Quarters of a 4 Quarters, 1 inc 37 inches a 3 Quarters and t	hes yard, or yard, or yard, or yard, or ch and o	36 inches 27 inches 45 inches 54 inches ne fifth, or	make on	Yard, Ell-Fl Ell-En Ell-Fr Ell-Sc	marked er of a yard, emish, nglish, ench, cotch,	na. qr. yd. E. Fl. E. E. E. Fr.
		EX.	AMPLES.			*
Yds.	l qr.	n.		E. E.	2 qr.	n.
614	3	· 3		19	3	2
36	1	• 2	÷	<i>5</i> 6	1	3
· 7	O	11		7	2	2 .
1	· 2	O	•	6 3	O .	· 1
1 5	3	. 2		18	2	0
			, <u> </u>	,		
- 6					. &	

7. OF LONG MEASURE.

By Long Measure are measured distances, or any thing where length is considered without regard to breadth.

TABLE.

3 Barley corns bar.		Inch	marked	in.
12 Inches		Foot,		ft.
3 Feet		Yard,		yd.
5; Yards, or 16; feet		Rod, Per	ch, or Pole,	pol.
40 Poles	make one <	Furlong,		fur.
8 Furlongs -	make one	Mile,	/	mile.
69½ Statute miles nearly		? Circle.	of a great	ı
360 Degrees		SA greather Early	t Circle of rth.	deg.
_	EVAMBI	TC	* *	

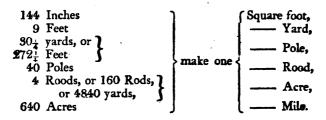
EXAMPLES.

Deg. 1 6 8	mi. 5 7	für. 7	1. pol. 2 6	ft. 1 <i>5</i>	in. 1 1	bar.
124	<i>5</i> 3	6	18	7	6	1
79	36	1 -	7	9	10	O
4.	7	3	0.	3	2	1

	•	2.			
Deg.	mi.	fur.	pol.	ft.	in.
1 3	<i>5</i> 6	5	13	8	1.
. 49	1-8	1	27	16	2
267	12	3	16	9	0
29	8	. 0	5	3	. 1
					

8. OF LAND OR SQUARE MEASURE.

By square measure are measured all things that have length and breadthe TABLE.



EXAMPLES.

. A	Acres	•	rood.	pol.	ft.	in.
3	7 6	5	. 3	3 6	93	121
5	6 8	3	1	27	58	7 6
. 2	4 7	, .	2	3 5	6 1	24

9. OF SOLID MEASURE.

By Solid Measure are measured all things that have length, breadth and thickness.

TABL	E.	
1728 Inches)	foot, Yard,
27 Feet 40 Feet of round timber, or		
50 feet of hewn timber	make one	Ton or Load,
128 folid feet, i. e. 8 in length 4 in breadth, and 4 in height	,	Cord of Wood.

EXAMPLES.

Ton.	ft.	in.	cord.	ft.	in.
6 5	3 71	229	` 3 9	1 1 8	1021
19	26	1207	3	<i>5</i> 6	4 3 7
3.6	1 7	5 4	18	72	6 5 9
5 7 ·.	3 ·8	6 ,	2 9	8 6	124

10. OF WINE MEASURE.

By Wine measure are measured Rum, Brandy, Perry, Cider, Mead, Vinegar and Oil.

TABLE.

9.	Pints pts.	1	(Quart, marked	qts.
4	Quarts		Gallon,	gal.
	Ğallons	ļ	Anchor of Brandy,	anc.
	Gallons	1	Runlet,	run.
317	Gallons	make one	Half a hogshead	lhhd.
42	Gallons		Tierce,	tier.
	Gallons		Hogshead,	hhd.
2	Hogsheads	. :	Pipe or Butt,	P. or B.
	Pipes		Tun,	Т.

EXAMPLES.

	1.	· · ·	
Hhd.	gal.	qts.	pts.
3 9	5 2	3	1
16	27	ľ	0
3 5	12	0 -	1
29	38	2	0
·		· · · · · · · · · · · · · · · · · · ·	

T.	hhd.	2. val.	qts.	pts.
3 6	2	gal. 5 8	3	1
3 5	1	3.6	1	0
1.7	0	29	2	1
23	2	1 2	. 1	σ
				<u> </u>

N. B. A PINT wine measure, is 287 cubic inches,

11. OF ALE OR BEER MEASURE.

		TABLE.			
2	Pints)	Quart,	marked	qts.
4	Quarts ·	İ	Gallon,		gal.
-8	Gallons	}	Firkin of A	le in London,	A. fir.
81	Gallons		Firkin of A	Ale or Beer	
Š	Gallons	make one	Firkin of I	Beer in London	B. fir.
2	Firkins	make one	Kilderkin,		Kill.
2	Kilderkins	Į.	Barrel,		Bar.
1:	Barrel, or 54 Gallons	1	Hogshead	of Beer,	hhd.
2	Barrels		Puncheon,		Pun.
3	Barrels or 2 hogsheads		Butt.		Butt.

EXAMPLES.

	1.	•		2.	
Hhd. 3 2 7	gal. 4-8	qts. 2	B.fr. 2 3	gal.	qts.
28	<i>5</i> _0	3	4 5	2	3
173	24	1	98	. 7	1
27	16	· · · · ·	9 6	8	. 0
			,		•
			*		
		 ,	- b		
		· ' .			

N. B. A pint, Beer measure, is 351 cubic inches.

6. OF DRY MEASURE.

By Dry Measure are measured all dry goods, such as Corn, Wheat, Seed, Fruit, Roots, Salts, Coal, &c.

	$\mathbf{T}A$	ABLE.	
2 Pints)	Quart, marked	qtş.
2 Quarts		Pottle,	pot.
2 Pottles		Gallon,	gal.
2 Gallons		Peck,	pk.
4 Pecks	1	Bushel,	bu.
2 Bushels	[Strike,	ſtr.
2 Strikes	make one	Coom,	co.
2 Cooms	1	Quarter,	qr.
4 Quarters ·	1	Chaldron,	ch.
		Chaldron in London,	
4½ Quarters 5 Quarters	.]	Wey,	wey.
2 Weys	Ĵ	Last,	lalt.

EXAMPLES.

1.					2.		
Bus.	pk.	qts.	pts.	Ch.	bus.	pk.	qts.
27	2	6	1	37	16	2	5
18	3	7	0	• 26	28	3	7
20	0	1	1	18	15	1	. 0
19	1	3	0	1 7	2 5	3	6

N. B. A gallon, Dry Measure, contains 2684 cubic inches.

The following are denominations of things counted by the Table.

- 12 particular things make 1 Dozen,
- 12 Dozen 1 Gross,
- 12 Gross or 144 dozen great Gross
- 20 Particular things make one Score.

Denominations of measure not included in the Tables.

- 6 Points make 1 Line,
- 12 Lines -- Inch,
- 4 Inches --- Hand,
- 3 Hands Foot,
- 66 Feet, or 4 Poles, a Gunter's Chain.
 - 3 Miles League.

A hand is used to measure Horses....A Fathom, to measure depths...A League, in reckoning distances at Sea.

N. B. A Quintal of Fish weighs 1 Cwt. Avoirdupois.

§ 6 Compound Subtraction.

COMPOUND SUBTRACTION teaches to find the difference between two fums of diverse denominations.

RULE FOR COMPOUND SUBTRACTION.

"Place those numbers under each other, which are of the same donominaof tion, the less being below the greater; begin with the least denomination, " and if it exceed the figure over it, borrow as many units as make one of the " next greater; fubtract it therefrom; and to the difference add the upper er figure, remembering, always to add one to the next superior denomination, " for that which you borrowed.

PROOF. In the same manner as Simple Subtraction.

I. OF MONEY.

1. Supposing a man to have lent £185 10s. 7d. and to have received at gain of his money, £93 15s. how much remains due?

			0:	PERÁ:	1 10	N.					4	<u>?</u> .	•
Lent Received		£. 8 9	5		s. 0	d. 7 0		. •	From Take	3	£. 1 0 8 £		s. 1 5
Due		9	1	***************************************	5	7			•				
Proof	ì	8	5	1	O	7	•		•.				

						5.
r		6			s.	d.
Lent	6	3	7	1	7.	8
		1	6	3	2	5
Received	1		7	8	4	
at c	₹		Ì	9	1 5	1 1
Sundry times.	1	1	3	9	6	8
times.	L ₃	2	6	1	1	4

The feveral payments must first be added together, and their fum fubtracted from the fum lent.

Rec	eived :	in
~	all	
		
Yet	due	

54

4. A certain man fold a lot of land for \$\times 735 11 6; he received at one time £61 5; at another time, £195 13 11 how much is there yet due?

Ans. £478 12 7.

2. OF TROY WEIGHT.

		1.					2.	
From Take	1b. 7 6 3	oz. 8 9	pwt. 1 6 1 7.	gr. 1 3 6	1	b. 7 2	oz. 3 8	pwt. 5 9
Remains					· /s		Š. ja	
Proof				1		e e		

3. OF AVOIRDUPOIS WEIGHT.

	′ 1.		ν.	2)			
	oz.		T.	cwt.	qr.	1ь.	oz.	dr.
9	15	5	6	1 1	ĩ	14	7	3
5	6	7 .	1 .	5	1	16	9	8

4. OF TIME.

(ı.		A			
Y.	me.	w.	d.	h.	m.	s.		
89	6	3	6 .	20	44	55		
1 6	9	1	2	18	59	57		

5. OF MOTION.

	1.	
b ·	į.	"
16	27	3 3
8	3 . 4	23

s	. 0	,
6	8	5 1
3	9	57

6. OF CLOTH MEASURE.

	1.	
Yds.	qr.	n
27	ĩ	2
,16	1	3

	z.	
E. E.	qr.	n.
2 6	2	1
17	3	2

7. OF LONG MEASURE.

D	•	C	1.		c.	•	1
⊥⁄eg.	mı.	r.	p.	yas.	II.	ın.	Dar.
5 6	13	5	26	2	1	8	1
17	15	2	27	yds. 2 1	2.	9	2

8. OF LAND OR SQUARE MEASURE.

1.			2.			
A.	R.	pol.	pol.	ft.	in.	
17	3	17	Ì 8	16	11	
16	1,	16	10		130	
-						

9. OF SOLID MEASURE.

1.			2.				
Tons.	ft.	in.	Cords.	ft.	in.		
45	29	186	68	23	810		
19	34	1 3 72	6	1 2 7	1529		

10. OF WINE MEASURE.

1	l.		2.		
Hhd.	. gal.	qts,	Hhd.	Tun.	gal.
6 6	Š 1	2	75	1	1 6
17	9 9	· · 3	2 4	1	4 3

11. OF ALE AND BEER MEASURE.

	1.				2.	
Hhd.	gal.	qts.		Butt.	hhd.	gal.
89	ĭ 9	2		6 3	1	Ī 6
3 7	25	3		29	1	10
			• •			

12. OF DRY MEASURE.

Bu.	pk.	qts.			Chal.	bu.	pk.
6 1	1	2		•	171	1 8	l
5	1	4			76	22	2
			•				· ·

SCHOLAR'S ARITHMETIC.

OBSERVATIONS.

THE Scholar has now surveyed the ground work of Arithmetic. It has before been intimated, that the only way in which numbers can be affected is by the operations of Addition, Subtraction, M stiplication and Division. These rules have now been taught him, and the exercises in a supplement to each suggest their use and application to the purposes and concerns of life. Further, the thing needful, and that which distinguishes the Arithmetician, is to know how to proceed by application of these four rules to the solution of any arithmetical question. To afford the Scholar this knowledge is the object of all succeeding rules.

SECTION II.

Rules effentially necessary for every person to fit and qualify them for the transaction of business.

These are nine: REDUCTION, FRACTIONS,* FEDERAL MONEY, INTEREST, COMPOUND MULTIPLICATION, COMPOUND DIVISION, SINGLE RULE OF THREE, BOUBLE RULE OF THREE and PRACTICE.

A thorough knowledge of these rules is sufficient for every ordinary occurrence in life. Short of this a person in any kind of business, will be liable to repeated embarrassments. It is the extreme usefulness of these rules which commends them to the attention of every Scholar.

^{*} Fractions are taken up here no further than is necessary to shew their signification, and to illustrate the principles of REDERAL MONEY.

1. Reduction.

"REDUCTION teaches to bring or exchange numbers of one denomi-" nation to others of different denominations, retaining the fame value."

It is of two kinds.

1. When high denominations are to be brought into lower, as pounds into shillings, pence, and farthings; it is then called REDUCTION DESCENDING, and is performed by Multiplication.

2. When lower denominations are to be brought into higher, as farthings into pence, or into pence, shillings and pounds; it is then called REDUCTION AS-CENDING, and is performed by Division.

REDUCTION DESCENDING.

RULE.

Multiply the highest momination by that number which it takes of the next less to make one of that greater; so continue to do, till you have brought it as low as your question requires.

PROOF. "Change the order of the question, and divide your last prod-

uct by the last multiplier, and fo on."

EXAMPLES.

1. In £17 13s. 6d. 3qrs. how many farthings?

7. s. d. 1.3 6

2 0 Shillings in a pound.

3 5 3 Shillings in £17 13s. 1 2 Pence in a shilling.

4 2 4 2 Pence in £17 13s. 6d.

A. 1 6 9 7 1 Farthings.

In this example, the highest denomination is pounds, the next less, is shillings, and because 20 shillings make one pound therefore I multiply £17 by 20, increasing the product by the addition of the given shillings (13) which it must be remembered, must always be done in like cases; then, because 12 4 Farthings in a penny. pence make one shilling, I multiply the faillings, (353) by 12, adding in the given pence (6d.) lastly because 4 farthings make one penny, I multiply the

pence (4242) by 4 and add in the given farthings (3qrs.) I then find, that in £17 13s. 6d. 3qrs. there are 16971 farthings.

4) 16971 12) 4 2 4 2 3qrs.

20) 3 5 3 6d.

£17 13s.

PROOF.

To prove the above question change the order of it, and it will stand thus; in 16971 farthings how many pounds?

Divide the last product by the last multiplier, the remainder will be farthings. Proceed in this way till all the steps of the operation have been retraced back; the last quotient with the remainders will be proof of the accuracy of the operation if they agree with the fum given in the question.

2. In £7 14s. 6d. 1qr. how many 3. In £7 6s. 4d. how many pence? farthings?

An. 7417 qrs.

Ans. 1756d.

- 4. In 29 Guineas, at 28s. how many farthings? Ans. 38976 qrs.
- 5. In £173 15s. how many fixpences? Ans. 6950.

6. In 12 crowns, at 6s. 7d. how many pence and farthings?

Ans. 948d, 3792 qrs.

7. In 671 eagles, at 10 dollars each, how many shillings, three-pences, pence and farthings? Ans. 40260 shill. 161040 three-pences, 483120 pence, and 1932480 qrs.

REDUCTION ASCENDING.

RULE.

Divide the lowest denomination given by that number which it takes of the same to make one of the next higher, and so continue to do, till you have brought it into that denomination which your question requires.

EXAMPLES.

1. In 16971 farthings how many pounds?

OPFRATION.

Farthings in a penny 4(16971

Pence in a shilling

12)4242 3qrs.

Shillings in a pound

2'0)35|3 6d.

417 13s.

Ans. £17 42s, 6d. 3qrs.

2. In 1765 pence, h mppeunds? Ans. 67 7s. 1d.

Reduction descending and ascending reciprocally prove each other.

8. In 38976 farthings, how many quineas? Ans. 29.

4. In 6950 fix-pences, how many pounds?

Ans. £173 15s.

5. In 3792 farthings, how many crowns? Ans. 12.

- 6. In 48960 farthings, how many pence, three-pences, fix-pences, and dollars?

 Ans. 12240 pence, 4080 three-pences, 2040 fix-pences, 170 dollars.
- 7. In 6952 three-pences, how many pistoles at 22s. each?

 Ans. 79.

REDUCTION ASCENDING AND DESCENDING.

1. MONEY.

1. In 67 moidores, at 36s. each, how many dollars?

Ans. 342 dollars.

In this question, the first step will be to bring the emoidores into shillings; lastly bring the shillings into dollars.

2. In 75 pittoles how many pounds?

Ans. 682 10s.

3. In £73 how many guineas?

Ans. 52 guineas, 4s.

4. In £63 and 5 guineas how many dollars?

Ans. 233 dollars, 2s.

- "When it is required to know how many forts of coin of different values, and of equal number, are contained in any number of another kind; reduce the several forts of coin into the lowest denomination mentioned, and add them together for a divisor; then reduce the money given, into the same denomination for a dividend, and the quotient arising from the division will be the number required."
 - "Note. Observe the same direction in weights and measures."
- 1. In 54 guineas, how many pounds, dollars and shillings of each an equal number?

OPERATION.		
41 is 20 shillings	54 guineas	
A dollar is 6 shillings	28 Shillings is	a guinea
1 fhilling		_
	492	100
Divisor, 27 Shillings	108	

Dividend, 1512 faillings.

27)1512(56 of each; that is, 54 guineas include the value of one pound, one dollar and one failling, 56 times.

162 162 000

2. In 172 moidores, how many eagles, dollars and nine-pences, of each the like number. Ans. 92 of each, and 68 nine-pences over.

2. TROY WEIGHT.

1. In 4lb. 5oz. 16pwts. how many grains?

OPERATION.

lb. oz. pwts. 4 5 16 12 oz. in a pound.

53 Ounces.

20 pwts. in an ounce.

1076 Penny weights.

24 grs. in one pwt.

4304

2152

Proof. 24)25824 Grains, the answer. 20)1076 16 pwts.

12)53 5 oz.

4 lb.

2. In 10lb. of filver, how many spoons, each weighing 5 oz. 10 pwts:?

Ans. 21 spoons, and 90 prots. over.

3. In 45681 grains of filver, how many pounds?

		20	12	oř	ERATION.
24	4) 45681 24	(1908 180		Answer, 7lb. 12	11oz. 3pwts. 9grss
	216 216	103 100	11 oz.	. 95 20	
i	081 72	003	pwts.	1903 24	4.
	09	ors.		45681 P	mof.

4. In 4560 grains of filver, how many tea-spoons, each one ounce?

Ans. 9\frac{1}{2} tea-spoons.

3. AVOIRDUPOIS WEIGHT.

cwt. qr. lb. oz 1. in 67 13 11 how many drams? PROOF. 16)1931696 269 28 16)120731 11 oz. 2165 28)7545 13 lb. 538 4)269 l qr. 7545 16 67 Cwt. 45281 7545 120731 16 724386 120731

1931696

2. In 14848 os. how many hundred weight? Aus. 7 C. 3qrs. 10lb.

3. In 470 boxes of Sugar, each 26lb. how many Gwt. ?

Ans. 109 C. Oqrs. 12fb.

4. In 17Cwt. 1qr. 6lb. of Sugar, how many parcels, each 17lb. ?

Ans. 114 parcels.

4. TIME.

1. In 121812 feconds, how many hours?

OPERATION.	PROOF.			
6,0) 21812	H. m.	s.		
	33 5 0	12		
60)2030 12 fec.	60			
`				
Ans. 33h. 50 m. 12s.	2030	•		
	60			
·	121812			

2. Supposing a man to be 21 years old, how many seconds has he lived allowing 365 days, 6 hours to a year?

Au. 662709600 seconds.

3. How many minutes from the commencement of the war between America and England, April 19, 1775, to the fettlement of a general peace which took place Jan. 20, 1783?

Ans. 4079160 minutes.

4. In 413280 minutes how many weeks? Ans. 41.

5. LONG MEASURE.

1. Reduce 16 miles to barley-corns.

16 Miles.	3)3041280
128 Furlongs.	12)1013760
40	3)84480
5120 Rods. 51**	+ 11)28160
25600 2560	2560 2
28160 Yards.	8)128
84480 Feet. 12	16 Miles.
1013760 Inches.	† Divide by 11 for $5\frac{1}{2}$ and multiply the quotient by 2. The reason is because $5\frac{1}{2}$ reduced to balf yards is 11.

Answer, 3041280 Barley-corns.

- * To multiply by one half $(\frac{1}{2})$ i is only to take half the Multiplicand:
- 2. In 47520 feet, how many leagues? Ans. 3 leagues:

3. How many times does the wheel, which is 18 feet 6 inches in circumference, turn round in the distance of 150 miles?

Am. 42810 times, and 180 inches over.

4. How many barley-corns will reach round the Globe, it being 360 degrees?

Ans. 4755801600:

6. LAND OR SQUARE MEASURE.

6. In 13 acres, 2 roods, how many poles?

OPERATION. Ac. r.	proof. 4 0)216 0				
13 2	4)54				
 					
54	13 Ac. 2 roods.				
40					

Ans. 2160 Poles.

2. In 2852 rods how many acres?

Ans. 17 A. 3 R. 12 P.

7. SOLID MEASURE.

1. In 1296000 folid inches, how many tons of hewn timber?

OPERATI	ON.	PROOF
,	5 0	15
1728)129600	0 <i>(75</i> 0	50
12096		
-	15 Tons, the Answer.	- 750
8640		1728
8640	•	
		6000
00		1500
	~	5250
	·	750
•		

1296000 Inches.

2. In 5529600 folid inches, how many cords of wood?

Ans. 25.

8. DRY MEASURE.

1. In 75 bushels of corn, how many pints?

PERATION.	•	PROOF.
75		2)4800
4		8)2400
300		4)000
8		4)300
2400	, .	75 bufbels.
2		
	i	.*

Ans. 4800 pints.

2. In 9376 quarts, how many bushels?

Ans. 293

It would be needless to give examples of Reduction in all the weights and measures. The understanding, which the attentive scholar must already have acquired of this rule, by help of the tables, will ever be sufficient for his purpose:

Supplement to Reduction.

QUESTIONS.

- 1. WHAT is Reduction ?
- 2. Of how many kinds is Reduction? What are they called? Wherein do these kinds differ one from the other? Which of these fundamental rules are employed in their operations?
- 3. How is Reduction Descending performed?
- 4. How is Reduction Ascending performed?
- 5. When it is required to know how many forts of coin, weights or measures of different values, of each an equal number, are contained in any other number of another kind, what is the method of procedure?

EXERCISES.

1. In 36 guineas how many crowns? Ans. 153 crowns, and 9d. over.

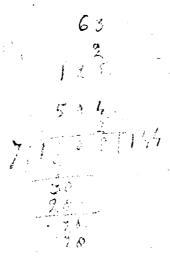
2. How many steps of 2 feet 5 inches each, will it require a man to take, going from Leominster to Boston, it being 43 miles.

Ans. 93948 steps; The last step will carry him into the town 12 inches.

3. Let 70 dollars be distributed a mong three men in such a manner that as often as the first has 5s. the second shall have 7s. and the third 9s. What will each one receive? Ans. First 16 dolls. 4s. Second 23 dolls. 2s. Third 30 dells.

6)100 20 20 6)100 6)100 15-4 9 20-2 9 4. If a vinter be defirous to draw off a Pipe of Canary into bottles containing pints, quarts and 2 quarts, of each an equal number, how many must be have?

Ans. 144 of each.

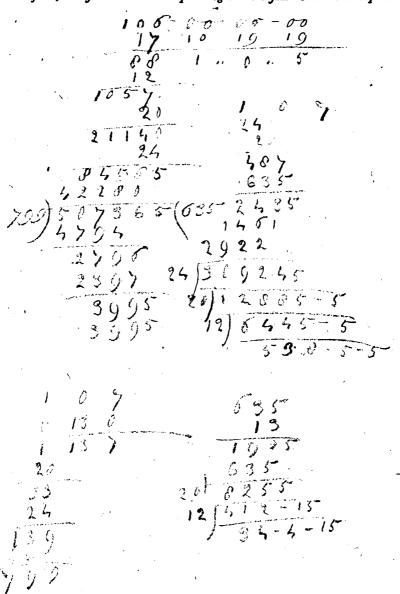


5. There are three fields; one contains 7 acres, another 10 acres and the other 12 acres and 1 rood; how many shares of 76 perches each, are contained in the whole?

Ans. 61 shares and 44 perches over.

6. There are 106lb. of filver, the property of 3 men; of which A receives 17lb. 10oz. 19pwts. 19grs. of what remains, B shares 1oz. 7grs. so often as C shares 13pwts. What are the shares of B and C?

Auswer, B's share 53lb. 80z. Spwts. 5grs. C's share 34lb. 40z. 15pwts.



§ 2. Fractions.

WHEN the thing or things fignified by figures are whole ones, then the figures which fignify them are called *Integers* or whole numbers. But when only fome parts of a thing are fignified by figures, as two thirds of any thing, five fixths, seven tenths, &c. then the figures which fignify these parts of a thing being the expression of some quantity less than one, are called Fractions.

Fractions are of two kinds, Vulgar and Decimal; they are diffinguished by the manner of representing them; they also differ in their modes of operation.

VULGAR FRACTIONS.

To understand Vulgar Fractions, the learner must suppose an integer (or the number 1) divided into a number of equal parts; then any number of these parts being taken, would make a fraction, which would be represented by two numbers placed one directly over the other, with a short line between them, thus $\frac{2}{3}$ two thirds, $\frac{3}{5}$ three fifths, $\frac{7}{6}$ seven eights, &c.

EACH of these figures have a different name and a different signification. The figure below the line is called the Denominator and shews into how many parts an integer, or one individual of any thing is divided—the figure above the line is called the numerator and shews how many of those parts

are fignified by the fraction.

For illustration, suppose a filver plate to be divided into nine equal parts. Now one or more of these parts make a fraction, which will be represented by the figure 9 for a denominator placed underneath a short line shewing the plate to be divided into nine equal parts; and supposing two of those parts to be taken for the fraction, then the figure 2 must be placed directly above the 9 and over the line $(\frac{2}{3})$ for a Numerator, shewing that two of those parts are signified by the fraction, or two ninths of the plate. Now let 5 parts of this plate, which is divided into 9 parts, be given to John, his fraction would be five ninths; let 3 other parts be given to Harry, his fraction would be three ninths; there would then be one part of the plate remaining still (5 and 3 are 8) and this fraction would be expressed thus $\frac{1}{8}$ one ninth.

In this way all vulgar fractions are written; the Denominator, or number

In this way all vulgar fractions are written; the Denominator, or number below the line shewing into how many parts any thing is divided, and the numerator, or number above the line, shewing how many of those parts are ta-

ken, or fignified by the fraction.

To ascertain whether the Learner understands what has now been taught him of fractions, let us again suppose a dollar to be cut into 13 equal parts;—let 2 of those parts be given to A; 4 to B; and 7 to C.

REQUIRED of the Learner that he should write A's fraction——.

C's fraction——.

It is from Division only that fractions arise in Arithmetical operations: the remainder after division is a portion of the Dividend undivided; and is always the Numerator to a fraction of which the Divisor is the Denominator. The Quotient is so many integers.

THE Arithmetic of Vulgar Fractions is tedious and even intricate to beginners. Besides, they are not of necessary use. We shall not, therefore, enter into any further consideration of them here. This difficulty arises chiefly from the variety of denominators; for when numbers are divided into different kinds, or

parts they cannot be eafily compared. This confideration gave rife to the invention of

DECIMAL FRACTIONS.

Decimal fractions are also expressions of parts of an integer; or, are in value something less than one of any thing, whatever it may be, which is signified

by them.

In decimals, an integer, or the number one, as 1 foot, 1 dollar, 1 year, &c. is conceived to be divided into len equal parts, (in vulgar fractions an integer may be divided into any number of parts) and each of these parts is subdivided into ten lesser parts, and so on. In this way, the denominator to a decimal fraction in all cases, will be either 10, 100, 1000, or unity (1) with a number of cyphers annexed; and this number of cyphers will always be equal to the number of places in the numerator. This is to to to the number of which the cyphers in the denominator of each are equal to the number of places in its own numerator.

"As the denominator of a decimal fraction is always 10, 100, 1000, &c. "the denominators need not be expressed; for the numerator only may be "made to express the true value; for this purpose it is only required to "write the numerator with a point, (,) before it, called a feparatrix, at the left hand to distinguish it from a whole number; thus, 10 is written, 6;

" $\frac{27}{100}$, 27; $\frac{685}{1000}$, 685, &c.

When integers and decimals are expressed together in the same sum, that sum is called a mixed number: Thus, 25,63 is a mixed number; 25, or all the sigures to the left hand of the separatrix being integers, and ,63 or all the sigures to the right hand of the same point being decimals.

The first figure on the right hand of the decimal point signifies tenth parts,

the next hundredth parts, the next thousandth parts, and so on.

,7 fignifies feven tenth parts. ,07—feven hundredth parts.

,27—two tenth parts and feven hundredth parts; or twenty-feven hundredths,

357—three tenth parts, five hundredth parts, and feven thousandth parts; or, 327 thousandths,

5,7—five and feven tenth parts.

5,007—five and feven thousandths.

The value of each figure from unity, and the decrease of decimals toward the right hand, may be seen in the following

TABLE.

	z.		.,		. :	á		· ·		parts	Thousandth part	part	parts	rts	parts	parte
		LG.	nds	nds	spu	sp			Tenth parts	Hundredth	ndth		Thoufandth	Millionth parts	h pa	
Millions	Millions	Millions	Thoufan	Thousands	Thoufands	Hundreds	us	Units	nth.	ındre	onla	Thoufandth	oufai	llion	Millionth	Millioath
W		M	_	-	H	Ħ	Tens	C	Te	H	Ë	ij	Ä	M	Mil	MEI
D.	×		C	×				•	3			×	S		×	C
9	8	7.	6	5	4	3	2	1	2,	3	4	5	6	7	8 ,	9

Cyphers placed to the right hand of decimals do not alter their value; placed at the left hand, they diminish their value in a tenfold proportion.

ADDITION OF DECIMALS.

RULE.

"1. PLACE the numbers whether mixed or pure decimals, under each

" other, according to the value of their places."

"2. Find their fum as in whole numbers, and point off to many places for decimals as are equal to the greatest number of decimal places in any of the given numbers."

examples

1. What is the amount of 73,614 gair of a guinea, and 100,19 guines whe

436 guineas, 3,27 guineas, ,8632 d together?

OPERATION ... 73,612 436, 3,27 ,8632 100,19

Ans. 613,9352 guineas.

2. 345,601 ,3724 63,1 572,313 7,5462 The decimals are arranged from the feparatrix towards the right hand, and the whole numbers from the same point towards the left hand. The greatest number of decimal places in any of the numbers is four, consequently, four sigures in the product must be pointed of for decimals.

3. Required the fum of 37,821 + 546,35+8,4+37,325?

Ans. 629,896.

4. What is the fum of three hundred twenty nine and feven tenths; thirty feven and one hundred fixty two thousandths, and fixteen hundredths when added together?

Ans. 367,922.

5. Add fix hundred and five thousandths, and four thousand and three hundredths?

Sum 4600,035.

Ans. 301,022.

Note. When the numerator has not fo many places as the denominator has cyphers, prefix fo many cyphers at the left hand as will make up the defect; fo $\frac{1}{1000}$ is written thus, ,005, &c.

SUBTRACTION OF DECIMALS.

RULE.

"Place the numbers according to their value; then fubtract as in whole numbers, and point off the decimals as in addition."

EXAMPLES.

1. From 716,325 take 81,6201.

OPERATION.

2. From 119,1384 take 95,91.

Rem. 23,2284.

From 716,325 Take 81,6201

Rem. 634,7049

3. What is the difference between 287 and 3,115?

Ans. 283,885

4. From 67 take ,92

Rem. 66,08

All the operations in Decimal Fractions are extremely easy; the only liability to error will be in placing the numbers and pointing off the decimals; and here care will always be security against mistakes.

MULTIPLICATION OF DECIMALS.

RULE.

"Whether they are mixed numbers, or pure decimals, place the factors

and multiply them as in whole numbers."

"2. Point off fo many figures from the product as there are decimal places in both the factors; and if there be not so many decimal places in the product, supply the defect by prefixing cyphers."

EXAMPLES.

1. Multiply ,0261 by ,0035 OPERATION. ,0261 ,0035

1305

783

,00009135 Produtt.

In this example, the decimals in the two factors taken together are eight; the product falls short of this number by four figures, consequently, four cyphers are prefixed to the left hand of the product,

2. Multiply 31,72 by 65,3 Product, 2071,316

> OPERATION. 31,72 65,3

9. Multiply 25,238 by 12,17 Product, 307,14646

4. Multiply ,62 by ,04 Product, ,0248 5. Multiply 17,6 by ,75 Produë, 13,2

DIVISION OF DECIMALS.

RULE.

*1. The places of decimal parts in the dividend, therefore divide as in whole numbers, and from the right hand of the quotient, point off so many places for decimals, as the decimal places in the dividend exceed those in the dividen.

"2. If the places of the quotient be not so many as the rule requires, sup-

ply the defect by prefixing cyphers to the left hand.

" 3. If at any time there be a remainder, or the decimal places in the divisor be more than those in the dividend, cyphers may be annexed to the dividend, or to the remainder, and the quotient carried on to any degree of exactness."

EXAMPLES.

Divide 2,735 by 51,2

2048

92

In this example, there are five decimals in the dividend (counting the two cyphers which were added to the remainder of the dividend after the first division) that the decimals in the divisor and quotient counted together may equal that number, a cypher is prefixed to the left hand of the quotient. In division of decimals it is proper to add cyphers so long as there continues to be a remainder, this however is not practifed, nor is it necessary; four or five decimals being sufficiently accurate for most calculations.

2. Divide 3156,293 by 25,17.

Quotient, 1253+

The Scholar is requested to point the following example as the rule directs.

3. Divide 5737 by 13,3 Quotient, 431853+

4. Divide 173948 by ,375.

Quotient, 463861+

5. Divide 2 by 53,1 Quotient, 037+

REDUCTION OF DECIMALS.

CASE 1.

To reduce Vulgar Fractions to Decimals.

RULE.

ANNEX a cypher to the numerator and divide it by the denominator, annexing a cypher continually to the remainder. The quotient will be the dec. imal required.

EXAMPLES.

1. Reduce 3 to a decimal.

30

00

2. Reduce 1 to a decimal.

OPERATION.

5)3,0(,6 Answer.

The numerator in these operations is confidered as an integer, and always requires the decimal point to be placed immediately

after it, the cyphers annexed occupy the places of decimals, the quotient must be pointed off according to the rule in Division.

OPERATION. 7)1,0(,1428+Ans.

> 30 28 20

> > 14 60

56

3. Reduce $\frac{1}{4}$, $\frac{1}{4}$ and $\frac{3}{4}$ to decimals.

Answers, ,25. ,5. ,75.

4. Reduce $\frac{5}{36}$, $\frac{12}{480}$ and $\frac{9}{1129}$, to decimals. Answers, ,1923+,025,00797+

To reduce numbers of different denominations, as of money, weight and measure, to their decimal values.

RULE.

"I. Write the given numbers perpendicularly under each other for dividends, proceeding orderly from the least to the greatest."

"II. Opposite to each dividend, on the left hand, place such a number for "a divifor as will bring it to the next superior denomination, and draw a

"line perpendicularly between them.

"III. Begin with the highest, and write the quotient of each division, as "decimal parts, on the right hand of the dividend next below it, and fo on-" till they are all used, and the last quotient will be the decimal sought."

EXAMPLES.

1. Reduce 10. 61d. to the fraction of a pound.

OPERATION.

3, 6,75 12 20 10,5625

The given numbers arranged for the operation, all stand as integers. I then suppose 2 cyphers annexed to the 3 (3,00) which divided by 4, the quotient is 75, which I write against 6 in the next line and ,528125 Ans. the fum thus produced (6,75) I divide by 12, placing the quotient, (5625) at the right hand of the 10; lastly, I divide by 20 and the quotient, (,528125) is the decimal required.

2. Reduce 13s. 51d. to the deci-3. Reduce 12pwts. 14grs. to the demal of a pound. Ans., 6729+ cimal of an ounce. Ans. ,6291.

CASE 3.

To find the value of any given decimal in the terms of an integer.

RULE.

MULTIPLY the decimal by that number, which it takes of the next less denomination to make one of that denomination in which the decimal is given, and cut off fo many figures for a remainder to the right hand of the quotient, as there are places in the given decimal. Proceed in the fame manner with the remainder, and continue to do fo thro' ail the parts of the integer, and the leveral denominations standing on the left hand make the answer.

EXAMPLES.

1. What is the value of ,528125 of a

pound? OPERATION. ,528125 20 Shillings, 1 0,5 6 2 5 0 0

Pence, 6,7, 5 0 0 0 0

Farthings, 3,00000 Ans. 10s. $6\frac{3}{4}$ d.

This question is the first example in the preceding case inverted, by which it will be feen, that questions in these two cases may reciprocally prove each other.

The given decimal being the decimal of a pound, and shillings being the next less inferior denomination, because 20 shillings make one pound, I multiply the decimal by 20, and cutting off from the right hand, of the product a number of figures, for a remainder, equal to the number of fig-

on the left hand which are shillings. I then multiply the remainder which is the decimal of a shilling by 12, and cutting off as before, gives 6 on the left hand of pence; lastly, I multiply this last remainder, or decimal of a penny by 4 and find it to be 3 farthings, without any remainder. It then appears that ,528125 of a pound is in value 10s. 63d.

2. What is the value of ,73968 of a pound? Ans. £14 91d

3. What is the value of ,768 of a pound Troy? Ans. 902. 4pwt.7 17 grs.

Thus, 8) 680 = 15 = 17

^{* 17/25} is the last remainder, 680 reduced to its lowest terms: A fraction is said to be reduced to its lowest terms, when there is no number which will divide both the numerator and denominator without a remainder. Thus, fet to the fraction its proper denominator 680, then divide the numerator and the denominator by any number which will divide them both without a remainder, continue to do so as long as any number can be found that will divide them in that manner.

Supplement to Fractions.

QUESTIONS.

- 1. What are fractions?
- 2. What are integers, or whole numbers?
- 3. What are mixed numbers?
- 4. Of how many kinds are fractions?
- 5. How are Vulgar Fractions written?
- 6. What is fignified by the denominator of a fraction?
- 7. What is fignified by the numerator?
- 8. How are Decimal Fractions written?
- 9. How do Decimals differ from Vulgar Fractions?
- 10. How can it be afcertained, what the denominator to a Decimal Fraction is, if it be not expressed?
- 11. How do cyphers placed at the left hand of a Decimal Fraction affect its value?
- 12. How are Decimals distinguished from whole numbers?
- 13. In the addition of Decimals what is the rule for pointing off?
- 14. What is the rule for pointing off Decimals in Subtraction? In Multiplication? and in Division?
- 15. In what manner is the reduction of a vulgar Fraction to a decimal performed?
- 16. How are numbers of different denominations, as pounds, shillings, pence, &c. reduced to their decimal values?
- 17. If it be required to find the value of any given decimal in the terms of an integer what is the method of procedure?

EXERCISES.

1. What is the fum of 794 61 and of 3 when added together?

OPERATION.

79,5 6,25

,75

86,50 Ans.

2. From 17 take 3 OPERATION. ,75

16,25 Remainder.

In case 1. Ex. 3d, under Reduction of decimal fractions the Scholar may notice, that 1, 1 and 3 reduced to decimals are, ,25,5 and ,75. When numbers, therefore, for operation in either of the fundamental Rules, are in-

cumbered with these fractions !,

3. Multiply 68½ by 5½
OPERATION.
6 8,2 5
5,5
3 4 1 2 5
3 4 1 2 5
3 7 5,3 7 5 Product.

4. Divide 264 by 54 OPERATION. 2,5) 26,25(10,5 Quotient. 25

125 125 $\frac{1}{3}$, $\frac{1}{4}$, fubstitute for them their equivalent decimal fractions, that is, for $\frac{1}{4}$, 25 for $\frac{1}{4}$, 5 for $\frac{1}{4}$, 75 then proceed according to the rules already given for these respective operations in decimal fractions.

Many persons are perplexed by occurrences of a similar nature to the examples above. Hence it is seen in some measure the usefulness of Fractions, particularly decimal fractions. The only thing necessary to render any person adveit in these operations is to have riveted in his mind the rules for pointing as taught and explained in their proper places. They are not burstensome; every scholar should have them perfectly committed.

5. If a pile of wood be 18 feet long, 11! wide, and $7\frac{1}{4}$ high, how many cords does it contain?

Ans. 12 cords 68 feet* 432 inches.

A cord of wood is 128 folid feet; the proportions commony affigued are, 8 feet in length, 4 in breadth, and 4 in height.

The contents of a load or pile of wood of any dimensions may be found by multiplying the length by the breadth and this product by the height; or, by multiplying the length, breadth, and height into each other. The last product divided by 128 will shew the number of cords, the remainder, if any, will be so many folid seet.

^{*} The 432 inches in the fraction ,25 of a foot valued according to CASE 3, Reduc. Dec. FRACTIONS.

6. If a load of wood be 9 feet long, $S_{\frac{1}{2}}^{1}$ feet wide, and 4 feet high, how many square feet does it contain?

Ans. 126 feet, which is 2 feet floort of a cord.

7. What is the value ,725 of a day?

Ans. 17 hours 24 minutes.

8. What is the value of ,0625 of 2 shilling? Ans. 3 farthings.

9. Reduce 9Cwt. Oqrs. 7lb. 802. to the decimal of a Ton.

Ans. 15334821+

10. Reduce 3 farthings to the decimal of a shilling. Am., 0625

11. Reduce $\frac{6}{48\pi}$ to a decimal fraction. Ans. ,0125.

§ 3. Pederal Money.

FEDERAL MONEY is the coin of the United States, established by Congress, A. D. 1786. Of all coins this is the most simple, and the operations in it, the most easy.

The denominations are in a decimal proportion, as exhibited in the following

TABLE.

10 Mills 10 Cents 10 Dimes 10 Dollars	make one	Cent, Dime, Dollar, Eagle.	marked thus,	\$
--	----------	-------------------------------------	--------------	----

The expression of any sum in Federal Money is simply the expression of a mixed number in decimal fractions. A dollar is the Unit money: dollars therefore must occupy the place of units, the less denominations, as dimes, cents, and mills, are decimal parts of a dollar, and may be distinguished from dollars in the same way as any other decimals by a comma or separatrix. All the sigures to the less thand of dollars, or beyond Units place are eagles. Thus, 17 Eagles, 5 dollars, 3 dimes, 4 cents, and 6 mills are written—

Hundreds

Eag's ; or, Tens.

Doll's ; or, Units.

Dimes ; or, Tenth parts.

Cents ; or, Hundredth parts.

Of these, four are real coins, and one is imagin-

The real coins are the Eagle, a gold coin; the Dollar and the Dime, filver coins; and the Cent, a copper coin. The mill is only imaginary, there being no piece of money of that denomination.

There are half-eagles, half-dollars, double-dimes,

half-dimes, and half cents, real coins.

These denominations, or different pieces of money, being in a tenfold proportion, consequently, any sum in Federal Money does of ittelf exhibit the particular number of each different piece of money contained in it. Thus 175,346 (feventeen eagles, five dollars, three dimes, four cents, fix mills) contain 175346 mills, 17534_{10}^{6} cents, 1753_{100}^{6} dimes, 175_{1000}^{40} dollars, 17_{1000}^{40} eagles. Therefore, eagles and dollars reckoned together, express the number of dollars contained in the sum; the same of dimes and cents; and this indeed is the usual way of account, to reckon the whole sum in dollars, cents and mills, thus,

Dolls.

175 34 6

175 34 6

The Addition, Sub-raction, Multiplication and Division of Federal Money is performed in all respects as in Decimal Fractions, to which the Scholar is referred for the use of rules in these operations.

ADDITION OF FEDERAL MONEY.

1. Add 16 Eagles; 3 Eagles, 7 Dollars, 5 Cents; 26 Dollars, 6 Dimes, 4 Cents, 3 Mills; 75 Cents, 8 Mills; 40 Dollars, 9 Cents, together.

Or, the fums may be reckoned in dollars, cents, and mills, thus,

Ear	9	Do'lls.	Dimes.	Cts.	Mills.			•	,	Dells.	Cis.	Mills.	
_	7	_											
1	6	0,	•							1,60			
	3	7,	0	5	•					37	05		
	2	6,	6	4	3	•				26	64	3	
		,	7	5	8	•		,			75	8	
	4	0,	0	9			•			40	09		
					<u> </u>		•						

\$264 4, 5 4 1 \$264 54 1
2. If I am indebted 59 dollars, 112 dollars, 98 cts. 113 dolls. 15 cts. 15 dolls. 21 dolls. 50 cts. 200 dolls. 73 dolls. 35 dolls. 17 cts. 75 dolls. 20 dolls. 40 dolls. 33 cts. and 16 dolls. What is the fum which I owe?

Ans. \$781 13

Accountants generally omit the comma and diftinguish cents from dollars by setting them apart from the dollars.

SECT. II. 3. SUBTRACTION OF FEDERAL MONEY. 89

SUBTRACTION OF FEDERAL MONEY.

1. From Dolls. 863,17 take, Dolls. 69,82 OPERATION. 8 6 3,1 7 6 9,8 2

2. From Dolls. 681 take, Dolls. 57,63 Remainder, Dolls. 623,37

Remainder, 7 9 3,3 5

MULTIPLICATION OF FEDERAL MONEY.

1. If Flour be Dolls. 10,25 per barrel, what will 27 barrels cost?

OPERATION.
1 0,2 5
2 7
7 1 7 5
2 0 5 0

Dolls. 2 7 6, 7 5 Anfwer. 2. MULTIPLY Dolls. 76,35 by Dolls. 37,46 Product, Dolls. 2860,0710 Point off the decimels in the product according to the rule in multiplication of decimals; if at any time there shall be more than three decimal figures, all beyond mills, or the third place will be decimal parts of a mill.

3. Multiply Dolls. 24,675 by D.lls. 13,63 Product, Dolls. 336,320 705

DIVISION OF FEDERAL MONEY.

1. If 2728 bushels of wheat cost Dolls. 2961, how much is it per bushel?

OPERATION.

Bushels. Dolls. D. d. c. m. 2723)2961(1, 0 8 5 Answer. 2728

> > 1120

WHEN the dividend confifts of dollars only, if there be a remainder after division, cyphers must be annexed as in division of decimals. 2. Divide Dolls. 3756 equally among 13 men; what will each man receive?

Ans. Dolls. 288,923.

3. Divide Dolls. 16,75 by 27 Product, 62 Cents.

SECT. II. 3.

REDUCTION OF FEDERAL MONEY.

CASE 1.

To reduce Pounds, Shillings, Pence and Farthings, to Dollars, Cents and Mills.

RULE.

SET down the pounds and to the right hand write half the greatest even number of the given shillings; then consider how many farthings there are contained in the given pence and farthings, and if the sum exceed 12, increase it by 1, or if it exceed 36 increase it by 2, which sum set down to the right hand of half the greatest even number of shillings before written, remembering to increase the second place, or the place next to shillings by 5, if the shillings be an odd number; to the whole sum thus produced, annex a cypher and divide the sum by 3; cut off the three right hand sigures in the quotient, which will be cents and mills, the rest will be dollars.

EXAMPLES.

1. Reduce £ 47 7s. 10\frac{1}{4}d. to Dollars, Cents and Mills.

OPERATION.

Half of the number of faillings.

The farthings in pence and farthings increased according to rule,
Cypter annexed.

In this example to the right hand of pounds (47) I write 3, half the greatest even number of the given shillings (7,) the farthings in $10\frac{3}{4}d$ (43) increased by two (45) because exceeding 36 and the second place increased by 5 because shillings were an odd number, are 95, which sum written to the right hand of the 3, a cypher annexed, and the sum divided by 3, gives the Answer, 157 dollars, 98 cents, and 3 mills.

Divide by 3) 4 7 3 9 5 0

Dolls. 1 57, 9 8 3

Is pounds only are given to be reduced, a cypher must be annexed and the number divided by 3; the quotient will be dollars. If there be a remainder annex more cyphers, and divide, the quotient will be cents and mills.

WHEN there are no shillings, or only 1 shilling in the given sum, so there be no even number, write a cypher in place of half the even number of shillings, then proceed with the pence and farthings as in other cases.

Is it be required to reduce pounds, shillings, pence, &c. to Dollars and Cents only, the cypher must not be annexed; in this case two figures only must be cut off from the quotient.

A little practice will make these operations extremely easy.

3. In 417 1s. 61d how many dol-2. In £763 how many dollars, cents and mills? lars, cents and mills? Ans. 2543 Dolls. 33 cents 3 m.

Ans. Dolls. 56 92 3.

4. In £109 3s. 8d. how many Dollars and cents? Ans. Dolls. 363,944. +

5. In \$86 6s. 5\fmathbb{1}d. how many dollars, cents and mills? Ans. Dells. 287,74.

CASE 2.

To reduce Dollars, Cents, and Mills, to Pounds, Shillings, Pence? and Farthings.

RULE.

Multiply the given fum by 3, cut off the four right hand figures, which will be decimals of a pound, the left hand figures will be the pounds. the value of the decimals, double the first figure for shillings, and if the figure in the second place be 5, add another shilling, then call the figures in the second and third places, after deducting the 5 in the second place, so many farthings, abating 1 when they are above 12, and 2, when they are above 36.

EXAMPLES.

1. Reduce 255 dollars 40 cents 6 mills, to pounds, shillings pence and farthings.

OPERATION.

255406

76|6218 £76 12s. 5d. Anfewer.

In this example having multiplied the given fum by 3 and cut off the four right hand figures of the product, I double the first figure (6) for shillings, the figures in the fecond and third places (21) abating 1 for being over 12, (20) I confider as farthings, equal to 5d. In dolls. 255,406 therefore, are 76 12s. 5d.

Here 8 in the fourth place of decimals (1000) of a pound being of inferior value is not reckoned. The loss in this place is always less than one farthing.

If there be no mills in the given fum, multiply as before and cut off 3 figures only.

If there be neither cents nor mills that is, if the given fum be dollars, multiply by 3 and cut off one figure only.

2. In Dolls. 392,75 how many pounds fhillings, pence and farthings?

Ans. 6117 16s. 6d.

3. In Dolls. 39,635 how many pounds, shillings, pence, &c.? Ans. £11 17s. 9'd.

4. Reduce 134 Dollars, 65 Cents to pounds, shillings, pence and farthings. Ans. 640 7s, 101d.

5. Reduce Dolls. 684 to pounds and shillings. Ans. £205 4s.

Supplement to Federal Money.

QUESTIONS.

- 1. What is Federal Money? When was its establishment, and by what authority?
- 2. What are the denominations in Federal Money?
- 3. Which is the unit Money?
- 4. How are dollars distinguished from dimes, cents and mills?
- 5. What places do the different denominations occupy, from the decimal points?
- 6. How is the Addition of Federal Money Performed? Subtraction? Multiplication? Division?
 - 7. By what method are Pounds, Shillings, Pence ond Farthings reduced to Federal Money?
 - 8. How are Dollars, Dimes, Cents and Mills, reduced to Pounds, Shillings, Pence and Farthings?

EXERCISES.

1. A man dies leaving an estate of 71600 Dollars, there are demands against the estate of Dolls. 39876,74; the residue is to be divided between 7 sons; what will each one receive?

Ans. 4531 Dolls. 89 cts.

2. A man fells 1225 bushels of wheat at Dolls. 1,33 per bushel, and receives Dolls. 93,76 for transportation; what does he receive in the whole?

Ans. Dolls. 1723.01.

94 SUPPLEMENT TO FEDERAL MONEY. SECT. IL. 3.

- 3. Reduce £375 1s. 6 d. to dollars and cents.
 - Ans. Dolls. 1250,256
- 4. In 67 13s. 8d. how many dollars cents and mills?
 - Ans. Dolls. 25 61

- 5. Reduce Dolls. 781,27 to pounds, shillings, pence and farthings.

 Ans. 4234 7s. 7'.
- 6. Reduce Dolls. 98,763 to pounds, fhillings, pence and farthings.

 Ans. 429 12s. 7d.
- TABLE
 For reducing Shillings and Pence to Cents and Mills.

	0)	Sh	ill. 1		ill. 2	Sh	ill. 3	Shi	11.	Shi	ll. 5
	ctsN	1ills	crs.M		LteM	[ılls	icts N	_	i crosi		C':	ils
0			16	7	33	3	50		66	7	83	3
1	1	4	18	1	34	7	51	4	68	1	84	7
2	2	8	19	5	36	1	52	8	69	5	86	1
3	4	2	20	9	37	5	54	2	70	9	87	5
1-4	5	6	22	3	38	9	55 .	6	72	3	88	9
5	7		23	. 7	40	3	57		73	7	90	3
6	8	3	25		41	1	58	3	75		91	6
7	9	7	26	4	43		5 9	7	76	4	93	
- 8	11	1	27	8	44	4	61	į	77	8	94	4.
9	12	5	2 9	2	45	8	62	5	79	2	95	8
10	13	9	30	6	47	2	63	9	80	6	97	2
11	15	3	32		48	6	65	3	82		98	6

To find by this Table the Cents and Mills in any fum of Shillings and Pence under one Dollar, look the Shillings at top, and the Pence in the left hand column; then under the former and on a line with the latter, will be found the Cents and Mills fought.

TABLE
For reducing the currencies of the several United States to
Federal Money.

		N. Hamp.	· · · · · · · · · · · · · · · · · · ·	N. Jersey,	
		Mass.	N. York,	Pennfylvánia,	S. Carolina,
		Rh. Island.	and	Delaware	and
		Conn. and	N. Carolina.	and	Georgia.
	÷	Virginia.		Maryland.	
s c		D.cts.m.	D.cts.m.	D.cts.m.	D.cts.m.
투 }	1	, 3	, 3	, 3	, 4
Farthings	2	, 7	, 5	, 6	, 9
art.	3 ●	, 10	, 8	, 8	, 14
压	1	, 14	, 10	, 11	, 18
	2	, 28	, 21	, 22	, 36
- 1	3	, 42	, 31	, 33	, 54
	4	, 56	, 42	, 44	, 71
1	5	, 69	, 52	, 56	, 89
Pence	6	, 83	, 62	, 67	, 107
ē {	7	, 97	, 73	, 78	, 125
4	8	, 111	, 83	, 89	, 143
1	9	, 125	, 94	, 100	, 161
	10	, 139	, 104	, 111	, 179
	11	, 153	, 114	, 122	, 196
ļ	- 1	, 167	, 125	, 133	, 214
1	2	, 333	, 250	, 267	, 429
1	3	, 500	, 375	, 400	, 643
j	4	, 666	, 500	, 533	, 857
	5	, 833	, 625	, 667	1, 171
	6	1,000	, 750	, 800	1, 286
	7	1,167	, 875	, 933	1, 500
	· 8	1,333	1,000	1,067	1,714
Shillings.	9	1,500	1, 125	1, 200	1, 929
	10	1,667	1, 250	1, 333	2, 143
Sh	. 11	1,833	1, 375	1, 467	2, 657
-	12	2,000	1, 500	1,600	2, 571
,	13	2, 167	1, 625	1, 733	2, 786
	14	2,333	1, 750	1, 867	3,000
	15	2,500	1,875	2,000	3, 214
	16	2,667	2,000	2, 133	3, 424
	17	2,833	2, 125	2, 267	3, 643
	18	3,000	2, 250	2, 400	3, 857
	t 19	3, 167	2, 375	2, 533	4,071

TABLE

For reducing the currencies, &c. continued.

	· .		1	
•	New-Hamp.	New-York,	New-Jersey,	South-Caroli.
	&c. &c.	&c.	_&c. &c.	&c.
£.	D. c.m.	D.c.m.	D.c.m.	D.c.m.
1	3,333	2,5	2, 666 -	4,256
2	6,667	5,0	5,333	8,571
3	10,000	7,5	8,000	12,857
4	15,333	- 10,0	10,667	17,143
.5	16,667	12,5	13,333	21,429
6	20,000	15,0	16,000	25,714
7	23,333	17,5	18,667	30,000
8	26,667	20,0	21,333	34,286
9	30,000	22,5	24,000	98,571
10	33,333	25,0	26,667	42,857
20	66,667	50,0	<i>5</i> 3,33 3	85,714
30	100,000	75,0	80,000	128,571
40	133,333	100,0	106,667	171,429
50	166,667	125,0	133,333	214,286
60	200,000	150,	160,000	257,143
70	2 33,333	175,	186,667	300,000
√80	266,667	200,	213,333	342,857
90	300,000	225,	240,000	385,714
100	3 33 ,333	250,	266,667	428,571
200	666,667	500,	5 33,333	857,143
30 0	1000,000	750,	800,000	1285,714
400	1333,333	1000,	1066,667	1714,286
5 00	1666,667	1250,	1333,333	2142,857
600	2000,000	1500,	1600,000	2571,429
700	2333,333	1750,	1866,667	3000,000
800	2666,666	2000,	2133,333	3428,571
900	3000,000	2250	2400,000	3857,143
1000	3333,333	2500,	2666,667	4285,714

TABLE
For reducing Federal Money to the currencies of the several
United States.

	New Hamp.	New-York,	New-Jersey,	South-Caron.
	&c. &c.	&c.	&c. &c.	&c.
	Dol. 6s.	Dol. 8s.	Dol. 7s6	Dol. 4.8
D. Cts.	6. s. d. q.	6. s. d. q.	£. s. d. q.	£. s. d. q.
,01	3	10	10	2
,02	1 2	20	1-5	10
,03	2 1	3 0	2 3	1 3
,04	3 0	3 3	3 2	2 1
,0.5	3 2	4.3	4 2	23
,06	4 1	5 3	5 2	2 3 3 1
,07	5 0	£ 3	6 1	4 0
,08	5 3	7 3	7 1	4 2
,09	6 2	8 3	80	5 0
- ,10	7 1	92	9.0	5 2

TABLE
For reducing the currencies, &c. continued.

	New-Hamp.	New-York,	New-Jersey,	South-Carolina.
	&c. &c.	&c.	&c. &c.	&c.
Dolls. cts.	6. s. d. q.	£. s. d. q.	6. s. d. q.	6. s. d. q.
,20	1 2 2	171	160	11 1
,30	192	2 4 3	230	1 4 3
,40	243	3 2 2	300	1 10 2
,50	300	400	890	2 4 0
,60	371	492	460	292
,70	4 2 2	571	<i>5</i> 3 0	3 3 1
,80	492	643	600	3 8 3
,90	543	7 2 2	690	4 2 2
1,	600	8.00	760	4 8 0
2,	12 0 0	16 0 0	15 0 0	9 4 0
3,	18 0 0	1.400	1 260	14 0 0
4,	1 400	1 12 0 0	1 10 0 0	18 8 0
5,	1 10 0 0	2 0 0 0	1 17 6 0	1 3 4 0
6,	1 16 0 0	2 800	2 500	1800
7,	2 200	2 16 0 0	2 12 6 n	1 12 8 0
8,	2 8 0 0	3 4 0 0	3 000	1 17 4 0
. 9,	2 14 0 0	3 12 0 0	3 7 6	2 2 0 0
10,	3 000	4 0 0 0	3 15 0	2 6 8 0
20	6	8	7 10 0	4 13 4
30	9	12	11 50	700
40	12	16	15 0 0	968
50	15	20	18-15 0	11 13 4
60	18	24	22 10 0	14 0 0
70 80	- 21 '	28	26 5 0	16 6 8
90	24	32	30 0 0	18 13 4
100	27	36	3 3 15 0	21 0 0
200	30 60	40	37 10 0	23 6 8
300	90	80	75 0 0	41 13 4
400	120	120	112 10 0	70 6 0
500	150	160	150 0 Q	93 6 8
600	180	200	187 10 0	116 13 4
700	210	240	225 0 0	140 0 0
800	240	280	262 10 0	163 6 8
900	270	320	300 0 0	186 13 4
1000	300	360	337 10 0	210 0 0
2000	600	400	375 0 0	233 6 8
3000	900	800	750	466 13 4
4000	1200	1200	1,25	700 0 0
5 00 0	1500	1600	1500	933 6 8
6 000	1800	2000	1875	1166 13 4
7000	2100	2400	2250	1400 0 0
8000	2400	280 0 3200	2625	1633 6 8
9000	2700		3000	1866 13 4
10000	3000	3600	337 <i>5</i>	2100 0 0
		4000	37 <i>5</i> 0	2333 6 8

§ 4. Interest.

- 0000 a

INTEREST is the allowance given for the use of money, by the Borrower to the Lender. It is computed at so many dollars for each hundred lent for a year, (per annum) and a like proportion for a greater or less time. The highest rate is limited by our laws to 6 per cent. that is 6 dollars for a hundred dollars, 6 cents for a hundred cents, 46 for a £100, &c. This is called legal interest, and is always understood when no other rate is mentioned.

There are three things to be noticed in Interest.

- 1. The PRINCIPAL; or, money lent.
- 2. The RATE; or, fum per cent. agreed on.
- 3. The Amount; or, principal and Interest added together.

Interest is of two forts, fimple and compound.

- 1. Simple Interest is that which is allowed for the principal only.
- 2. Compound Interest is that which arises from the interest being added to the principal and (continuing in the hands of the lender) becomes a part of the principal, at the end of each stated time of payment.

GENERAL RULE.

- 1. For one year, multiply the principal by the rate, from the product cut off the two right hand figures of the dollars, which will be cents, those to the left hand will be dollars; or which is the same thing, remove the separatrix, from its natural place two figures towards the left hand, then all those figures to the left hand will be dollars, and those to the right hand will be cents, mills, and parts of a mill.
- In the same way is calculated the interest on any sum of money in pounds, shillings, pence and farthings, with this difference only, that the two figures cut off to the right hand of pounds, must be reduced to the lowest denomination, each time cutting off as at sirst.
- 2. For two or more years, multiply the interest of one year by the number of years.
- 3. For months, take proportional or aliquot parts of the interest for 1 year, that is, for 6 months, $\frac{1}{3}$; for 4 months $\frac{1}{3}$; for 3 months, ξ , &c.

For days, the proportional or aliquot parts of the interest for 1 month, allowing 30 days to a month.

EXAMPLES.

1. What is the interest of Dolls 86,446 for one year, at 6 per cent?

Dolls. cts. m.

86, 44 6 principal.

6 rate.

5] 18, 67 6 Interest.

In the product of the principal multiplied by the rate is found the answer.

Thus, cutting off the two right hand figures from the dollars leave 5 on the left hand, which is dollars; the two figures cut off (18) are cents, the next

figure (6) is mills; all the figures which may chance to be at the right hand of mills, are parts of a mill; hence we coilect the Ans. 5 dolls. 18 cts. 6 18 m.

2. What is the interest of Dolls. 365 14 cents 6 mills, for three years, 7 months and 6 days?

OPERATION.

3 6 5, 1 4 6 principal. 6 rate.

6 Months 1)2 1 9 0, 8 7 6 interest for one year.

6 5, 7 2 6 2 8 interest for 3 years.

1 Month 1 0, 9 5 4 3 8 interest for 6 months.
6 Days 3 1, 8 2 5 7 3 interest for 1 month.
, 3 6 5 1 4 interest for 6 days.

7 8, 8 7 1 5 3 interest for 3 years, 7 months, and 6 days; that is 78 dolls. 87cts. 1 200 m.

Because 7 months is not an even part of a year, take two such numbers as are even parts and which added together will make 7 (6 and 1,) 6 months is 5 of a year, therefore, for 6 months, divide the interest of one year by 2; again, 1 month is 1 of 6 months, therefore for 1 month, divide the interest of 6 months by 6. For the days, because 6 days is 1 of 2 month, or of 30 days, therefore, for 6 days, divide the interest of 1 month by 5. Lastly add the interest of all the parts of the time together, the sum is the answer.

3. What is the interest of £71 7s. $6\frac{1}{2}d$.
4. What is the interest of 16s.
5d. for 1 year? Ans. 1 stilling.

OPERATION.

q. 3|32 Ans. 64 5s. 74.

When the rate is at 6 per cent, there is not, perhaps, a more concife and easy way of cassing interest, on any sum of money in Dollars, Cents, and Mills, than by the sollowing

METHOD.

Write down half the greatest even number of months for a multiplier; if there be an odd month it must be reckened 30 days, for which and the given days, if any, seek how many times you can have 6 in the sum of them, place the figure for a decimal at the right hand of half the even number of months, already found, by which multiply the principal; observing in pointing off the product, to remove the decimal point or separatrix two figures from its natural place towards the left hand, that is point off two more places for decimals in the product, than there are decimal places in the multiplicand and multiplier counted together; then all the figures to the left hand of the point, will be dollars, and those to the right hand, dimes, cents, mills, &c. which will be the interest required.

Should there be a remainder in taking one fixth of the days, reduce it to a vulgar fraction, for which take aliquot parts of the multiplicand. Thus,

Iſ	the	ren	nainder	be	1=2,	divide	the r	nultir	olicano	d by 6
If	**•	-	•	-	2=,,	-	, =	•	•	by 3
	_				3=;,		• 1	. •	-	by 2
If	_	•	-	•	4=1,	-	•	•	~	by 3 twice.
Ϊf			-		5-1	and !	_		-	by 2 and 3

The quotients which in this way occur, must be added to the product of the principal multiplied by half the months, &c. the sum thus produced, will be the interest required.

When there are days, but a less number than 6, so that 6 cannot be contained in them, put a cypher in place of the decimal at the right hand of the months, then proceed in all respects as above directed.

Note. In casting interest, each month is reckoned 30 days.

EXAMPLES.

1. What is the interest of Dolls. 76,54 for 1 year 7 months, and 11 days?

The number of months being 19, the greatest even number is 18, half of which is 9, which I write down; then seeking how often 6 is contained in 41, (the sum of the days in the odd month and given days) I find it will be 6 times, which I also set down at the right hand of half the even number, of months for a decimal, by which together I multiply the principal. In taking one sixth of the days (41) there will be a remainder of $5 = \frac{1}{2}$ and $\frac{1}{3}$ for which I take, first one half the multiplicand, that is, divide the multiplicand by 2, then by 3, and these quotients added, with the products of half the even number of months &c. the sum of them will shew the inter-

est required, observing to count off two more figures for decimals in the product than there are decimal figures in both the multiplier and multiplicand, counted together.

For the concileness and simplicity of the above METHOD, it is conceived, that Instructors will recommend it to their Pupils in preference to any other.

2. What is the interest of Dolls. 5,93 for 2 years and 8 months?

Ans. 94 cents, 8 mills.

3. What is the interest of Dolls. 67,62 for 3 years and 2 months?

Ans. 12 Dolls. 84 cts. 7 mills.

4. What is the interest of 91 cents for 27 years?

Ans. 1 dol. 47cts. 4m.

162

When the interest on any sum is required for a great number of years, it will be easier, first to find the interest for I year, then multiply the interest so found by the number of years.

5. What is the interest of Dolls. 2870,32 for 10 days?

Ans. 4 dolls. 78cts. 3m.

~ 576,32

When the rate is any other than 6 PER CENT, first find the interest at 6 per cent, then divide the interest so found by such parts as the interest at the rate required, exceeds or falls short of the interest at 6 per cent, and the questiont added to or subtracted from the interest at 6 per cent, as the cose may be, will give the interest at the rate required.

6. What is the interest of Dolls. 137,84 for 2 years and 6 months at 5 per cent?

Ans. Dolls. 17,23.

7. What is the interest of Dolls. 79,07 for 10 months at 8 per cent?

Ans. Dolls. 5,271.

- 8. What is the interest of Dolls. 2,29 for 1 month 19 days at 3 per cent?

 Ans. 9 mills.
- 10. What is the interest of Dolls. 1600 for one year, and 3 months?

 Ans. 120 dolls.
- 12. What is the interest of Dolls. 17,68 for 11 months, and 28 days?

 Ans. dolls. 1,054.
- 14. What is the interest of Dolls. 105,61 for 1 year, 7 months, and 6 days?

 Ans. 10 dolls. 13cts. 8m.
- 16. What is the interest of 78 Dolls. 36cts. for 5 years 10 months, and 3 days?

 Ans. 27 dolls. 46cts. 5m.

- 9. What is the interest of Dolls. 18 for 2 years, 14 days at 7 percent?

 Ans. 2 dolls. 56cts. 9m.
- 11. What is the interest of Dolls. 5,811 for one year 11 months?

 Ans. 66 cents. 8m.
- 13. What is the interest of Dolls. 861,12 for 9 months, 25 days at 7 per cent?

 Ans. dolls. 49,394.
- 15. What is the interest of Dolls. 86 for 9 months?

 Ans. dolls. 3,87.
- 17. What is the interest of 812 Dolls. 30cts. for 2 years, 8 months, and 4 days?

 Ans. 6130,509.

To this mode of computing interest, I would add from the " Massachusette Justice," a

METHOD

Of computing the interest due on bonds, notes, &c. when partial payments may at different times be made, as established by the Courts of Law in Massachusetts.

RULE.

Cast the interest up to the first payment, and if the payment exceed the interest, deduct the excess from the principal, and cast the interest upon the remainder to the time of the second payment. If the payment be less than the interest, place it by itself, and cast on the interest to the time of the next payment, and so on, until the payments exceed the interest, then deduct the excess from the principal, and proceed as before.

EXAMPLES.

Suppose A should have a bond against B for 1166 dollars, 66 cents, and 6 mills, dated May 1, 1796, upon which the following payments should be made, viz.

	Dollars, Mills.	Months, Days.
1. December 25, 1796,	- 166,666	7 24
2. July 10, 1797,	- 16,666	6 15
3. September 1, 1798,	- 50,000	13 21
4. June 14, 1799,	- 333,333	9 13
5. April 15, 1800,	- 620,000	10 1
What will be due upon it August 3, 1	801 ?	15 · 18

Ans. Dolls. 237 76 cents.

To facilitate the operation, let the space of time from the date of the Bond to the day of the first payment, and from the time of one payment to that of another, and from that of the last payment to the time of settlement, be first computed and set down against the day of payment as above. Then set down

the fum on which the interest is to be cast, with the interest and payments in columns thus,

	Principal.	Time.	7	Interest.	Payments.	Excess.
	Dolls. Mills.	Mo. 1	Da.	Dolls. M.	Dolls. M.	Dolls. M.
1	1166,666 121,167	7	24	25,499	166,666	121,167
2	1045,499	6	15	33,978	16,666	
3	1045,499	13	21	71,616	50,000	-
4	1045,499	' 9	13	49,312	833,333	
	245,093			154,906	399,999	245,093
5	800,406 579,847	10	1	40,153	620,000	579,847
٠,	220,559	15	18	17,203		
4		The last Interest f		inder the last payme	220,559 ent 17,203	,

Sum due Aug. 1, 1801, 237,762

2. Supposing a note of 867 dollars, 33 cents, dated January 6, 1794, upon which the following payments should be made, viz.

Dolls. Cents.

1. April 16, 1797, - 136,44

2. April 16, 1799, - 319,

3. Jan. 1, 1800, - 518,68

What would be due July 11, 1801? Aus. Dolls. 215,103:

COMPOUND INTEREST,

Is calculated by adding the interest to the principal at the end of each year and making the amount the principal for the succeeding year; then the givenprincipal subtracted from the last amount, the remainder will be the compound interest.

A concife and easy method of casting Compound Interest, at 6 per cent. on any sum in Federal Money.

RULE.

Multiply the given fum, if For 7 years, by 150,3630 For 2 years by 112,36 8 years — 159,3848 3 years - 119,1016 4 years - 126,2476 9 years — 168,9478 5 years - 133,8225 10 years — 179,0847 6 years - 141,8519 11 years — 189,8298

- Note 1. Three of the first highest decimals, in the above numbers, will be fufficiently accurate for most operations; the product, remembering to move the separatrix two figures from its natural place towards the left hand will then shew the amount of principal and compound interest for the given Subtract the principal from the amount, and it will shew number of years. the compound interest.
- 2. When there are months and days; first find the amount of principal and compound interest for the years, agreeable to the foregoing method, then, for the months and days cast the simple interest on the amount thus found; this added to the amount will give the answer.
- 3. Any fum of money at Compound Interest, will double itself in 11 years 10 months and 22 days.

EXAMPLES.

eft of

O TITL

							2. What is the amount of \$236 a compound interest, for 4 years, months and 6 days?																	
						O	E	A	rio	N.								OP	ER.	ΔT	10)	ī.		
	-	,		1	8				5 9	f,						1	2	6,	2		7			
		c		5	1 4	3 C	_							` 2		7	8	7 7 9	4	2	_	6		, , , , , , , , , , , , , , , , , , ,
		5	4	0							٧			5 2	9	7							Amou 4 yea	
31									5. ibtr					7 9		-	_	-	4			,	. (
8	55	0,	9	7	Co	mp	อนก	d i	ntei	reft.	2	S1 9	0, 7,	7	2 4	5 4	9 A1	8 nou	4 nt	Inte for	erej 4	n (fl fo year	mo. 6 or 7 rs	aay

-(added.

\$3 0 8, 6 6 9 Answer.

Supplement to S. Anterest.

QUESTIONS.

- 1. WHAT is Interest !
- 2. What is understood by 6 per cent? 3 per cent? 8 per cent? &c.
- 3. What per cent per annum is allowed by law to the lender for the use of his money?
- 4. What is understood by the principal? The rate? The amount?
- 5 Of how many kinds is interest? In what does the difference confist?
- 6. How is simple interest calculated for one year, in Federal Money?
- 7. For more years than one, how is the interest found?
- .8. When there are months and days, what is the method of procedure?
- S. What other method is there of casting interest on sums in Federal Money?
- 10. When the days are a less number than 6, so that 6 cannot be contained in them, what is to be done?
- 11. How is simple interest cast in pounds, shillings, pence and farthings?
- 12. When partial payments are made at different times, how is the interest calculated?

EXERCISES.

1. What is the interest of \$916,72, for one year and 4 months?

Ans. \$73,327.

2. What is the interest of \$93,17 cts. for 11 days?

Ans. 17ets.

3. What is the interest of \$5,19 for 7 months?

Ans. 18 cts. 1 m.

4. What is the interest of \$1,07 for 3 years, 6 months and 15 days?

Ans. 22 cts. 7 m.

5. What is the interest of £41 11s. $3\frac{1}{4}d$. for a year and 2 months?

Ans. £2 18 $2\frac{1}{4}d$.

6. What is the interest of \$273,51 at 7 per cent for 1 year and 10 days?

Aus. \$19,677

7. Supposing a note of \$317,92 dated July 5, 1797, on which were the following payments—Sept. 13, 1799, \$208,04: March 10, 1800, \$76; what was the sum due Jan. 1, 1801?

Am. \$83,991:

§ 5. Compound Multiplication.

COMPOUND MULTIPLICATION is when the Multiplicand confilts of several denominations. It is particularly useful in finding the value of Goods.

The different denominations in what was formerly called Lawful Money, render this rule with some others in Arithmetic, as Compound Division and Pradice, rules of great usefulness, quite tedious, and the variety of cases necessarily introduced, extremely burthensome to the memory. This sumber of the mind might be almost wholly dispensed with, were the habit of reckoning

in Federal Money generally adopted through the U. States.

For important reasons, Pounds, Shillings, Pence and Farthings ought to fall wholly into disuse: Federal Money is our National currency; the scholar might encompass the most useful rules of Arithmetic in half the time; the value of commodities bought and sold, might be cast with half the trouble, and with much less liability to errors, were all the calculations in money universally made in Dollars, Cents and Mills. But this, to be practised must be taught; it must be taught in our schools, and so long as the prices of goods and almost every man's accounts are in Pounds, Shillings, Pence and Farthings, this mode of reckoning must not be left untaught.

To comprise the greater usefulness, and also to shew the great advantage which is gained by reckoning in Federal Money, I have contrasted the two modes of account, and in separate columns, on the same page, have put the

fame questions in Old Lawful and in Federal Money.

OPERATIONS.

In Pound, Shill. Pence, Farthings.

CASE 1.

When the quantity does not exceed 12 yards, pounds, &c. set down the price of 1 yard or pound, and place the quantity underneath the lowest denomination for a multiplier. Begin by multiplying the lowest denomination, and carry by the same rules from one denomination to another, as in Compound Addition.

EXAMPLES.

1. What will 7 yards of cloth cost at 9s5 per yard?

OPERATION.

L. s. d. O 9 '5 price of 1 yard. 7 yards.

Ans. 3 5 11 price of 9 yards. I fay, 7 times 5 is 35 pence—2:11. I fet down 11 and carry 2, faying, 7 times 9 is 63, and 2 I carry is 65s.—
£. 3 5s. which I fet down.

In Dollars, Cents, Mills.

IN ALL CASES,

Multiply the price and the quantity together, according to the rules of multiplication in *Decimal Fractions*, and *Federal Money*, and the product will be the answer, That is,

Multiply as in fimple multiplication, and from the product point off so many places for cents and mills as there are places of cents and mills in the price.

EXAMPLES.

1. What will 7 yards of cloth cost at \$1,57 (cqual to 905) per yard?

OPERATION.

D. cts. As there are
1, 57 Price. two decimals
7 quantity. places in the
price, fo I make
Ans. 10,99 price of 9y. two in the pro-

2. What will 9 pounds of sugar cost at 10d. per pound?

Ans. 7s6.

Dollars, Cents, Mills.

2. What will 9 pounds of fugar cost at \$0, 139 per pound?

Am. \$1,251

What will 6 yards of cloth coft
 10s. 5d. per yard ?
 Ans. 49 2s. 6d.

3. What will 6 yards of cloth coft at \$5,07 per yard? Ans. 8\$0,42

CASE 2.

When the quantity exceeds 12 and is any number within the Multiplication Table multiply by two such numbers, as when multiplied together, will produce the given quantity.

If no two numbers will do this exactly, multiply by two fuch numbers as come the nearest to it, and by the deficiency or excess, multiply the multiplicand, and this product added to, or subtracted from the first product, as the case may require, gives the answer.

EXAMPLES.

1. What will 42 yards of cloth cost at 1509 per yard?

OPERATION.

Multiplied by

5. s. d.
0 15 9 price 1 yard.
6

4 14 6 price of 6yds.
Multiplied by 7

Ans. 38 1 6 price of 42yds.

Because 6 times 7 is 42, I multiply
the price of 1 yard by 6, and this product by 7, as the rule directs.

d. 4. What will 42 yards of cloth col 2 price 1 yard. at \$2,625 per yard?

 $\begin{smallmatrix}&&5&2&5&0\\1&0&5&0&0\end{smallmatrix}$

\$1 1 0, 2 5 0 Answer.

Dollars, Cents, Mills.

2. What will 125 yards of cloth cost at 5s7 per yard? Ans. £34 17 11.

5. What will 125 yards of cloth coft at 93 cents per yard?

Ans. \$116,25

What will 51 pounds of tea cost at \$0,583 per pound?

6. What will 51 pounds of tea cost \$0,583 per pound?

Ans. £29,733

4. What will 130 yards of cloth cost at 42 3s. Od. per yard?

Ans. 6284 7s. 6d.

7. What will 130 yards of clock coft at \$7,25 per yard?

Ans. \$942,50

CASE 3.

When the multiplier, that is, the quantity exceeds 144, multiply first by 10, and this product again by 10, which will give the price of 100 yards, &c. and if the quantity be even hundreds, multiply the price of one hundred by the number of hundreds in the question, and the product will be the answer; if there are odd numbers, multiply the price of 10 by the number of tens, and the price of unity, or 1, by the number of units, then these several products added together will be the answer.

EXAMPLES.

1. What will 563 yards of cloth cost at £1 6s. 7d. per yard?

OPERATION.

£. 1	s. 6	d. 7 10	price of 1 yard.
13	5	10 10	price of 10 yds.
132	18	4	price of 100 yds.

664 11 8 price of 500 yds. 6 times 10 yds. 79 15 0 price of 60 yds.

3 times 1 yd. 3 19 9 price of 3 yds. Ans. 748 6 5 price of 563 yds.

2. What will 328 yards of cloth cost at 10r. 61 per yard?

Ans. 6172 17 8d.

Dollars, Cents, Mills.

8. What will 563 yards of cloth cost at \$4,43 per yard?

> OPERATION. Tds. 5 6 3 8, 9

2 5 2 5 2

82 9 4, 0 9 4

9. What will 328 yards of cloth cost at \$1,757 per yard? Ans. \$576,296

8. What will 624 yards of cloth cost at 12s. 8d. per yard?

Ans. £395 4s.

10. What will 624 yards of cloth coft at \$2.11 per yard?

Ans. \$1317,264

SECT. II. 5. SUPPLEMENT TO C. MULTIPLICATION. 111

Supplement to Compound Multiplication.

QUESTIONS.

- (1. WHAT is Compound Multiplication?
 - 2. What is its use?
- 3. Are operations most easy in Old Lawful, or in Federal Money?
 - 4. What is the rule for Compound Multiplication?
- 5. When the quantity, that is, the Multiplier, exceeds 12, and is within the Multiplication Table, what are the steps to be taken?
- 6. When no two numbers multiplied together will produce the given quantity, what then is to be done?
- 7. When the multiplier exceeds 144, what is the method of procedure?
- 8. When the price of goods is given in Federal Money, what is the general and universal rule for finding their value by multiplication?

EXERCISES.

- 1. A man has 38 filver cups, each one weighing 102. 3pwts. 16grs. how much filver do they all contain?

 Ans. 3lb. 028. 19pwts. 8grs.
- 2. If a man travel 34 miles, 3 furlongs, and 17 rods in one day, how far will he travel in 62 days?

 Am. 2134 miles, 4 fur. 14 rods.

- What will 235 yards of cloth dime to at £1 2s. 5½d. per yard?
 Am. £263 17s. 6½d.
- 4. If a horse run a mile in 12 minutes, 16 seconds, in what time would he go 176 miles?

Ans. 1D. 11h. 58m, 56s.

6 6. Compound Division.

COMPOUND DIVISION is the dividing of different denominations. OPERATIONS.

∞ :::: <:::: **∞**

In Pounds, Shil. Pence, Farthings.

In Dollars, Cents, Mills.

CASE 1.

- 1. When the Divisor, that is the quantity, does not exceed 12, begin at the high- and point off fo many places for cents est denomination, and in the manner of and Mills in the product as there are short division, find how many times the places of cts. and mills in the dividend. divisor is contained in it; place the quotient under its own denomination, that is, produced by the multiplicaand if any thing remain, reduce it to tion of two numbers, the operation the next less denomination, and divide may be varied by dividing the price as before; fo proceed through all the first by one of those numbers, and this denominations.
- 2. If the quantity exceeds 12, and there be any two numbers, which multiplied to--gether will produce it, divide the price first by one of those numbers, and this what is that per yard? quotient by the other.

EXAMPLES.

1. If 5 yards of cloth cost 63 13s. 6d. what is that per yard?

OPERATION.

£. s. d. 6 price of 5 yards. **5**)3 13

0 14 81 price of 1 yard.

Finding I cannot have the divisor (5) in the first denomination (£3) I reduce it to shillings, (60) and add in the 13 thillings, which make 73 fhillings, in which the divisor (5) is contained 14 times, and 3 remain; I fet down the 14, and the remainder (3 shillings) reduce to pence (36) and the 6d. added make what is that per yard? 42 pence, in which the divisor is contained 8 times and two remain; I fet down the 8, and reduce the 2 pence to farthings (8) in which I have the divifor once (1qr. or 4d.) and a remainder of 3 of a farthing, which being of small value is neglected.

2. If 48 yards of cloth cost £4 16s. 4d. what is that per yard?

Ans. 60 2s.

IN ALL CASES,

Divide the price by the quantity, If the quantity be a composite number, quotient by the other.

EXAMPLES.

1. If 5 yards of cloth cost \$12,25

OPERATION.

D. Cts. 5) 1 2, 2 5. There are two decimal places in 2, 4 5 the dividend. therefore, point off two places for decimals, or cents in the quotient.

2. If 48 yards of cloth cost \$16,06 Ans. £0,33

3. If 24lb. of tea cost 62 7s. 9\frac{1}{2}d. what is that per lb.?

Ans. £0 1s. $11\frac{3}{4}d$.

Dollars, Cents, Mills.

3. If 24 lb. of tea cost \$7,97 what is that per lb. ? Ans. \$0,332.

4. If 35 yards of cloth cost 642 6s. 7.d. what is that per yard?

Ans. £1 4s. 2.d.

4. If 35 yards of cloth coft \$141,103 what is that per yard?

Ans. \$4,031.

CASE 2.

1. "Having the price of an hundred weight (1121b.) to find the price of 11b. divide the given price by 3, that quotient by 7, and this quotient by 2, and the last quotient will be the price of 11b. required."

2. If the number of hundred weight be more than one, first divide the whole price by the number of hundreds, then proceed as before.

EXAMPLES.

1. If lowt, of fugar cost 43 7s. 6d. what is that per lb.?

OPERATION.

£. s. d. q. 8)3 7 6 price of 1 cwt.

7)0 8 5 1 price of 14lb. or 1 cwt.

2) 1 2 2 price of 2lb. or 1 caut.

Ans. 0 7 1 price of 1/b.

5. If 1cwt. of fugar cost \$11,25 cts. what is that per lb.

The fame may be done in Federal

Money.

Ans. 10 cts.

2. If 8 cwt. of cocoa cost £15 7s. 4d, what is that per lb.? Ans. 4d.

Dollars, Cents, Mills.

6. If 8 cwt. of cocoa cost \$51,223 what is that per lb.?

Ans. 5 cents, 7 mil/s. -

3. If 3 cwt. of fugar cost £15 13s. what is that per lb.? Ans. 11d.

7. If 8 cwt. of fugar cost \$52,167 what is that per lb.?

Ans. 15 cents 5 mills.

CASE 3.

When the divisor is such a number as cannot be produced by the multiplication of small numbers, divide after the manner of long division, setting down the work of dividing and reducing."

EXAMPLES.

1. If 46 yards of cloth cost £53 10s. 6d. what is that per yard?

OPERATION.

£ s. d. f. s. d. 46)53 10 6(1 3 8 d. Ann. 20

46)150(3 138 12

12 46)150(3

138 12

46)48(1

46

7s. 10d. what is that per bushel? Ans. 6s. 63d. Dollars, Cents, Mills.

8. If 46 yards of cloth cost \$178 ,416 what is that per yard? Ans. £3,878.

9. If 263 bushels of wheat cost 2. If 263 bushels of wheat cost £86 \$287,973, what is that per bushel? Ans. 1,093

1s. 11d. what is that per gallon? Ans. 4s. 4.d.

10. If 670 gallons of wine colt 3. If 670 gallons of wine cost £147 \$490,32; what is that per gallon? Ans. \$0,73.

Supplement to Compound Division.

QUESTIONS.

- 1. What is Compound Division?
- 2. When the price of any quantity, not exceeding 12. of yards, pounds, &c. is given in pounds, shillings, pence and farthings, how is the price of one yard found?
- 3. When the quantity is flich a number as cannot be produced by the multiplication of small numbers, what is the method of procedure?
- 4. Having the price of an hundred weight given, in what way is found the price of 1 lb.?
- 5. If there be feveral hundred weight, what are the steps of operating?
- 6. When the price is given in Federal Money, what is the method of operating?

EXERCISES.

Pounds, Shill. Pence, Farthings.

Dollars, Cents, Mills.

1. If 10 sheep cost 64 5s. 7d. what is the price of each? Ans. 8s. $6\frac{1}{4}$.

Let the scholar reduce the price of sheep and of the cows to Federal Monley, and perform the operations in Dolls. Cents and Mills.

2. If 84 cows cost £253 13s. what is the price of each?

Ans. £3, $0.4\frac{1}{2}$.

Price of 1 Sheep, \$1,426.

Price of 1 cow, 10,035.

SECT. II. 6. SUPPLEMENT TO COMPOUND DIVISION. 117

3. If 121 pieces of cloth measure 4. If 66 tea-spoons weigh 2lb. 1002. 2896 yards 1qr. 3na. what does each 14pwt. what is the weight of each? piece measure? Ans. 10pwt. 1213grs. Ans. 23 yards, 3qr. 3na.

5. If 2 cwt. of rice cost £2 11s. 6!d what is that per lb.? Ans. 2¹₄d.

6. At £2 11s. 6 d. for 2 cwt. of rice, what is that in Federal Money, and what is that per lb.? Price of 1 lb. 3cts. 8m.

cwt. lqr. 26lb. 4oz. what does each will each horse eat per day ? weigh? Ans. 1qr. 1lb. 1202.

8. If 8 horses eat 900 bushels, and 7. If 47 bags of Indigo weigh 12 1 peck of oats in 1 year, how much Ans. 1 peck, 1qr. 1pt. 2gills.

118 SUPPLEMENT TO COMPOUND DIVISION. SECT. II. 6.

9. Divide £297 2t. 3d. among 4 men, 6 boys, and give each man 3 times fo much as one boy; what will each man share, and each boy?

OPERATION.

The men have triple d. G. shares, therefore, mul-18)297 2 3 (16 10 tiply the number of men 18 (4) by 3, and add the 2=1 man's share. number of boys, (6) for 117 10 4 Ans. 49 a divisor. 108 PROOF. 9 £.49 10 men. boys, 4 and 6 20 3)182(10 198 1 0 men's sbare. 6 12 18 2 and 16 10 1 6 2 12 18 the number of equal Shares in the whole 99 0 O boy's share.)27(1 _Divisor. £.297 2 3 0 added. 18

> 9 4

)36(2 36 10. Divide £.39 12r. 5d. among 4 men, 6 women, and 9 boys; give each man double to a woman, each woman double to a boy.

§ 7. Single Rule of Three.

THE Single Rule of Three, fometimes called the Rule of Proportion, is known by having three terms given to find the fourth.

It is of two kinds, Dirett and Indirett, or Inverse.

SINGLE RULE OF THREE DIRECT.

The Single Rule of Three Direct teaches, by having three numbers given to find a fourth, which shall bear the same proportion to the third that the second does to the sirst.

It is evident that the value, weight, and measure of any commodity is proportionate to its quantity, that the amount of work, or consumption is proportionate to the time; that gain, loss, and interest when the time is fixed, is proportionate to the capital sum from which it arises; and that the effect produced by any cause is proportionate to the extent of that cause.

These are cases in direct proportion, and all others may be known to be so, when the number sought increases or diminishes along with the term from

which it is derived. Therefore,

If more require more, or less require less, the question is always known to be long to the Rule of Three Direct.

More requiring more, is when the third term is greater than the first and re-

quires the fourth term to be greater than the fecond.

Less requiring less, is when the third term is less than the first and requires the fourth term to be less than the second.

RULE.

"1. State the question by making that number which asks the question, the third term, or putting it in the third place; that which is of the same are name or quality as the demand, the first term, and that, which is of the fame name or quality with the answer required, the second term."

"2. Multiply the fecond and third terms together, divide by the first, and the quotient will be the answer to the question, which (as also the remainder) will be in the same denomination in which you left the second term,

" and may be brought into any other denomination required."

The chief difficulty that occurs in the Rule of Three, is the right placing of the numbers, or stating of the question; this being accomplished there is nothing to do, but to multiply and divide, and the work is done.

To this end the nature of every question must be considered, and the circumstances on which the proportion depends, observed, and common sense

will direct this if the terms of the question be understood.

The method of proof is by inverting the order of the question.

N te 1. If the first and third terms, both or either, be of different denominations, both terms must be reduced to the lowest denomination mentioned in either before stationable and in

in either, before stating the question.

2. If the fecond term confifts of different denominations, it must be reduced to the lowest denomination; the fourth term, or answer will then be found in the same denomination, and must be reduced back again to the highest denomination possible.

3. After division if there be any remainder, and the quotient be not in the lowest denomination, it must be reduced to the next less denomination, dividing as before. So continue to do, till it is brought to the lowest denomina-

tion, or till nothing remains.

4. In every question there is a supposition and a demand; the supposition is implied in the two sire terms of the statement, the demand in the third-

120 SINGLE RULE OF THREE DIRECT. Sect. II. 7.

5. When any of the terms are given in Federal Money, the operation is conducted in all respects as in simple numbers, observing only to place the point, or feparatrix between dollars and cents, and to point off the refults according to what has been taught already in Decimal Fractions, Federal Money,

and further illustrated in Compound Division.

6. When any number of barrels, bales, or other packages, or pieces are given, if they be of equal contents, find the contents of one barrel or piece, &c. in the lowest denomination mentioned, which multiply by the number of pieces, &c. the product will be the contents of the whole. If the pieces &c. be of unequal contents find the content of each, add these together, and the fum of them will be the whole quantity.

7. The term which asks the question, or that which implies the demand is generally known by some of these words going before it; how much? H.w

many? How long? What cost? What will? &c.

EXAMPLES.

1. If 9lbs. of tobacco cost 6s. what will 25lbs. cost? OPERATION.

lbs. : 6:: 25: to the answer. 25 30 12 -s. d. 9)150(16 8 answer. 9* 60 54 6 12

Here 25lbs. which asks the question, (what will 25lbs. &c.) is made the third term, by being put in the third place; 9lbs. being of the fame name, the first term, and 6s. of the same name with the term fought, the fecond term.

I Multiply the fecond and third terms together and divide by the first. The remainder (6) I reduce to pence, and divide as before. The quotients make the answer, 16.8.

00 By inverting the order of the question it wi'l stand thus, 2. If 6s. buy 9lbs. of tobacco, what will 16s8 buy?

d. s. 16 8 6 12 12

9)72(8 72

72 pence 200 pence.

pence. lbs. pence-As, 72:9::200200

.360

Here the term which asks the question (16:8) is of different denominations; it must, therefore, be reduced to the lowest denomination mentioned (pence) as must also the other term of the same name, confequently, to be the first term.

72)1800(25 lbs. Answer. 144 360

Again—By inverting the order of the question.

3. If 16:8 (=200 pence) buy 25lbs. of tobacco, how much will 6:. (=78 pence) buy?

OPERATION.

These three questions are only the first varied; they shew how any question in this Rule, may be inverted.

4. If loz. of filver cost 6:9, what will be the price of a silver cup that weighs 90z. 4pwts. 16grs.?

02. 1 20	s. 6 12	<i>d</i> . 9	ez. 9 20	pwis.	gts. 16
20pwt. 24	81ps	encë	184pv 24	Vtu	As each of the terms contains dif- ferent denomina- tions, they must all
80 40			7 <i>5</i> 2 968		be reduced to the lowest denomina-
480grs. grs. As 480	<i>d</i> .): 81: 4432	grs. : 4432	4432gr	5.	won meanonen
	162 243 324				
480):	358992(° 3360	747 31 Anj	wer, which to the denominating 1 2)747	tion; th	reduced to the high- us,
•	2299 1920 	> ,	2 0)6	2 3 <i>d</i> . 93 2s. 3	J. 339. Ans.
# 	432				•

122

5. If 6 horses eat 21 bushels of oats in 3 weeks, how many bushels will 20 pories eat in the same time?

Ans. 70 bufbels.

The fame question inverted.

6. If 20 horses eat 70 bushels of oats in 3 weeks, how many bushels will 6 horses eat in the same time?

Ans. 21 bufbels: -

The statement of every question requires thought and consideration;—here are four numbers given in the question; to know which three are to

be employed in the statement there can be no difficulty if the Scholar proceed deliberately and as his rule directs—first, consider which of the given numbers it is, that asks the question; that determined on, put it in the third place, then seek for another number of the same name, or kind, put that in the first place, the second place must now be occupied by that number which is of the same name or kind with the number sought; when these steps are cautiously followed, the Scholar cannot fail to make his statement right.

- 7. If an Ingot of filver weigh 360z. 10pwt. what is it worth at 5s. per ounce?

 Ans. 69 2s. 6d.
- 8. A Goldsmith sold a tankard for £10 12s. at the rate of 5s. 4d. per ounce, I demand the weight of it.

 Ans. 390z. 15past.

there are 30 in the family?

Ans. 9 bushels.

9. If a family of 10 persons spend 10. If a family of 30 persons spend 3 bushels of malt in a month, how 9 bushels of malt in a month, how many bushels will serve them when many bushels will serve a family of 10 persons, the same time?

Ans. 3 bushels.

11. If 12 acres, 3 roods produce 78 quarters, 3 pecks, how much will 35 Ans. 216 quarters, 5 bufbels, 1 peck. acres, 1 rood, 20 poles, produce?

12. If 5 acres 1 rood, produce 26 quarters 2 bushels, how many acres will be required to produce 47 quarters 4 bushels?

Ans. 9 acres, 2 roods.

13. If \$65 men confume 75 barrels of provision in 9 months, how much will 500 men confume in the fame time?

Ans. 1025 barrels.

14. If 500 men confume 10273 barrels of provision, in 9 months, how much will 365 men confume in the same time?

OPERATION.

barrels.
102††
Multiply by 73 the denominator
of the fraction.
306
714
Add 54 the numerator.

Note. In the 14th example, in order to embrace the fraction $(\frac{2}{7}, \frac{4}{7})$ of a barrel) the integers, 102 barrels must be multiplied by the denominator of the fraction, (73) and the numerator, (54) added to the product.

After division, the quotient must be divided by the denominator of the fractions and this last quotient will be the answer, all which may be seen in the example.

The Scholar must remember to do the same in all limitar cases.

As 500: 7500: : 365
7500

182500
2555

5|00|27375|00

73)5475(75 Ans.,
511

36**5** 365 15: If I give 6 Dolls. for the use of 100 Dolls. for 12 months, what must I give for Dolls. 357,82 the same length of time?

OPERATION.

		7.25.
D. D	. D. Cts.	٠.
	: : 357,82	
100	6	
-	D.ci	te.m.
1	00)21 46, 92(21,	
	-	
	146	
	100	
•		
	469	
•	400	
	*	
	692	
*	600	
ς.		
	920	
4 7 7	- 900	

Here in the third term I had two decimal places, (82) or places of cents multiplied by the fecond term (6) I point off two places for cents (,92) in the product, which divided by 100, I point off three decimal places in the quotient equal to the number of decimal places in the dividend (,92 cents and 0 annexed to the remainder) there being no decimals in the divisor.

16. How much land at \$2,50 per acre should be given in exchange for \$60 acres, at \$3,75 per acre?

Ann. 540 acres.

The Scholar is defired to invert and prove the question.

17. If I buy 7lb. of Sugar for 75 cents, how much can I buy for 6 dollars?

Ans. 56lb.

N. B. Sums in Federal Money are of the fame denomination when the decimal places in each are equal.

To reduce fums in federal money to the sume denomination, annex to many cyphers to that sum which has the least number of decimal, places, or places of cents, mills, &c. as shall make up the deficiency.

SINGLE RULE OF THREE DIRECT. SECT. II, 7. 126

18. If I buy 76 yards of cloth for | 19. A man spends \$3,25 per week, \$113,17 what did it cost per Ell Eng- what is that per annum?

Ish? Ans. \$1,861.

Ans. \$169,464.

20. Bought a filver cup weighing 90z. 4pwt. 16grs. for £3 2s. 3d. 334. Ans. 6s. 9d. what was that per ounce?

21. There is a ciftern, which has 4 | cocks; the first will empty in 10 minutes; the fecond, in 20 minutes; the third in 40 minutes; and the fourth in 80 minutes; in what time will all four running together empty it ?

11,25 Cift. would empty Then, Cift. Min. Cift. Min. As 11,25: 60: 1: 5,33 Ans.

of cod fish, for \$780; freight \$37,70; cast a shadow of 6 feet; how high duties and other charges \$30,60; is that steeple whose shadow measwhat must be sell it at, per quintal to ures 153 feet? gain \$143 in the whole? Ans. \$3,671.

The sum of all the expenses of the fish with the Merchant's gain must be found for the fecond term.

22. A man having a piece of land to plant, hired two men and a boy to plant it, one of the men could plant it in 12 days, the other in 15 days, and the boy in 27 days; in how long time would they plant it if they all worked together ? Ans. 5,346 days.

23. A Merchant bought 270 quintals | 24. If a staff 5st. 8in. in length

Ans. 144 feet.

128 F SINGLE RULE OF THREE DIRECT. SECT. II. 7.

25. Bought 12 pieces of cloth each 10 yards at \$1,75 per yard, what came 10 yards at \$1,75 per yard, what came 126. Bought 4 pieces of Holland, 10 yards at \$1,75 per yard, what came 126. Bought 4 pieces of Holland, 10 yards at \$1,75 per yard, what came 126. Bought 4 pieces of Holland, 10 yards at \$1,75 per yard, what came 126. Bought 4 pieces of Holland, 10 yards at \$1,75 per yard, what came 126. Bought 4 pieces of Holland, 10 yards at \$1,75 per yard, what came 126. Bought 4 pieces of Holland, 10 yards at \$1,75 per yard, what came 126. Bought 4 pieces of Holland, 10 yards at \$1,75 per yard, what came 126. Bought 4 pieces of Holland, 10 yards at \$1,75 per yard, what came 126. Bought 4 pieces of Holland, 10 yards at \$1,75 per yard, what came 126. Bought 4 pieces of Holland, 10 yards at \$1,75 per yard, what came 126. Bought 4 pieces of Holland, 10 yards at \$1,75 per yard, what came 126. Bought 4 pieces of Holland, 10 yards at \$1,75 per yard, what came 126. Bought 4 pieces of Holland, 10 yards at \$1,75 per yard, what came 126. Bought 4 pieces of Holland, 10 yards at \$1,75 per yard,
27. Bought 9 Chests of tea, each weighing 3C. 2qrs. 21 lb. at £4 9s. per cwt. what came they to?

Ans. £147 13s. \$\frac{2}{4}d^2\$

28. A Bankrupt owes in all 972 dollars, and his money and effects are but \$607,50; what will a creditor receive on \$11,333?

Au. \$7,083.

29. A owes B < 3475, but B compounds with him for 13s. 4d. on the pound; what must be receive for his debt?

Ans. £2316 13s. 4d.

30. If a person whose rent is \$145 pays \$12,69 of parish taxes, how much should a person pay whose rent is \$378.

Ans. \$32,925.

INVERSE PROPORTION.

IN fome questions the number sought becomes less, when the circumstances from which it is derived become greater. Thus, when the price of goods increases the quantity which may be bought for a given sum, is smaller. When the number of men employed at work is increased, the time in which they may complete it becomes shorter; and, when the activity of any cause is increased, the quantity necessary to produce any given effect is diminished.

These and the like cases belong to the

SINGLE RULE OF THREE INVERSE.

The Single Rule of Three Inverse teaches, by having three numbers given to find a fourth, having the same proportion to the second, as the first has to the third.

If more require less, or less require more, the question belongs to the Single Rule of Three Inverse.

More requiring less, is when the third term is greater than the first, and re-

quires the fourth term to be less than the second.

Less requiring more, is when the third term is less than the first, and requires the fourth term to be greater than the second.

RULE.

"State and reduce the terms as in the rule of three direct; then multiply the first and second terms together, divide the product by the third, and the quotient will be the answer in the same denomination with the second term."

EXAMPLES.

1. If 48 men can build a wall in 24 days, how many men can do the same in 192 days?

OPERATION.

2. If a board be 9 inches broad, how much in length will make a square foot?

InB. InL InB. InL. As 12: 12:: 9:16 Ans. Here the third term is greater than the first, and common sense teaches the fourth term, or answer must be less than the second, for if 48 men can do the work in 24 days, certainly 192 men will do it in less time. In this way it may be determined if a question belong to the Rule of Three Inverse.

3. How many yards of farcenet, 3qrs. wide, will line 9 yards of cloth of 8qrs. wide? Ans. 24 yards.

4. Lent a friend 292 dollars for 6 months; fome time afterwards, he lent me 806 dollars; how long may I keep it to balance the favor?

Atts. 2 months 5 days.

5. A garrifon had provisions for 8 months at the rate of 15 ounces to each person per day; how much must be allowed per day in order that the provisions may last 9\frac{1}{4} months?

Ans. 1212 ounces:

6. A garrifon of 1200 has provisions for 9 months at the rate of 14 ounces per day, how long will the provisions last at the same allowance if the garrifon be reinforced by 400 men?

Ans. 6\frac{1}{4} months.

7.——How must the daily allowance be in order that the provisions may last 9 months after the garrison is reinforced?

Ans. 101 ounces.

132 SINGLE RULE OF THREE INVERSE. Sect. II. 7.

- 8. If a man perform a journey in 15 days, when the day is 12 hours long, in how many will he do it when the day is but 10 hours? Ans. 18 days.
- 9. If a piece of land 40 rods in length, and 4 in breadth make an acre, how wide must it be, when it is but 25 rods long? Ans. 6²/₄ rods.

- 10. There was a certain building raifed in 8 months by 120 workmen, but the fame being demolished it is required to be rebuilt in 2 months; I demand how many men must be employed about it?

 Ans. 480 men.
- 1. How much in length, that is 3 inches broad, will make a fquare foot?

 Ans. 48 inches.

- 12. There is a cistern, having 1 pipe which will empty it in 10 hours; how many pipes of the same capacity will empty it in 24 minutes? Ans. 25 pipes.
- 13. If a field will feed 6 cows 91 days, how long will it feed 21 cows?

 Ans. 26 days.

GENERAL RULE

For stating all questions whether direct or inverse.

- 1. PLACE that number for the third term, which fignifies the fame kind of thing, with what is fought, and confider whether the number fought will be greater or less. If greater place the least of the other terms for the first; but if less, place the greater for the first, and the remaining one for the second
- 2. Multiply the fecond and third terms together, divide the product by the first, and the quotient will be the answer.

EXAMPLES.

1. If 30 horses plough 12 acres, how many will forty plough in the same time ?

OPERATION.

Here because the thing fought is a number of acres, we place 12, the given number of acres for the third term; and because 40 horses will plough more than 12, we make the leffer number, 30, the first term and the greater number, 40 the fecond term.

2. If 40 horses be maintained for a certain sum on hay at 5 cents per stone, how many will be maintained, on the same sum, when the price of hay rises to 8 cents per stone ?

40

Here, because a number of horses is sought we make the given number of horses, 40, the third term, and because fewer will be maintained for the same money, when the price of hay is dearer, we make the greater price, 8 cents, the first term, and the lesser price, 5 cents the fecond.

The first of these examples is direct, the second inverse. Every question consists of a supposition and a demand.

In the first the supposition is, that 30 horses plough 12 acres, and the demand bow many 40 horses will plough? And the first term of the proportion, 30, is found in the supposition, in this and every other direct question.

In the second, the supposition is that 40 borses are maintained on kay at 5 cents per stone, and the demand, how many will be maintained on lay at 8 cents? And the first term of the proportion, 8, is found in the demand, in this and every other inverse question.

- 3. If a quarter of wheat afford 60 4. If in 12 months, 100 dollars gain ten penny loaves, how many eight penny loaves may be obtained from fame fum in 5 months? it ? Ans. 75 leaves.
 - 6 dollars interest, what will gain the
 - Ans. 240 dellars.

134 SUPPLEMENT TO THE SING. R. OF THREE. SECT. II. 7.

Supplement to the Single Kule of Three.

QUESTIONS.

- 1. WHAT is the Single Rule of Three; or, the Rule of Proportion?
- 2. How many kinds of Proportion are there?
- 3. What is it that the Single Rule of Three Direct teaches?
- 4. How can it be known that a question belongs to the Single Rule of

 Three Direct?
- 8. What is understood by more requiring more, and less requiring less?
- 6. How are questions in the Rule of Three stated?
- 7. Having stated the question, how is the answer found in direct Proportion?
- What do you observe of the first and third terms concerning the different denominations, sometimes contained in them?
- 9. When the second term contains different denominations, what is to be done?
- 10. How is it known what denomination the quotient is of?
- 11. If the quotient, or answer, be found in an inferior denomination, what is to be done?
- 12. When the terms are given in Federal Money, how is the operation conducted?
- 13. How are fums in Federal Money reduced to the same denomination?
- 14. When any number of barrels, bales, or pieces, &c. are given, what is the method of procedure?
- 15. What is it that the Single Rule of Three in Inverse teaches?
- 16 How are questions stated in Inverse Proportion?
- 17. What is understood by more requiring less, and less requiring more?
- 18. How is the answer found in the Rule of Three Inverse?
- 19. What is the general Rule for stating all questions, whether Direct or Inverse?

EXERCISES.

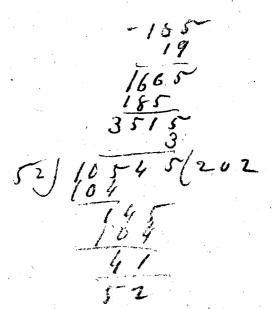
1. If my horse and saddle are worth 18 guineas, and my horse be worth six times as much as my saddle, pray what is the value of my horse?

SECT. II. 7. SUPPLEMENT TO THE SING. R. OF THREE. 135

- 2. How many yards of mattin, that is, half a yard wide, will cover a room that is 18 feet wide, and 30 feet long? Ans. 120 yards.
- 3. Suppose 800 foldiers were place ed in a garrison, and their provisions were computed fufficient for two months; how many foldiers must depart that the provisions may serve them 5 months? Ans. 480.

4. I borrowed 185 quarters of corn when the price was 19s. how muc must I repay, to indemnify the lender, when the price is 17s. 4d.

Ans. 2024:



136 SUPPLEMENT TO THE SING. R. OF THREE. SECT. II. 7.

5. A and B depart from the same place and travel the same road; but A goes 5 day 5 before B at the rate of 20 miles per day; B follows at the rate of 25 miles per day; in what time and distance will be overtake A?

Ans. B will overtake A in 20 days and travel 500 miles.

Here two statements will be necessary; one to ascertain the time, and another to ascertain the distance.

25-20/00/80

100

METHOD

Of affessing town or parish taxes.

1. An inventory of the value of all the estates, both real and personal, and the number of polls, for which each person is ratable, must be taken in separate columns. Then to know what must be paid on the dollar, make 'e total value of the inventory the first term; the tax to be affessed, the second and I dollar, the third, and the quotient will shew the value on the dollar.

NOTE. This method is taken from Mr. PIKE's Arithmetic, with this difference, that here the money is reduced to Federal Currency.

SECT. II. 7. SUPPLEMENT TO THE SING. R. OF THREE. 137

2. Make a table, by multiplying the value on the dollar by 1,2,3,4,5, &c.

3. From the Inventory take the real and personal estates of each man, and find them separately, in the table, which will shew you each man's proportional share of the tax for real and personal estates.

If any part of the tax be averaged on the polls, before stating to find the value on the dollar, deduct the sum of the average tax from the whole sum to be assessed; for which average make a separate column as well as for the real and personal estates.

EXAMPLES.

• Suppose the General Court should grant a tax of 150,000 dollars, of which a certain town is to pay Dolls. 3250,72 and of which the polls being 624 are to pay 75 cents, each; the town's inventory is 69568 dollars; what will it be on the dollar; and what is A's tax (as by the inventory) whose estate, is as follows, viz. real 856 dollars; personal 103 dollars; and he has 4 polls?

Pol. Cts. Pol. Dolls.

1. As 1:,75:: 624: 468 the average part of the tax to be deducted from \$3250,72 and there will remain \$2782,72.

Dolls. Dolls. Cts. Doll. Cts.

2. As 69568: 2782, 72::1:4 on the dollar.

TABLE.

Dolls.	Dolls. cts.	Dolls.	Dolls.	cts.	Dolls	Dolls.
1 is	4	20 is	•	80	200 is	8
2 —	8	30	1	20	300	12
3	12	40 —	. 1	60	400	16
4 —	16	50	· 2	00	500	20
5 —	20	60 —	2	40	∂600 —	24
6-	24	70 —	2	80	700 —	28
7 —	28	80	3	20	800	32
8 —	32	90 —	3	60	900	36
9 —	36	100	· 4	00	1000	40
10-	40	**				
5 — 6 — 7 — 8 — 9 —	20 24 28 32 36	70 — 80 — 90 —	2 3 3	80 20 60	700 — 800 — 900 —	3:3

Now to find what A's rate will be.

His real estate being 856 dollars I find by the Table that 800 dollars is \$32 cts.

that 50 — 2 that 6 — 0 24

Therefore the tax for his real estate is 34 24

In like manner I find the tax for his personal estate to be 4 12

His 4 polls, at 75 cents each, are

41 36

Real. Dolls. Ets.		Polls. Dolls. Cts.	Total. Dolls. Cents.	
34 24	4 12	.3 0	1 - 41 - 36	

§ 8. Pouble Mule of Chree.

THE Double Rule of Three, fometimes called Compound Proportion, teaches, by having five numbers given to find a fixth, which, if the proportion be dired, must bear the same proportion to the fourth and fifth, as the third does to the first and second. But if the proportion be inverse, the fixth number must bear the same proportion to the fourth and fifth, as the first does to the second and third.

RULE.

"1. State the question, by placing the three conditional terms in such order, that that number which is the cause of gain, loss, or action, may possess the sirst place; that which denotes space of time, or distance of place, the second; and that which is the gain, loss, or action, the third."

"2 Prace the other two terms, which have the question, under those of

the fame name."

- "3. Then, if the blank place, or term fought, fall under the third place, the proportion is direct, therefore multiply the three last terms together, for a dividend, and the other two for a divider; then the quotient will be the answer."
- "4. But if the blank fall under the first or second place, the proportion is inverse, wherefore, multiply the first, second, and last terms together, for a dividend, and the other two, for a divisor; the quotient will be the answer."

EXAMPLES.

1. If 100 dollars gain 6 dollars, in 12 months, what will 400 dollars gain in 8 months?

Statement of the question.

D. M. D.

100 : 12 : 6 Terms in the supposition.

100: 12:: 6 Terms in the supposition, or conditional terms.

400: 8 Terms which m ve the question.

Of the three conditional terms, it is evident, that 100 dollars put at interest is that one, which is the cause of gain; consequently, 100 dollars must be the first term; and because, 12 months is the space of time in which the gain is made, this must be the second term; and 6 dollars which is the gain, the third term. The other two terms must then be arranged under those of the same name.

Now as the blank falls under the third place, therefore, the question is in direct proportion, and the answer is found by multiplying the three last terms

together for a dividend and the two first for a divisor.

OPERATION.

1200 Div. 19200 Dividend. .

2. If 100 dollars gain 6 dollars in 12 months, in what time will 400 dollars gain 16?

OPERATION.

D. M. D. 100:12::6 400 16 12 6 2400 divis. 192 100

Here the blank falling under the fecond term, the proportion is indirect.

Therefore multiply the first, second and last terms together for a dividend, and the other two for a divisor.

19200 divided. М. Then, 24|00) 192|00(8 Ans. 192

3. A farmer fells 204 dollars is fold at 60 cents per bushel; what | reap 100 acres in 5 days? is it per bushel when he fells 1000 dollars worth, in 18 years, if he fell the same quantity yearly?

Cts. Y. 60:5::204 ets.m. 18:: 1000: ,816 Ans.

4. If 7 men can reap 84 acres of worth of grain, in 5 years, when it wheat in 12 days; how many men can

> M. D. 7:12::84 M. 5 ; ; 100 ; 20 Ans.

Supplement to the Double Hule of Three.

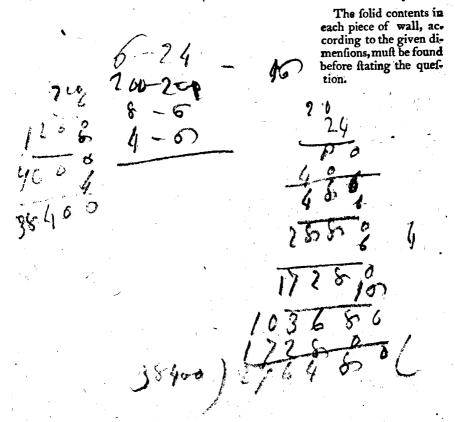
QUESTIONS.

- 1. WHAT is the Double Rule of Three; or Compound Proportion?
- 2. How are questions to be stated in the Double Rule of Three?
- 3. How is it known, after the statement of the question, whether the proportion be direct or inverse?
- 4. When the proportion is Direct, how is the answer to be found?
- 5. When the proportion is Inverse, how is the answer to be found?

EXERCISES.

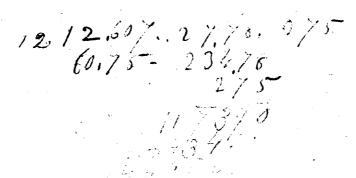
1. If 6 men build a wall 20 feet long, 6 feet high, and 4 feet wide in 16 days, in what time will 24 men build one 200 feet long, 8 feet high and 6 thick?

Ans. 80 days.



SECT. II. 8. SUPPLEMENT TO THE DO. R. OF THREE. 141

2. If the freight of 12Cwt. 2qrs. 6lb. 275 miles, cost \$27,78; how fair may 60cwt. 3qrs. be shipped for \$234,78? Ans. 480 miles.



3. An usurer put out 75 dollars, at | interest; and at the end of 8 months | wall in 6 days; in what time will received for principal and interest, 79 dollars; I demand at what rate per cent he received interest?

Ans. 8 per cent.

4. If 7 men can make 84 rods of 10 men make 150 rods? Ans. 71 days.

142 SUPPLEMENT TO THE DO. R. OF THREE. SECT. II 8.

5. If the freight of 9hhd. of fugar, each weighing 12 Cwt. 20 leagues, cost £16; what must be paid for the freight of 50 tierces ditto, each weighing 2; Cwt. 100 leagues?

Ans. 492 11 10;

§ 9. Practice.

"PRACTICE is a contraction of the Rule of Three Direct, when the first term happens to be an unit, or one; it has its name from its daily use among Merchants and Tradefmen, being an easy and concise method of working most questions, which occur in trade and business.

PROOF. By the Single Rule of Three, Compound Multiplication, or by va-

rying the parts.

Before any advances are made in this rule, the Learner must commit to memory, the following

TABLES.

even parts of Money

OPERATIONS,

Pounds, Shill. Pence, Farthings.

When the price of the given quantity is 1c. 1s. 1d. per pound, yard, &c. then will the quantity itself be the anfwer at the supposed price. Therefore.

CASE 1.

When the price of 1yd. 1lb &c. confills of farthings only; if it be one farthing, take a fourth of the quantity; if a half penny, take a half; if three farthings take a half and a fourth of the quantity and add them. This gives the value in pence, which must be reduced to pounds.

Dollars, Cents, Mills.

RULE.

Multiply the quantity by the price of 1 pound, yard, &c. the product will be the answer.

1. What will 362 yards cost, at \d. per yard?

OPERATION.

2)362 12)181 pence.

15s. 1d. Ans.

Here the quantity stands for the price at one penny per yard, but as two farthings, are but half one penny, therefore dividing the quantity by 2 gives the price at half a penny per yard, which must be reduced to shillings.

2. What will 354; yards cost, at

4d per yard?

OPERATION.

d. q. 4)354 2 12)88 2 7s.4d. 2 Ans.

3. What will 263 yards cost at 3q. per yard?

Ans. 16s. 5¹/₄d.

4. What will 816 yards coft at 1q. per yard?

Ans. 17s.

Dollars, Cents, Mills.

1. What will 362 yards cost at 7 mills per yard?

OPERATION.

9 6 2 quantity. ,0 0 7 price.

\$2, 5 3 4 Answer.

Nors. The answers in the different kinds of money will not always compare, because in the reduction of the price, a small fraction is often lost or gained.

2. What will 354! yards cost, at 3 mills per yard?

OPERATION.

3 5 4 ,5 quantity.

\$10 ,6 3 5 Answer.

3. What will 263 yards cost, at 1 cent per yard?

Am. 52,63.

4. What will 816 yards coft at 3' mills per yard?

Ans. \$2,448.

5. What will 97 yards cost at 3q. per yard?

Ans. 6s. 0^3_4d .

Dollars, Cents, Mills.

5. What will 97 yards cost, at 1 cent per yard?

Ans. ,97 cts.

6. What will 126 yards cost at \d. per yard?

Ans. 5s. 3d.

6. What will 126 yards cost at 7 mills per yard?

Ans. \$0,882.

CASE 2.

When the price of 1lb. 1 yard, &c. confifts of pence, or of pence and farthings; if it be an even part of a shilling, find the value of the given quantity at 1s. per yard, (the quantity itself expresses the price at 1s. per_yard; if there are quarters, &c. write for \frac{1}{4} & 3d. for \frac{1}{2} & 6d. for \frac{1}{4} & 9d.) and divide by that even part, which the price is of 1 shilling. If the price be not an aliquot or even part of 1 shilling, it must be divided into two or more aliquot parts; calculate for these separately, and add the values; the answer will be obtained in shillings, which must be reduced to pounds.

EXAMPLES.

1. What will 476 yards cost, at 7;d. per yard?

OPERATION.

6d. | ½ | 476 Frice at 1s. per yard. 12d. | ‡ | 238 Price at 6d. per yard. 59 6d. price at 1.4d. per yd.

20)29|7 6d. price at 7 d. per yd.

£14 17s. 6d. Answer.

PROOF.

1. By the Rule of Three.

Y. L. s. d Y. As 476: 14 17 6:: 1

20

297 12

476)3570(7d.

3332

238

)952(2q. 952

2. By Compound Multiplication.

6. s. d.

7! price of 1 yard.

,10

6 3 price of 10 yards.

3 2 6 price of 100 yards.

12 10 0 price of 400 yards.

2 3 9 price of 70 gards.

3 9 price of 6 yands.

14 17 6 price of 476 gards.

Dollars, Cents, Mills.

7. What will 476 yards come to at 10 cents 4 mills per yard?

OPERATION.

476 ,104

1904 **4**760

\$49,504 Ans.

PROOF.

ets. m. D. ets. m. yds. 10 4)4 9 5 0 4(476

416

7 9 0

7 2 8

6 2 4 6 2 4

2. What will 176 yards coft, at 91d. per yard ?

OPERATION.

176 value at 1s. per yd. 1 88 value at 6d. per yd. 2 of 44 value at 3d. per yd. 7 4d. value at 1d. per yd.

> 2|0)13|9 4d.—at 9!d. per yd. 66 19s. 4d. Ans.

> > PROOF.

3. What will 5681 yards coft at 7d. per yard?

Ans. 616 11. 53d.

Dollars, Cents, Mills.

8. What will 176 yards coft, at 13 cents, 2 mills per yard? Ans. \$23,232

9. What will 568 yards coft at 9 cents, 7 mills per yard? Ans. \$55,12.

4. What will 6852 yards come to at 21d. per yard?

Ans. 67 2s. 104d.

Dollars, Cents, Mills.

10. What will 6853 yards come to, at 3 cents, 5 mills per yard?

Ans. \$24,001.

5. What will 649½ yards cost, at 10d. per yard? Au. 627 1s. 02d.

11. What will 649; yards coft, at 13 cents, 9 mills per yard?

Ans. \$90,245.

6. What will 6833 yards cost at 81d. per yard?

Ans. £23 10s. 01d.

12. What will 6831 yards coft, at

CASE 3.

If the price of 1lb. 1yd. &c. be shillings and pence, and an even part of 14. Divide the value of the given quantity at 16. per yard by that even part, which the price is of 16. The quotient will be the answer.

EXAMPLES.

1. What will 7191 yards cost at 1s. 22 cents, 3 mills per yard? 4d. per yard?

OPERATION.

£. | 1s4 | 1 | 719 10 price at £1 per yd. 143 18 price at 4s. per yd.

Ans. 47 19 4d. at 1s4 per yd. Here for the fake of ease in the operation, because $5 \times 3 = 15$, therefore I divide the price at one pound per yard by 5, and that quotient by 3, which gives the answer.

2. What will 648 yards cost, at 1s. 6d. per yard? Ans. £54.

Dollars, Gents, Mills.

13. What will 7191 yards cost, at Ans. \$160,448.

14. What will 748 yards cost, at 27 cents, 8 mills per yard? Ans. \$180,144.

3. What will 687 yards cost, at 5s. per yard? Ans. £17 17s. 6d.

Dollars, Cents, Mills.

15. What will 687; yards coft, at 83 cents, 3 mills per yard?

Ann. \$572,687.

CASE 4.

When the price of 1 yand, &c. is shikings, or shillings, pence & farthings and not an even part of £1. Multiply the value of the quantity at 1s. per yard by the number of shillings; for the pence and farthings take parts, as in Case 2, the results added will give the answer, which must be reduced to pounds.

If the price be shillings only, and an even number; multiply by half the price or even number of shillings for one yard, double the unit figure of the product for shillings, the remaining figures will be pounds.

Note. When the quantity contains a fraction, work for the integers, and for the fraction take proportional parts of the rate.

EXAMPLES.

1. What will $167\frac{1}{2}$ yards cost, at 17s. 6d. per yard?

OPERATION.

167

6d. 1 1

17
1169
167
2839 price at 17s. per yd.
83 6—at 6d. per yd.
8 9 price of \(\frac{1}{3}\) yd.
2|0)293|1 3d.

Ans. 6146, 11, 3d.

16. What will 167; yards cost, at \$2,916? Ans. \$488,48.

2. What will 5482 yards cost, at 12s. 4!d. per yard?

An. £3391 19s. 9d.

Dollars, Cents, Mills.

17. What will 5482 yards coft, at \$2,063 per yard?

Ans. \$11309,366.

3. What will 614 yards cost, at 16s. per yard?

OPERATION.

614 . 8 half the price.

4912 double the first figure for £491 4s. Ans. (shillings.

4. What will 176 yards cost, at 12s. per yard?

Ans. £105 12s.

5. What will 36 yards coft, at 7s. 6d. per yard?

Ans. £13 10c.

18. What will 614 yards coft, at \$2,667 per yard?

Ans. \$1637,538.

19. What will 176 yards cost, at 2 dollars per yard? Ans. \$352.

20. What will 36 yards cost, at \$1,25 per yard?

Ans. \$45.

CASE 5.

When the price of 1yd. 1lb. &c. is pounds, shillings and pence; Multiply the quantity by the pounds and if the shillings and pence be an even part of a pound, divide the given quantity by that even part, and add the quotient to the product for the answer; but if they are not an even part of £1, take parts of parts and add them together. Or, you may reduce the pound in the price of 1 yard, &c. to shillings and proceed as in the case before.

EXAMPLES.

1. What will 59 yards cost, at £6 \7s. 6d. per yard?

OPERATION.

5s. is 1 of £1 | 59 value at £1 per yd. 6 | 354—at £6 per yard. 14 15s. at 5s. per yd. 7 7 6d at 2s6 per yd.

Ans. £376 2.6 at £6 7s. 9d.

2. What will 163 yards cost, at £2 8s. per yard?

Ans. £391 4s.

Dollars, Cents, Mills.

21. What will 59 yards colly at \$21,25 per yard?

OPERATION.

D. C. 21,25 59 191 25 1062 5 \$1253 75 Ans.

22. What will 163 yards cost, at & dollars per yard?

Ani. \$13.04.

3. What will 76 yards cost, at £3 2s. 7d. per yard?

OPERATION.

6d. is $\frac{1}{3}$ of 1s. 76 value at 1s. per yd. 62=fbilling in £3 2s.

152 value at 2s. per yd. 456—at 60s. per yd.

1d. is \$ of 6d. 38—at 6d. per yd. 6 4d.—at 1d. per yd.

2|0)475|6 4d.

Ans. £237 16s. 4d.

4. What is the value of 84 yards, at £2 14s. per yard?

Ans. £226 16s.

Dollars, Cents, Mills.

23. What will 76 yards cost, at \$10,43 per yard?

Ans. \$792,68.

24. What is the value of 84 yards at 9 dollars per yard? Ans. \$756.

Supplement to Practice.

QUESTIONS.

- 1. WHAT is Practice ?
- 2. Why is it so called?
- 3. When the price of 1 yard, &c. is farthings, how is the value of any given quantity found at the fame rate?
- 4. When the price consists of pence and farthings, and is an even part of 1s. how is the value of any given quantity found?
- 5. When the price is pence and farthings and not an even part of 1s. what is the method of procedure?
- 6. When the price confifts of shillings, pence and farthings, how is the value of any given quantity found?
- 7. When the price contains shillings and pence and is an even part of £1 how is the operation to be conducted?
- 8. When the price confifts of shillings only, and an even number, what is the most direct way to find the value of any given quantity?
- 9. When the quantity contains fractions, as $\frac{1}{3}$, $\frac{1}{4}$, $\frac{3}{4}$, &c. how are they to be treated?
- 10. When the price confilts of pounds, and lower denominations, how is the value of any given quantity found?
- 11. When the prices are given in Dollars, Cents and Mills, how is the value of any given quantity found in federal money?
- 12. What is the method of proof?
- 13. How are the operations in Federal Money proved?

EXERCISES IN PRACTICE.

In the following exercises, the attention of the Scholar must be excited first to consider to which of the preceding cases each question is to be referred. That being ascertained, he will proceed in the operation according to the instruction there given.

I. What will 7453 yards cost, at 11d. per yard? Ans. 4

Ans. £34 3s. 7d.

Under which of the preceding cases does this question properly belong?

What must be done with the fraction (\frac{3}{4} of a yard) in the quantity \frac{3}{4}.

2. What will 964 yards cost, at 1s. &d. per yard?

Ans. £80 6s. &d.

GPERATION.

3. What will 354% yards coft, at 2d. per yard? Ass. 7s. 42d.

4. What will 316 yards cost at 3d. per yard? Ans. 19s. 9d.

5. What will 567 yards coft, at 11d. per yard?

Ans. 63 10s. 11 d.

6. What will 913! yards coft, at 6d. per yard?

Ans. 622 16s. 9d.

7. What will 912} yards cost, at 9d. per yard?

Ans. 634 4s. 4.d.

8. What will 76 yards coft, at 2d. per yard?

An: 12: 8d.

9. What will 845 yards cost, at 8s. per yard? Ans. £338.

10. What will 91 yards come to at 16s. per yard?

Ans. 672 16s.

11. What will 156‡ yards come to, at 6s. 4d. per yard?

Ans. £49 11s. 2d.

12. What will 96 yards cost, at 10s. 1 d. per yard?

Au. 648 F2.

13. What will 67½ yards cost, at 12s. 2d. per yard? Ans. 641 1s. 3d.

14. What will 843 yards cost, at 6s. 8d. per yard?

Ans. 6281.

15. What will 75 yards coft, at 63 3s. 4d. per yard?

Ans. 6237 10s.

16. What will 59 yards come to, at 66. 7s. 6d. per yard?

Ans. £376 2s. 6d.

17. What will 593 yards come to, at £3 6s. 8d. per yard?

Ans. £199 3s. 4d.

18. What will 68 yards cost, at £4 6s. per yard?

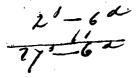
Ans. £292 8s.

N. B. The following questions are left without any answers, that the Scholar may operate and prove each question.

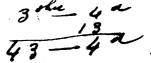
19. What will 11 yards of flannel, at 2s. 6d. per yard, come to?

OPERATION."

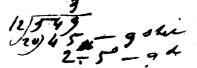
PROOF.



What will 13th of cotton coft, at 9s. 4d. per lb.?



21. What will 183 yards of ribbon come to, at 8d. per yard?



SCHOLAR'S ARITHMETIC.

SECTION III.

HILLIA COMMITTEE COM

Rules oceasionally useful to men in particular callings and pursuits of life.

§ 1. Involution.

INVOLUTION, or the raising of powers is the multiplying of any given number into itself continually, a certain number of times. The quantities in this way produced, are called powers of the given number. Thus,

 $4 \times 4 = 16$ is the 2d. power, or square of 4. $= 4^{\circ}$

 $4\times4\times4$ =64 is the 3d. power, or cube of 4. =43 $4\times4\times4$ =256 is the 4th power, or biquadrate of 4. =44

The given number, (4) is called the first power; and the small figure, which points out the order of the power, is called the *Index* or the *Exp. nent*.

§ 2. Evolution.

EVOLUTION, or the extraction of roots, is the operation by which we

and any root of any given number.

The root is a number whose continual multiplication into itself produces the power, and is denominated the square, cube, biquadrate, or 2d, 3d, 4th, root, &c. accordingly as it is, when raised to the 2d, 3d, 4th, &c. power, equal to that power. Thus 4 is the square root of 16, because $4 \times 4 = 16$. 4 also is the cube root of 64, because $4 \times 4 \times 4 = 64$; and 3 is the square root of 9, and 12 is the square root of 144, and the cube root of 1728, because $12 \times 12 \times 12 = 1728$, and 20 on.

160 EXTRACTION OF THE SQUARE ROOT. Sect. III. 3.

To every number there is a root, although there are numbers, the precise roots of which can never be obtained. But, by the help of decimals, we can approximate towards these roots, to any necessary degree of exactness. Such roots are called Surd Roots, in distinction from those, perfectly accurate, which are called Rational Roots.

The square root is denoted by this character \checkmark placed before the power; the other roots by the same character, with the index of the root placed over it. Thus the square root of 16 is expressed \checkmark 16, and the oube root of 27 is \checkmark 27, &c.

When the power is expressed by several numbers with the sign + or — between them, a line is drawn from the top of the sign over all the parts of

it; thus, the fecond root of 21-5 is $\sqrt{21-5}$, and the 3d. root of 56+8

is $\sqrt{56+8}$, &c.

The second, third, fourth, and fifth powers of the nine digits may be seen in the following

TABLE.

Roots, -	or 1st.	Powers	1	2	3	4	5	6	7	8	9
Squares,	or 2d.	Powers.	1	4	9	16	25	36	49	64	81
Cubes, -	or 3d.	Powers.	ı	8	27	64	125	216	343	512	729
Biquadrates,	or 4th	Powers.	1	16	81	256	625	1296	2401	4096	6561
Surfolids,	or 5th.	Powers.	1		24 3	1024	3125	7776	16807	32768	59049

§ 3. Extraction of the Square Root.

'TO extract the square root of any number, is to find another number which multiplied by, or into itself, will produce the given number; and after the root is found, such a multiplication is a proof of the work.

RULE.

1. "Diffinguish the given number into periods of two figures each, by putting a point over the place of units, another over the place of hundreds, and so on, which points shew the number of figures the root will consist of.

2. "Find the greatest square number in the first, or left hand period, place the root of it at the right hand of the given number (after the manner of a quotient in division) for the first sigure of the root, and the square number,

under the period, and fubtract it therefrom, and to the remainder bring down the next period for a dividend.

3. "Place the double of the root, already found, on the left hand of the dividend for a divisor.

4. "Seek how often the divisor is contained in the dividend (except the right hand figure) and place the answer in the root for the second figure of it, and likewise on the right hand of the divisor; multiply the divisor with the figure last annexed by the figure last placed in the root, and subtract the product from the dividend: To the remainder join the next period for a new dividend.

SECTAIII. 3. EXTRACTION OF THE SQUARE ROOT. 161

5. "Double the figure already found in the root, for a new divisor, (or bring down your last divisor for a new one, doubling the right hand figure of it) and from these, find the next figure in the root as last directed, and continue the operation in the same manner, till you have brought down all the periods.

"Note 1. If, when the given power is pointed off as the power requires, the left hand period should be deficient, it must nevertheless stand as the first

period.

"Note 2. If there be decimals in the given number, it must be pointed both ways from the place of units: If, when there are integers, the first period in the decimals be deficient, it may be completed by annexing so many cyphers as the power requires: And the root must be made to consist of so many whole numbers and decimals as there are periods belonging to each; and when the periods belonging to the given number are exhausted, the operation may be continued at pleasure by annexing cyphers."

EXAMPLES.

1. What is the square root of 729?

OPERATION.

729(27 the root. . The given number being distinguished into periods, I feek the greatest square number in the left hand period 47(329 (7) which is 4, of which the root (2) being placed to the 329 right hand of the given number, after the manner of a quotient, and the square number (4) subtracted from the period (7) to the remainder (3) I bring down the next period (29) making for a dividend, 329. Then the double of the 000 PROOF. 27 root (4) being placed to the left hand for a divisor, I say 27 how often 4 in 32? (excepting 9 the right hand figure) the answer is 7, which I place in the root for the second figure 189 of it, and also to the right hand of the divisor; then multi-54 plying the divisor thus increased by the figure (7) last obtained in the root, I place the product underneath the div-729 idend, and fubtract it therefrom, and the work is done.

DEMONSTRATION.

Of the reason and nature of the various steps in the extraction of the SQUARE ROOT.

The superficial content of any thing, that is, the number of square feet, yards, or inches, &c. contained in the surface of a thing, as of a table or floor, a picture, a field, &c. is found by multiplying the length into the breadth. If the length and breadth be equal, it is a square, then the measure of one of the sides as of a room, is the root, of which the superficial content in the floor of that room, is the second power. So that having the superficial contents of the floor of a square room, if we extract the square root, we shall have the length of one side of that room. On the other hand, having the length of one side of a square room, if we multiply that number into itself, that is to raise it to the second power, we shall then have the superficial contents of the floor of that room.

The extraction of the square root, therefore has this operation on numbers, to arrange the number of which we extract the root into a square form. As it a man should have 625 yards of carpeting, I yard wide, it he extract the square

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162 EXTRACTION OF THE SQUARE ROOT. SECT. III. 3.

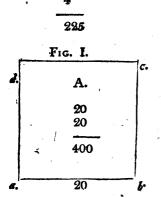
root of that number (625) he will then have the length of one fide of a fquare room, the floor of which, 625 yards, will be just sufficient to cover.—

To proceed then to the demonstration.

EXAMPLE 2. Supposing a man has 625 yards of carpeting, 1 yard wide, what will be the length of one side of a square room, the sloor of which his carpeting will cover?

The first step is to point off the number into periods of two figures each. This determines the number of figures of which the root will confist, and is done on this principle, that the product of any two numbers can have at most but so many places of figures as there are places in both the factors, and at least, but one less, of which any person may satisfy himself at pleasure.

OPERATION.



625(20

The number being pointed off, as the rule directs, we find we have two periods; confequently, the root will confift of two figures. The greatest square number in the left hand period (6) is 4, of which two is the root; therefore, 2 is the first figure of the root, and as it is certain we have one figure more to find in the root, we may for the present supply the place of that figure by a cypher, (20) then 20 will express the just value of that part of the root now obtained. But it must be remembered, that a root is the fide of a square of equal sides. Let us then form a square, A. Fig. I. each side of which shall be supposed 20 yards. Now the fide a b of this square, or either of the sides, shews the root, 20, which we have obtained.

To proceed then by the rule, "place the square number underneath the period subtrate, and to the remainder bring down the next period." Now the square number (4) is the superficial content of the square A—made evident thus—each side of the square A, measures 20 yards, which number multiplied into itself, produces 400, the superficial contents of the square A; also the square number, or the square of the sigure 2 already found in the root, is 4, which placed under the period (6) as it salls in the place of hundreds, is in reality 400, as might be seen also by filling the places to the right hand with cyphers, then 4 subtracted from 6 and to the remainder (2) the next period (25) being brought down, it is plain, the sum 225 has been diminished by the deduction of 400, a number equal to the superficial contents of the square A.

Hence, Fig. I. exhibits the exact progress of the operation. By the operation, 400 yards of the carpeting have been disposed of, and by the figure is

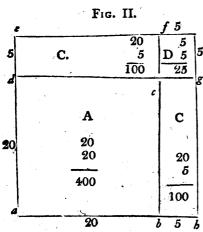
feen the disposition made of them.

Now the square A, is to be enlarged by the addition of the 225 yards which remain, and this addition must be so made that the sigure, at the same time, shall continue to be a complete and perfect square. If the addition be made to one side only, the sigure would lose its square form; it must be made to two sides; for this reason the rule directs, "place the double of the root already sound on the left hand of the dividend for a divisor." The double of the root is just equal to two sides be and c d of the square, A, as may be seen by what solows.

SECT. III. 3. EXTRACTION OF THE SQUARE ROOT, 168

OPERATION continued.

625(25 4	The double of the root is 4 which placed for divisor in place of tens (for it must be remembered that the next figure in the root is to be placed before	nbered,
45)225 225	it) is in reality 40, equal to the fides b c (20 and c d (20) of the square A.)
000		



Again, by the rule, " Seek how often the divisor is contained in the dividend (except the right hand figure) and place the answer in the root, for the second figure of it, and on the right hand of the divisor."

Now if the fides b c and c d of the fquare A, Fig. II. is the length to which the remaining 225 yards are to be added, and the divifor (4 tens) is the fum of these two sides, it is then evident, that 225 divided by the length of the two sides, that is by the divisor (4 tens) will give the breadth of this new addition of the 225 yards to the sides b c and c d of the square, A.

The fquare A = 400 yds.

C $_{e}$ $_{f}$ = 100 —

C $_{g}$ $_{h}$ = 100 —

D = 25 —

But we are directed to "except the right hand figure," and also to "place the quotient figure on the right hand of the divisor;" the reason of which is that the addition, C e f

Proof 635 yds. and C g h to the fides bc and cd of the fquare,
A, do not leave the figure a complete fquare,

but there is a deficiency, D, at the corner. Therefore, in dividing, the right hand figure is expected, to leave something of the dividend, for this deficiency; and as the deficiency, D, is limited by the additions, $C \circ f$ and $C \circ g \circ f$, and as the quotient figure (5) is the width of these additions, consequently equal to one side of the square, D; therefore, the quotient figure (5) placed to the right hand of the divisor (4 tens) and multiplied into itself, gives the contents of the square, D, and the 4 tens—to the sum of the sides, be and gd of the addition $C \circ f$ and $C \circ g \circ f$, multiplied by the quotient sigure, (5) the width of those additions, give the contents $C \circ f$ and $C \circ g \circ f$, which together subtracted from the dividend, and there being no remainder, shew that the 225 yards are disposed in the new additions $C \circ f \circ f$, $C \circ g \circ f$, and D, and the sigure is seen to be continued a complete square.

Confequently, fig. II. shews the dimensions of a square room, 25 yards on a side, the sloor of which, 625 yards of carpeting, 1 yard wide will be sufficient to cover.

The proof is seen by adding together the different parts of the figure.

Such are the principles, on which the operation of extracting the square root is grounded.

164 EXTRACTION of the SQUARE ROOT. Sect. III. 3.

8. What is the fquare root of 10342656? Ans. 3216.

4. What is the square root of 43264? Am. 208.

13342655

5: What is the square root of 964,5192360241? Ans. 31,05671.

SECT. III. 3. EXTRACTION OF THE SQUARE ROOT. 165

6. What is the square root of \$98001?

Ans. 999:

7. What is the square root of 234,69? Ans. 15,3.

8. What is the fquare root of 1030892198,4001?

Ans. 32107,51.

166 SUPPLEMENT TO THE SQUARE ROOT. SECT. III. S.

Supplement to the Square Moot.

QUESTIONS.

- 1. WHAT is to be understood by a root? A power? The second, third, and fourth powers?
- 2. What is the Index, or Exponent?
- 3. What is it to extract the Square Root?
- 4. Why is the given fum pointed off into periods of two figures each ?
- 5. In the operation, having found the first figure in the root, why do we subtract the square number, that is, the square of that figure, from the period in which it was taken?
- 6. Why do we double the root of a divisor?
- 7. In dividing why do we except the right hand figure of the dividend?
- 8. Why do we place the quotient figure in the root and also to the right hand of the divisor?
 - 9. If there be decimals in the given number, how must it be pointed?
 - 10. How is the operation of extracting the Square Root proved?

EXERCISES IN THE SQUARE ROOT.

1. A Clergyman's glebe confifts of three fields; the first contains 5 Acr. 2r. 12 p. the second, 2 ac. 2 r. 15 p. the third 1 ac. 1 r. 14 p in exchange for which the heritors agree to give him a square field equal to all the three. Sought the side of the square?

Ans. 39 poles.

2 - 2 - 15 2 - 2 - 14 and this and get the agreet

2. A General has an army of 4096 men; how many must be place in rank and file to form them into a square?

Answer 64.

SECT. III. 3. SUPPLEMENT TO THE SQUARE ROOT. 167

3. There is a circle whose diameter is 4 inches, what is the diameter of a circle 4 times as large?

Ans. 8 inches.

Note. Square the given diameter, multiply this fquare by the given proportion, and the fquare root of the product will be the diameter required. Do the fame in all fimilar cases.

If the circle of the required diameter were to be less than the circle of the given diameter, by a certain proportion, then the square of the given diameter must have been divided by that proportion.

4. There are two circular ponds in a gentleman's pleasure ground; the diameter of the less is 100 feet, and the greater is three times as large. What is its diameter?

Au. 173,2+

2725 25 65 200 10 4 850 Media de 12000 115,500 104 850 Media de 12000 115,500 104 850 Media de 12000 115,500 Media de 1500 Media 12000 115,500 Media 12000 Media 12000 115,500 Media 12000 Media 12000 115,500 Media 12000 Media 12000 115,500 Media 12000
5. If the diameter of a circle be 12 inches, what will be the diameter of another circle, half so large?

Ans. 8, 48+inches.

168 SUPPLEMENT TO THE SQUARE ROOT. SECT. III. 3.

6. A wall is 36 feet high, and a ditch before it is 27 feet wide 3 what is the length of a ladder, that will reach to the top of the wall from the opposite fides of the ditch?

Answer 45 feet.

Note. A Figure of three fides, like that formed by the wall, the ditch and the ladder is called a right angle triangle, of which, the iquare of the hypotenuse, or slanting fide, (the ladder) is equal to the sum of the squares of the two other fides, that is, the heighth of the wall and the width of the ditch.

7. A Line of 36 yards will exactly reach from the top of a Fort to the opposite bank of a river, known to be 24 yards broad; the height of the wall
is required?

Answer 26,83+yards.

8. Glasgow is 44 miles west from Edinburgh: Peebles is exactly south from Edinburgh, and 49 miles in a straight line from Glasgow; what is the distance-between Edinburgh and Peebles?

Aus. 21,5+miles.

TO extract the Cube Root of any number is to find another number, which multiplied into its square shall produce the given number.

RULE.

1. "Separate the given number into periods of three figures each, by putting a point over the unit figure, and every third figure beyond the place of units.

2. "Find the greatest cube in the left hand period, and put its root in the quotient.

3. Subtract the cube thus found, from the faid period, and to the remainder bring down the next period, and call this the dividend.

4. "Multiply the square of the quotient by 300, calling it the triple square, and the quotient by 30, calling it the triple quotient, and the sum of these call the divisor.

5. "Seek how often the divisor may be had in the dividend, and place the

refult in the quotient.

6. "Multiply the triple square by the last quotient sigure and write the product under the dividend; multiply the square of the last quotient sigure by the triple quotient, and place this product under the last; under all, set the cube of the last quotient sigure, and call their sum the subtrahend.

7. "Subtract the subtrahend from the dividend, and to the remainder bring down the next period for a new dividend, with which proceed as be-

fore, and so on till the whole be finished.

Note. "The same rule must be observed for chatinuing the operation, and pointing for decimals, as in the square root,"

1. What is the cube root of 373248? OPERATION.

373248(72 the root. $7 \times 7 \times 300 = 14700$, the triple square. 210 the triple quotient. 7×30 Divisor 14910)30248 14910 the divifor. **2**9400 840 $14700 \times 2 = 29400$ 8 2×2×210= $2\times2\times2$ 30248 30248 the fubtrahend. 00000 DEMONSTRATION

Of the Reason and Nature of the various steps in the operation of extracting the CUBE ROOT.

Any folid body having fix equal fides, and each of these sides an exact square, is a CUBE, and the measure in length of one of its sides is the root of that cube. For if the measure in feet of any one side of such a body be multiplied three times-into itself, that is, raised to the third power, the product will be the number of folid feet the whole body contains.

And on the other hand, if the cube root of any number of feet be extracted, this root will be the length of one fide of a cubic body, the whole contents of

which will be equal to fuch a number of feet.

2. Supposing a man has 13824 feet of timber, in distinct and separate blocks of one foot each; he wishes to know how large a solid body they will make when laid together, or what will be the length of one of the fides of that cubic body?

To know this, all that is necessary is to extract the cube root of that number, in doing which I propose to illustrate the operation.

OPERATION.

13824(20 8 5824 Fig I. 20 Đ B \boldsymbol{E} 8 20 20 400 20

In this number, pointed off as the rule directs, there are two periods, of course there will be two figures in the root.

The greatest cube in the right hand period, (13) is 8, of which 2 is the root, therefore, 2 placed in the quotient is the first figure of the root, and as it is certain we have one figure more to find in the root, we may for the present supply the place of that one 'figure by a cypher (20) then 20 will express the true value of that part of the root now But it must be remembered, that the cube root is the length of one of the fides of the cubic body, whoselength, breadth, and thickness are equal. Let us then form a cube, Fig. I. each fide of which shall be supposed 20 feet; now the side A. B. of this cube, or either of the fides, shews the root, (20) which we have obtained.

1

8000 feet the folid contents of the CUBE.

The Rule next directs, fubtrate the cube, thus found, from the faid period and to the remainder bring down the next period, &c. Now this cube (8) is the folid contents of the figure we have in representation. Made evident thus—Each fide of this figure is 20, which being raised to the 3d power, that is, the length, breadth and thickness being multiplied into each other, gives the folid contents of that figure—8000 feet. And the cube of the root, (2) which we have obtained is 8, which placed under the period from which it was taken as it falls in the place of the usanta, is 8000, equal to the solid contents of the cube A B C D E F, which being subtracted from the given number of feet, leaves 5824 feet.

Hence Fig. I, exhibits the exact progress of the operation. By the operation 8000 ft. of the timber are disposed of, and the figure shews the disposition made of them, into a square solid pile which measures 20 feet on every side.

Now this figure or pile is to be enlarged by the addition of the 5824 feet, which remains; and this addition must be so made, that the figure or pile, shall continue to be a complete cube, that is have the measure of all its sides equal.

To do this the addition must be made equally to the three different squares,

or faces a, c and b.

The ne,xt step, in the operation is, to find a divisor; and the proper divisor will be, the number of square feet contained in all the points of the figure, to which the addition of the 5824 feet is to be made.

Hence we are directed "multiply the fquare of the quotient by 300," the object of which is, to find the superficial contents of the three faces, a, c, b, to which the addition is now to be made. And that the square of the quotient, multiplied by 300 gives the superficial contents of the faces a, c, b, is evident from what follows.

Side A B=20
Side A F=20
Superficial contents = 400
3

of the face, a.

$$\begin{array}{c}
2 \text{ quotient figure.} \\
2 \\
4 \text{ the fquare of 2} \\
300
\end{array}$$

The triple square 1200=the superficial contents of the faces, a, c, and b.

The two fides A B and A F of the face, a, multiplied into each other, give the fuperficial content of a, and as the faces, a, c, and b, are all equal, therefore, the content of the face, a multiplied by 3, will give the contents of a, c, and b.

The triple fquare of 1200 = the fuperficial contents of the faces a, c, and b.

Here the quotient figure 2, is properly, two tens; for there is another figure to follow it in the root, and the fquare of 2, standing as units, is 4, but its true value is 20 (the fide A B) of which the fquare is 400, we therefore lose two cyphers, and these two cyphers are annexed to the figure 3.—Hence it

appears, that we square the quotient, with a view to find the superficial content of the face, or square a; we multiply the square of the quotient by 3, to find the superficial contents of the three squares, a, c, and b, and two cyphers are annexed to the 3, because in the square of the quotient two cyphers were lost, the quotient requiring a cypher before it in order to express its true value which would throw the quotient (2) into the place of tens, whereas now it stands in the place of units.

Now when the additions are made to the squares a, c, and b, there will evidently be a descious, along the whole length of the sides of the squares between each of the additions, which must be supplied before the signie can be a complete cube. These descious will be 3, as may be seen, Fig. II. n. n. m.

Therefore it is, that we are directed, " multiply the quotient by 30 calling it the triple quotient."

The triple quotient is the fum of the three lines, or fides against which are the deficiencies, n, n, n, all which meet at a point, nigh the centre of the figure. This is evident from what follows.

The deficiencies are 3 in number, they are the whole length of the fides; the length of each fide is 20 feet, therefore 20

Triple quotient 60—to the length of 3 fides where are deficiencies to be filled.

2 quotient. 30

Triple quotient 60 equal to the length of 3 fides, &c.

Here, as before, the quotient lacks a cypher to the right hand to exhibit its true value; the quotient,

itself, is the length of one of the sides, where are the desiciencies; it is multiplied by 3, because there are 3 desiciencies, and a cypher is annexed to the 3 because it has been omitted in the quotient, which gives the same product, as if the true value of the quotient, 20, had been multiplied by 3 alone.

We now have \{ \begin{aligned} \begin{aligned} \text{1200 the triple quare.} \\ \text{60 the triple quotient.} \end{aligned}

The fum of which, 1260 is the divifor, equal the number of square feet contained, in all the points of the figure or pile, to which the addition of the 5824 feet is to be made.

OPERATION continued.

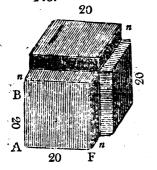
13824(24 the root.

8

Divis. 1260, 324 the dividend.

4800
960
64
5821 fubtrahend.

Fig. II



120C triple fquare.
4 last quotient figure.

This figure in the root, (4) hews the depth of the addition, on every point where it is to be made to the pile or figure, represented, Fig. I.

Fig. II exhibits the additions made to the squares a, c, b, by which they are covered or raised by a depth of 4 feet.

The next step in the operation is to find a subtrahend which subtrahend is the number of solid seet contained in all the additions to the cube, by the last figure 4.

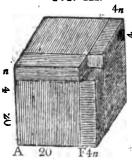
Therefore, the rule directs, " multiply the triple fquare by the last quotient figure."

The triple square, it must be remembered, if the superficial contents of the saces a, c, and b, which multiplied by 4, the depth now added to those saces, or squares, gives the number of solid feet contained in the additions by the last quotient figure 4.

4800 feet, equal to the addition made to the squares, or faces, a, c, b, of Fig.

L. a depth of 4 feet on each.

Fig. III.

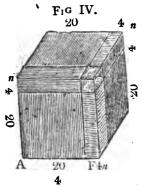


Then, "multiply the square of the last quotient figure by the triple quotient." This is to fill the deficiencies, n, n, n, Fig. II. Now these deficiencies are limited in length, by the length of the sides (20) and the triple quotient is the sum of the length of the deficiencies. They are limited in width by the last quotient sigure (4) the square of which gives the area, or superficial contents at one end, which multiplied into their length, or the triple quotient, which is the same thing, gives the contents of those additions 4n4, 4n, 4n.

60 triple quotient.
16 square of the last quotient figure, Fig. III.

360 60

, 960 feet disposed in the desiciencies, between the additions to the squares, a, c, b, Fig. III. exhibits these desiciencies supplied, 4n4, 4n, 4n, and discovers another desiciency where these approach together, of a corner wanting to make the sigure a complete cabe.



4

16 4 Lastly, "cube the last quotient figure."

This is done to fill the deficiency Fig. III. left at one corner, in filling up the other deficiencies, n, n, n. This corner is limited by those deficiencies on every side, which were 4 fect in breadth, consequently, the square of 4 will be the solid content of the corner, which in Fig. IV. e, e, e, is seen filled.

Now the fum of these additions make the subtrahend, which subtract from the dividend, and the work is done.

64 feet disposed in the corner, e, e, e, where the additions n, n, n, approach together.

FIGURE IV. shews the pile which 13824 solid blocks of one foot each, would make when laid together. The root (24) shews the length of a side. Fig. I. shews the pile which would be formed by 8000 of those blocks, first laid together: Fig. II. and Fig. III. shows the changes which the pile passes through in the addition of the remaining 5824 blocks or feet.

PROOF. By adding the contents of the first figure, and the additions ex-

174 EXTRACTION OF THE CUBE ROOT. SECT. III. 4.

Feet. 8000 Contents of Fig. I.

4800 addition to the faces or squares a, c, and b, Fig. II.

960 addition to fill the deficiencies n, n, n, Fig. III.

64 addition at the corner e, e, e, Fig. IV. where the additions which fill the deficiencies n, n, n, approach together.

13824 Number of blocks or folid feet, all which are now disposed in Fig. IV. forming a pile, or solid body of timber, 24 feet, on a side.

Such is the demonstration of the reason and nature of the various steps in the operation of extracting the cube root. Proper views of the figures, and of those steps in the operation illustrated by them, will not generally be acquired without some diligence or attention. Scholars, more especially will meet with difficulty. For their assistance, small blocks might be formed of wood in imitation of the Figures, with their parts in different pieces. By the help of these, Masters, in most instances, would be able to lead their pupils into right conceptions of those views, which are here given of the nature of this operation.

3. What is the cube root of 21024576?

Ans. 276.

21024576

SECT. III. 4. EXTRACTION OF THE CUBE ROOT. 175

4. What is the cube root of 253395799552?

Anfwer, 6828.

176 EXTRACTION OF THE CUBE ROOT. SECT. III. 4.

5. What is the cube root of 84,604519?

Anfaver, 4,39.

What is the cube root of 2?

Anfever, 1,25+

Supplement to the Cure Front.

- QUESTIONS.

- 1. WHAT is a cube?
- 2. What is understood by the cube root?
- 3. What is it to extract the cube root?
- 4. In the operation having found the first figure of the root, why is the cube of it subtracted from the period in which it was taken?
- 5. Why is the fquare of the quotient multiplied by 300?
- 6. Why is the quotient multiplied by 30?
- 7. Why do we add the triple square and the triple quotient together, and the fum of them call the divisor?
- 8. To find a fubtrahend, why do we multiply the triple square by the last quotient figure? The square of the last quotient figure by the triple quotient? Why do we cube the quotient figure? Why do these sums added, make the fubtrahend?
- 9. How is the operation proved?

EXERCISES IN THE CUBE ROOT.

1. If a bullet 6 inches diameter weigh 32lb. what will a bullet of the same metal weigh, whose diameter is 3 inches ? Ans. 4lb.

Nors. " The folid contents of fimilar figures are in proportion to each other, as the cubes of their fimilar fides, or diameters."

178 SUPPLEMENT TO THE CUBE ROOT. SECT. IH. 4.

2. What is the fide of a cubical mound equal to one 288 feet long, 216 broad, and 48 high?

Ans. 144 feet.

3. There is a cubical vessel, whose side is 2 feet: I demand the side of a vessel, which shall contain three times as much?

Aus. 2 feet 10 inches and $\frac{3}{5}$ nearly.

Nors. Cube the given fide, multiply it by the given proportion, and the cube root of the product will be the fide fought.

§ 5. Fellowship.

FELLOWSHIP is a rule by which merchants and others, trading in partnership, compute their particular shares of the gain or loss, in proportion to their stock and the time of its continuance in trade.

It is of two kinds, Single and Double.

Single Fellowship,

Is when the flocks are employed equal times.

RULE.

As the whole fum of the stocks is to the whole gain or loss, so is each man's particular stock to his particular share of the gain or loss.

PROOF. Add all the shares of the gain or loss together; and, if the work be right, the sum will be equal to the whole gain or loss.

EXAMPLES.

1. Two merchants, A and B, make a joint stock of 200 dollars: A puts in 75 dollars, and B 125 dollars; they trade and gain 50 dollars. What is each man's share of the gain?

OPERATION.

Dolls. Dolls.	Dolls.	*
As 200 : 50 : :	75 As	200:50::125
75	•	125
		·
250	•	250
350	•	100
	cts.	50
200)3750(18	.75 A's Share.	D, čts.
200	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	200)6250(31,25 D's Thare.
·		600
1750		**************************************
1600		250
-	*	200
1500		**************************************
1400		500
		400
1000	18,75 A's fbas	re.
1000	31,25 B's shar	e. 1000
		1000
-	50,00 proof.	
	~ -, Fj.	

2. Divide the number 360 into 4 such parts, which shall be to each other as 3, 4, 5, and 6.

60 80 100 120 \ Answer.

360 Proof.

3. A man died leaving 3 sons, to whom he bequeathed his estate in the following manner, viz. to the eldest he gave 184 dollars, to the second 155 dollars, and to the third 96 dollars; but when his debts were paid, there were but 184 dollars left: What is each one's proportion of his estate?

Ans. 77,829 65,563 Abares.

4. A and B companied:—A put in £45, and took \(\frac{1}{5}\) of the gain: what did B put in?

Ans. £30.

85

Double Fellowship.

DOUBLE FELLOWSHIP, or Fellowship with times of partners are continued unequal times.

RULE.

Multiply each man's stock by the time it was continued in trade. Then, as the whole sum of the products is to the whole gain or loss, so is each man's particular product to his particular share of the loss or gain.

EXAMPLES.

1. A, B and C, entered into partnership: A put in 85 dollars for 8 months: B put in 60 dollars for 10 months; and C put in 120 dollars for 3 months; by missertune they lost 41 dollars: What must each man sustain of the loss?

OPERATION.

120

680 A's product.

8	10	3	600 B's product. 360 C's product.	
680	600	360	1640	./
As 1640:	41 : : 680 680		As 1640 : 41 : : 600 600	
	680 20		164 0)2460 0(15 B's lo	ofs.
164 0)27 16	88 0(17 A's 1 4	ofs.	820 820	٠
11 11	48 48	· /	*	
00	000		. 6	1
-	60 60		Bolls. 17 A's loss. 15 B's loss. 9 C's loss.	•
	 60(9 C's loss	· , ·	41 Proof.	
9000	5 , , , ,			

B, and C, trade together: A, at first put in 480 dollars for 8 months, 3. At in 200 dollars more, and continued the whole in trade 8 months follower; at the end of which he took out his whole stock: B put in 800 dolders for 9 months, then took out \$583,333 and continued the rest in trade 3 months, C put in \$366,666 for 10 months, then put in 250 dollars more, and continued the whole in trade 6 months longer. At the end of their partmership, they had cleared 1000 dollars; what is each man's share of the gain?

Ans. Dolls. 378,827 A's share.

---- 320,452 B's share. ---- 300,721 C's share.

Supplement to Fellows!

QUESTIONS.

- 1. WHAT is Fellowship?
- 2. Of how many kinds is Fellowship?
- 3. What is fingle Fellowship?
- 4. What is the rule for operating in Single Fellowship?
- 5. What is double Fellowship?
- 6. What is the rule for operating in double Fellowship?
- 7. How is Fellowship proved?

EXERCISES IN FELLOWSHIP.

A, B, and C, hold a pasture in common for which they pay £20 per annum. In this pasture, A had 40 oxen for 76 days; B had 36 oxen for 50 days, and C had 50 oxen for 90 days. I demand what part each of these tenants ought to pay for the £20?

Aus. 6 10 2 $1\frac{2}{0}\frac{3}{4}\frac{4}{0}$ A's part. 3 17 1 $0\frac{3}{0}\frac{4}{3}\frac{1}{0}$ B's part. 9 12 8 $2\frac{4}{0}\frac{1}{3}\frac{1}{0}$ C's part. 3.

§ 6. Barter.

BARTER is the exchanging of one commodity for another, and teaches merchants fo to proportion their quantities, that neither shall sustain loss. PROOF. By changing the order of the question.

RULE.

1. When the quantity of one commodity is given, with its value, or the value of its integer, as also the value of the integer of some other commodity to be exchanged for it, to find the quantity of this commodity: Find the value of the commodity of which the quantity is given, then find how much of the other commodity at the rate proposed, may be had for that sum.

2. If the quantities of both commodities be given, and it should be required to find how much of some other commodity, or how much money should be given, for the inequality of their values: Find the separate value of the two given commodities, subtract the less from the greater, and the remainder will be the balance, or

value of the other commodity.

3. If one commodity is rated above the ready money price, to find the bartering price of the other: Say, as the ready money price of the one is to the bartering price to is that of the other to its bartering price.

EXAMPLES.

1. How much coffee, at 25 cents per lb. can I have for 56 lb. of tea at 43 cents per lb.?

operation.
5 6 lb. of tea.
4 3 per lb.

2 2 5

2. I have 760 gallons of molasses at 37 cents, 5 mills, per gallon, which I would exchange for 66 Cwt. 2qr. of cheese, at 4 dollars per Cwt. Must I pay or receive money and how much?

And must receive 19 dolls.

3. A and B, barter; A has 150 bushels of wheat at 5s. 9d. per bushel, for which B gives 65 bushels of barley, worth 2s. 10d. per bushel, and the balance in oats at 2s. 1d. per bushel; what quantity of oats must A receive from B?

Answer, 325 bushels.

4. A has linen cloth worth 20d. an Ell, ready money; but in barter he will have two shillings; B has broadcloth worth 14s. 6d. per yard ready money; at what price ought the broad cloth to be rated in barter?

Answer, 17s. 4d. 3q. 4per yard.

Supplement to Barter.

QUESTIONS. 1

- 1. WHAT is Barter?
- 2. When and how does this rule become useful to merchants?
- 3. When a given quantity of one commodity is bartered for some other commodity, how is the quantity that will be required of this last commodity found?
- 4. If the quantity of both commodities be given and it be required to know how much of some other commodity, or how much money must be given for the inequality, what is the method of procedure?
- 5. If one commodity be rated above the money price, how do you proceed to find the bartering price of the other commodity?
- 6. How is Barter proved ?

EXERCISES.

1. A and B bartered: A had 41 Cwt. of hops, 30s. per Cwt. for which B gave him 20 in money, and the reft in prunes at 5d. per lb. I demand how many prunes B gave A besides the £20?

Ans. 17 G. 3grs. 4lb.

2)0002 (1) 11002 (1)

2. How much wine, at \$1,28 per gallon, must I have for 26 Cwt. 2qr. 14lb. of raisins, at \$9,444 per Cwt. Ans. 196 gal. 1qt. 1pt. and \(\frac{1}{2}\) very nearly.

§ 7. Aoss and Gain.

* LOSS and GAIN is a rule which enables merchants to estimate their prof. it or loss, in buying and felling goods; also to raise or fall the price of them. fo as to gain, or lose so much per cent."

CASE 1.

To know what is gained or lost per cent. First, find what the gain or loss is by fubtraction; then, as the price it cost is to the gain or loss, so is 100 dollars (or £100) to the gain or loss, per cent.

EXAMPLES.

1. If I buy candles at 16 cents, 7 mills per lb. and sell them at 20 cents and sold the same at 90 cents per lb. per lb. what shall I gain per cent. or what was the loss per cent. ? in laying out 100 dollars?

2. Bought indigo, at \$1,20 per lb. Ans. 25 dollars.

OPERATION.

I fell at ,20 per lb. bought at ,167 per lb.

I gain ,038 per lb.

3. Bought 37 gallons of Brandy, at \$1,10 per gallon, and fold it for \$40; what was gained or lost per Ans. \$1,719 lofs.

4. Bought hats at 4s. a piece, and fold them again at 4s9; what is the profit in laying out £100? Ans. 618,15s.

CASE 2.

To know how a commodity must be fold to gain or lose so much per cent. As 100 dollars (or £100) is to the price; so is 100 dollars (or £100) with the prosit added, or loss subtracted, to the gaining or losing price.

EXAMPLES.

1. If I buy wheat at \$1,25 per bushel, how must I sell it to gain 15 per cent?

2. If a barrel of rum cost 15 dollars, how must it be fold to lose 10 per cent?

Aus. \$13,50,

3. If 120 lb. of freel cost £7 how must I sell it per lb. to gain £15; per cent?

Ans. 1:4 per lb.

Supplement to Logg and Gain.

QUESTIONS.

- 1. What is Lofs and Gain?
- 2. Having the price at which goods are bought and fold, how is the Loss or Gain estimated?
- 3. To know how much a commodity must be valued at to gain or lose so much per cent. what is the method of procedure?
- 4. How may questions in Loss and Gain be proved?

EXERCISES.

1. A draper bought 100 yards of broadcloth for £56. I demand how he must sell it per yard, to gain £15 in laying out £100? Ans. 12s. 10d. 2q. 200.

^{2.} Bought 30 hogsheads of molasses, at 600 dollars; paid in duties \$20,66; for freight \$40,78; for porterage \$6,05 and for insurance, \$30,84. If I sell it at 26 dollars per hogshead, how much shall I gain per cent.?

Ans. \$11,695.

§ 8. Turdecimals;

OR

CROSS MULTIPLICATION.

THIS rule is particularly useful to Workmen and Artificers in casting up the contents of their work.

Dimensions are taken in feet, inches and parts. Inches and parts 'are

fometimes called primes ('), feconds ("), thirds ("), and fourths ("").

TABLE. By this rule also may be calculated the folid contents of bodies, having the meas-

12 Thirds, - 1 Second. ures of their different fides, and is very

12 Seconds, - 1 Inch or Prime. useful, therefore, in measuring wood.

12 Inches or Pr. 1 Foot.

RULE.

1. Under the multiplicand write the corresponding denominations of the multiplier.

2. Multiply each term in the multiplicand, beginning at the lowest, by the feet in the multiplier, and write the result of each under its respective term, observing to carry an unit for every 12, from each lower denomination to its superior.

3. In the fame manner multiply the multiplicand by the inches in the multiplier, and write the result of each term in the multiplicand thus multiplied,

one place to the right hand in the product.

4. Proceed in the same manner with the other parts in the multiplier, which if seconds, write the result two places to the right hand; if thirds, three places, &c. and their sum will be the answer required.

The more easily to comprehend the rule, Note. Feet multiplied by Feet give feet.—Feet multiplied by Inches vive

feet.—Feet multiplied by Inches give Inches.—Feet multiplied by Seconds give Seconds —Inches multiplied by Inches give Seconds.—Inches multiplied by Seconds give Thirds.—Seconds multiplied by Seconds give Fourths.

EXAMPLES.

1. Multiply 7 feet, 3 inches, 2 Seconds, by 1 foot, 7 inches, and 3 Seconds.

OPERATION.

F. I. "
7 3 2
1 7 3
7 3 2 "
4 2 10 2 ""
1 9 9 6

Prod. 11 7 9 11 6

Here I multiply the 7f. 3in. 2" by the 1f. in the multiplier, which gives feconds, inches and feet.

Next I multiply the fame 7f. 3in. 2" by the 7in. faying 7 times 2 is 14 which is once 12 and 2 over, which (2) I fet down one place to the right hand, that is in the place of thirds, and carry 1 to the next place, and proceed in the fame manner with the other terms. Lastly I multiply the multiplicand by the 3" fay-

ing 3 times 2 is 6 which I fet down two places to the right hand and so proceed with the other terms of the multiplicand. The sum of all the products is the answer.

5. Multiply 7f. lin. 9" by 7f. Sin. 9" Produst 55f. 2in. 9" 3" 9"" 6. Multiply 9f. 8in. 7" by 12f 3in. 10" Produā 119f. 8' 2" 10" 16""

7. How much wood in a load which measures 10f. in length, 3f. 9iu. in width, and 4f. 8in. in height; and how much will it cost at 1 dol. 33cts. per cord?

Ans. 1 cord, and 47 folid feet over; it will cost 1 dol. 81 cts. 8m.

Or, we may multiply by the feet as already directed, and for the inches, take such parts of the multiplicand, &c. as the inches are aliquot or even parts of a foot, as done in the rule of Practice.

8. How many square feet in a board of 16 feet, 4 inches in length, and 2

feet, 8 inches wide?

OPERATION !

	Ft.	in.	
6 inches is	16	4	
	2	8	
	32	8	
2	-1 8	2	"
	2	8.	8
Ans.	43	6	8

Here, in the first place I multiply the 16st. 4in. by the feet (2) of the multiplier; the inches (8) not being an even part of a foot, I take such as are an even part; thus, 6in. is half a foot, therefore divide the multiplicand by 2 for 6 inches, and that quotient by 3, (2in. is τ of 6 inches) for 2 inches, all which being added, give the product of 16 feet, 4 inches multiplied by 2st. 8in.

9. Another board is 18 feet 9 inches in length, and 2 feet, 6 inches wide, how many square feet does it contain?

Ans. 46f. 10in. 6".

By Practice.

By Duodecimals.

10. There is a stock of 15 boards, 12 feet 8 inches in length, and 13 inches wide; how many feet of boards does the stock contain?

By Practice.

Ans. 205 f et 10 inches. By Duodecimals.

Supplement to Duovecimals.

QUESTIONS.

- 1. OF what use are Duodecimals? To whom more especially are they useful?
- 2. In what are dimensions taken!
- 3. How do you proceed in the multiplication of Duodecimals?
- 4.' For what number do you carry?
- 5. What do you observe in regard to setting down the product different from what is common in the multiplication of other numbers?
- 6. Of what term is the product which arises from the multiplication of feet by inches? Feet by feconds? Inches by inches? Inches by feconds? Seconds by feconds?
- 7. In what way can the operation be varied?

EXERCISES.

1. Multiply 76 feet 3 inches 9 feeends, by 84 feet 7 inches 11 feconds.

OPERATION.
F. I. "
6 inches is \(\frac{1}{2} \))76 3 9
84 7 11

 $76 \times 4 =$ 304 $76 \times 8 = 608$ 0 0 21 .0 3×84= 0 111 $9 \times 84 =$ 5 3 0 $I.1\frac{1}{9}$ 38 1 10 **~6**½) 6 4 3 9 "" 31) and 21) 3 2 1 10 7 0 11 3 1 1 0 8

Prod. 6460 7 1 8 3

3. How many fquare feet in a stock of 12 boards, 17f. 7' long, and, 1f. 5in. wide?

Ans. 298f. 11'.

2. What is the product of 371 feet 2 inches 6 feconds, multiplied by 181f. 1in. 9".

Ans. 67242f. 10in. 1" 4" 6""

4. How many cubic feet of wood in a load 6f. 7' long, 3f. 5' high, and 3f. 8' wide?

Ans. 82f. 5' 8' 4"

194 SUPPLEMENT TO DUODECIMALS. Sect. III. 8,

The Dimensions of Wainscotting, Paving, Plastering, and Painting, are taken in Feet and Inches, and the contents given in Yards.

PAINTERS AND JOINERS.

To find the dimensions of their work, take a line and apply one end of it to any corner of the room, then measure the room going into every corner with the line, till you come to the place where you first began; then see how many feet and inches the string contains; this call the Compass or round, which multiplied into the height of the room, and the product divided by 9, the quotient will be the contents in yards.

EXAMPLES.

- 1. If the height of a room painted be 12f. 4in. and the compass 84f. 11in. how many square yards does it contain? Ans. 116 Y. 3f. 3' 8'
- 2. There is a room wainscotted the compass of which is 47f. 3' and the height 7f. 6'. What is the content in square yards?

 Ans. 39 T. 3f. 4' 6'

84 to 11 am 3 2 - 4 3 3 9 8

GLAIZERS' WORK BY THE FOOT.

To find the dimensions of their work, multiply the height of windows by their breadth.

EXAMPLES.

There is a house with 4 tiers of windows, and 4 windows in a tier; the height of the first tier is 6s. 8s; of the second 5s. 9s; of the third, 4s. 6s and of the sourth, 3s. 10s; and the breadth of each is 3s. 5s; What will the glazing come to at 19 cents per foot?

Ans. \$53,88.

§ 9. Alligation,

ALLIGATION is the method of mixing two or more simples of different qualities, so that the composition may be of a mean or middle quality. of two kinds, Medial and Alternate.

ALLIGATION MEDIAL.

Alligation Medial is when the quantities and prices of feveral things are given, to find the mean price of the mixture compounded of those things.

RULE.

As the fum of the quantities or whole composition is to their total value so is any part of the composition to its value or mean price.

EXAMPLES.

1. A Farmer mingled 19 bushels of wheat at 6s. per bushel, and 40 bushels of rye, at 4s. per bushel, and 12 bushels of barley, at 3s. per bushel together, I demand what a bushel of this mixture is worth?

Busb. Bush. £. s. 19 Wheat, at 6 is 5 14 As 71: 15 10:: 1 40 Rye, — 4 —8 12 Barley, __ 3 -71)310(4s.4d.141q.Ans. Sum of the Amples 71 Total value 15 10 26 2. A refiner having 5lb. of filver bullion, 12 of 80z. fine, 10lb. of 70z. fine, and 15lb. of 6oz. fine, would melt all together; I demand)312(4d. what fineness 1lb. of this mass shall be? 284 Ans. 602. 13pwts. 8grs. fine. 28

)112(1₉₆

ALLIGATION ALTERNATE,

Is the method of finding what quantity of any number of fimples, whose rates are given will compose a mixture of a given rate; it is, therefore, the reverse of Alligation Medial, and may be proved by it.

RULE.

- 1. Write the prices of the simples, the least uppermost, &c. in a column under each other.
- 2. Connect with a continued line the price of each simple or ingredient, which is less than that of the compound, with one or any number of those that are greater than the compound, and each greater rate or price with one or any number of those that are less.

3. Write the difference between the mean rate or price and that of each

of the simples, opposite to the rates with which they are connected.

4. Then if only one difference stand against any rate, it will be the quantity belonging to that rate, but if there be several, their sum will be the quantity.

Note. Questions in this rule admit of as many various answers as there

are various ways of connecting the rates of the ingredients together.

EXAMPLES.

1. A goldfmith would mix gold of 18 carats fine, with fome of 16, 19, 22 and 24 carats fine, to that the compound may be 20 carats fine; what quantity of each must be take?

Mix 20 car.
$$\begin{cases}
16 & 7 \\
18 & 2 \\
19 & 2 \\
24 & 4
\end{cases}$$

$$\begin{cases}
16 & 7 \\
2 & 7 \\
2 & 7 \\
2 & 7 \\
3 & 7 \\
4 & 7 \\
4
\end{cases}$$
OPERATION.

PROOF.

PROOF.

16 × 4 = 64

18 × 2 = 36

18 × 2 = 36

22 × 3 = 66

24 × 4 = 96

15 --- 20 carats fine 15)300(20 car. fine.

2. A Druggist had several sorts of Tea, viz. one fort at 12s. ber lb. another sort at 11s. a third at 9s. and a sourth at 8s. per lb. I demand how much of each fort he must mix together, that the whole quantity may be afforded at 10s. per lb.

$$\begin{array}{c} 1b. & s.p.lb. \\ 2 & \text{at } 12 \\ 1 & \text{at } 11 \\ 1 & \text{at } 9 \\ 2 & \text{at } 8 \\ b. & s.p.lb. \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 2 & \text{at } 11 \\ 2 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 1 & \text{at } 12 \\ 2 & \text{at } 11 \\ 2 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 1 & \text{at } 12 \\ 2 & \text{at } 11 \\ 2 & \text{at } 9 \\ 1 & \text{at } 8 \\ \end{array} \begin{array}{c} 1 & \text{at } 12 \\ 2 & \text{at } 11 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 1 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 1 & \text{at } 11 \\ 3 & \text{at } 9 \\ 2 & \text{at } 8 \\ \end{array} \begin{array}{c} 2 & \text{at } 12 \\ 3 & \text{at } 11 \\ 1 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 2 & \text{at } 12 \\ 3 & \text{at } 11 \\ 1 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array} \begin{array}{c} 3 & \text{at } 12 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 11 \\ 3 & \text{at } 9 \\ 3 & \text{at } 8 \\ \end{array}$$

Note. These seven answers arise from as many different ways of linking the rates of the simples together.

CASE 2.

When the rates of all the ingredients, the quantity of but one of them, and the mean rate of the whole mixture are given to find the several quantities of the rest in proportion to the given quantity, take the difference between each price and the mean rate as before. Then say, price and the mean rate as before.

As the difference of that simple whose quantity is given, Is to the given quantity, So is the rest of the differences feverally; To the feveral quantities required.

EXAMPLES.

1. How much wine, at 80 cents, at 88, and 92 cents per gallon, must be mixed with four gallons of wine at 78 cents per gallon, fo that the mixture may be worth 86 cents per gallon?

86
$$\begin{cases} 75 & 6+2 = 8 \text{ ftands against the given quantity.} \\ 88 & 2+6 = 8 \\ 6+11 = 17 \\ 11+6 = 17 \\ 11+6 = 17 \end{cases}$$
As 8: 4::
$$\begin{cases} 8: 4 \text{ at } 80 \\ 17: 8\frac{1}{9} - 88 \text{ per. gal. The answer.} \\ 17: 8\frac{1}{9} - 92 \end{cases}$$
A non-being determined to vir 10 by the cof wheat at 4. per by the

A man being determined to mix 10 bushels of wheat at 4s. per bushel, with rye at 3s. with barley at 2s. and with oats at 1s. per bushel; I demand how much rye, barley, and oats must be mixed with the 10 bushels of wheat that the whole may be fold at 28d. per bushel.

CASÉ 3.

When the rates of the several ingredients, the quantity to be compounded, and the mean rate of the whole mixture, are given to find how much of each fort will make up the quantity; find the difference between the mean rate, &c. as in case 1. Then,

As the fum of the quantities, or differences, Is to the given quantity or whole composition; So is the difference of each rate, To the required quantity of each rate.

EXAMPLES.

1. How many gallons of water of no value, must be mixed with brandy, at one dollar twenty cents per gallon, so as to fill a vessel of 75 gallons, that may be afforded at 92 cents per gallon?

2. Suppose I have 4 forts of currants, of 8d. 12d. 18d. and 22d. per lb. of which I would mix 120lb. and so much of each fort as to sell them at 16d. per lb. how much of each must I take?

Ans.
$$\begin{cases}
lb. & \text{at } d. \\
36 & - 8 \\
12 & - 12 \\
24 & - 18 \\
48 & - 22
\end{cases}$$
 per lb.

5. A grocer has currants of 4d. 6d. 9d. and 11d. per lb. and he would make a mixture of 240 lb. fo that it might be afforded at 8d. per lb. how much of each fort must be take?

Ans.
$$\begin{cases}
b. & \text{at } d. \\
72 - 4 \\
24 - 6 \\
48 - 9 \\
96 - 11
\end{cases}$$
 per lb.

Supplement to Alligation.

QUESTIONS.

- 1. What is Alligation?
- 2. Of how many kinds is Alligation?
- 3. What is Alligation Medial?
- 4. What is the rule for operating?
- 5. What is Alligation ALTERNATE?
- 6. When a number of ingredients of different prices are mixed together, how do we proceed to find the mean price of the compound or mixture?
- 7. When one of the ingredients is limited to a certain quantity, what is the method of procedure?
- '8. When the whole composition is limited to a certain quantity, how do you proceed?
- 9. How is Alligation proved?

EXERCISES.

1. A Grocer would mix three forts of fugar together; one fort at 10d. per lb. another at 7d. and another at 6d. how much of each fort must be take that the mixture may be fold for 8d. per lb.?

Ans. 3lb. at 10d. 2 at 7d. and 2 at 6d.

2. A Goldsmith has several sorts of gold; some of 24 carats sine, some of 22, and some of 18 carats sine, and he would have compounded of these forts the quantity of 60 oz. of 20 carats sine; I demand how much of each sort he must have?

Ans. 12 oz. 24 carats fine, 12 at 22 carats fine, and 36 at 18 carats fine.

§ 10. Position.

POSITION is a rule which, by false or supposed numbers, taken at pleasure, discovers the true one required. It is of two kinds, Single and Double.

SINGLE POSITION,

Is the working with one supposed number, as if it were the true one, to find the true number.

RULE.

1. Take any number and perform the fame operations with it as are defcribed to be performed in the question.

2. Then fay; as the fum of the errors is to the given fum, so is the fup-

posed number to the true one required.

Proof. Add the feveral parts of the fum together, and if it agree with the fum, it is right.

EXAMPLES.

1. Two men, A and B, having found a bag of money, disputed who should have it; A said the half third, and one fourth of the money made 130 dollars, and if B could tell how much was in it, he should have it all, otherwise he should have nothing; I demand how much was in the bag?

,	UPERATION.
Suppose 60 dollars.	As 65: 130:: 60
	60
The half 30	
-third 20	65)7800(120 dollars, the answer.
—fourth 15	65
) 	
~ 65	130
<u> </u>	130
	

2. A B and C talking of their ages, B faid his age was once and a half the age of A; C faid his age was twice and one tenth the age of both and that the fum of their ages was 93; what was the age of each?

Ans. A's 12, B's 18, C's 63 years.

3. A person having spent $\frac{1}{3}$ and $\frac{1}{3}$ of his money, had $626\frac{2}{3}$ left; what had he at first? Ans. 6160

4. Seven eighths of a certain number exceeds four fifths by 6; what is that number?

Am. 80.

DOUBLE POSITION.

DOUBLE POSITION is that which discovers the true number, or number sought, by making use of two supposed numbers.

RULE.

1. Take only two numbers and proceed with them according to the conditions of the question.

2. Place each error against its respective position or supposed number; if

the error be too great, mark it with +; if too small with -

3. Multiply them cross wife, the first position by the last error, and the last

position by the first error.

4. If they be alike, that is, both greater or both less than the given number, divide the difference of the products by the difference of the errors, and the quotient will be the answer; but if the errors be unlike, divide the sum of the products by the sum of the errors, and the quotient will be the answer.

EXAMPLES.

1. A man lying at the point of death, left to his three fons all his estate, viz. to F half wanting 50 dollars; to G one third; and to H the rest, which was 10 dollars less than the share of G. I demand the sum left, and each son's share.

OPERATION.

Suppose the fum 300 dollars.

Again, Suppose the sum 900 dollars.

Then, $300 \div 2 - 50 = 100$ F's part. $300 \div 3 = 100$ G's part. G's part 100 - 10 = 90 H's part.

Then, 900÷2-50=400 F's part. 900÷ 3=300 G's part. G's part 300-10=290 H's part.

Sum of all their parts 290

Sum of all their parts 990

Error 10-

Error 90+

Having proceeded with the supposed numbers according to the conditions of the question, the sum of all their parts must be subtracted from the supposed number; thus the 290 is subtracted from 300, the supposed number, &c.

Sum of the errors. 100)3

160)36000(360 Answer.

-Dollars.

The divisor is the sum of the errors 90+and 10-

2. There is a fifth whose head is 10 feet long; his tail as long as his head and half the length of his body, and his body as long as his head and tail; what is the whole length of the fish?

Ans. 80 feet.

3. A certain man having driven his Swine to market, viz. Hogs, Sows, and Pigs, received for them all 50l. being paid for every hog 18s. for every fow 16s. for every pig 2s.; there were as many hogs as fows, and for every fow there were three pigs; I demand how many there were of each fort?

Ans. 25 hogs, 25 fows, and 75 pigs.

4. A and Blaid out equal fums of money in trade; A gained a fum equal to 1 of his stock, and B lost 225 dollars; then A's money was double that of B's; what did each one lay out?

Ans. 600 dollars.

5. A and B have the same income; A saves 1/8 of his; but B, by spending 30 dollars per annum more than A, at the end of 8 years finds himself 40 dollars in debt; what is their income, and what does each spend per annum?

Aus. their income is 200 dolls. per ann. A spends 175 dolls. & B 205 per ann.

20 = their in come

12 + 90 = 13 + inas a year

162 240 = 12 + 40

1 = 1020 = (112 + 320

§ 11. Discount.

DISCOUNT is an allowance made for the payment of any fum of money before it becomes due, and is the difference between that fum, due fometime hence, and its prefent worth.

The present worth of any sum, or debt due some time hence, is such a sum, as, if put to interest, would in that time and at the rate per cent. for which

the discount is to be made, amount to the sum or debt, then due.

RULE.

As the amount of 100 dollars, for the given time and rate is to 100 dollars, fo is the given fum to its present worth, which subtracted from the given sum, leaves the discount.

EXAMPLES.

1. What is the discount of Dolls.
2. What is the present worth of 321,63 due 4 years hence, at 6 per cent?
2. What is the present worth of 426 dollars, payable in 4 years and 12 days, discounting at the rate of

operation. 5 per cent.

Dolls. Ans. Dolls. 354,515.

6 interest of 100 dolls. 1 year.

4 years.

24

100

124 amount.

Then, As 124: 100:: 321,63
321,63

124)32163,00(259,379

321,63 given fum. 259,379 present worth.

Aus. 62,251 discount.

§ 12. Equation of Papments.

EQUATION of Payments is the finding of a time to pay at once, feveral debts due at different times so that neither party shall sustain loss.

RULE.

Multiply each payment by the time at which it is due; then divide the fum of the products by the fum of the payments, and the quotient will be the equated time.

EXAMPLES.

1. A owes B 136 dollars, to be paid in 10 months; 69 dollars to be paid. in 7 months; and 260 to be paid in 4 months: what is the equated time for the payment of the whole?

0PERATIO 136× 96× 260×	7= 672 4=1040
492 492)3072 2952	3072 (6months:
120 50	
492)3600 3444	(7 days.
156	-

2. I owe Dolls. 65,125, to be paid $\frac{1}{4}$ in 3 months, $\frac{1}{2}$ in 5 months, $\frac{1}{8}$ in 10 months, and the remainder in 14 months: at what time ought the whole to be paid?

Ans. 6' months.

- 3. A merchant has owing to him 300% to be paid as follows, 50% at 2 months, 100% at 5 months, and the rest at 8 months; and it is agreed to make one payment of the whole; I demand when that time must be?
 - Ans. 6 months.
- 4. A merchant owes me 900 dollars to be paid in 96 days, 130 dollars in 120 days, 500 dollars in 80 days, 1267 dollars in 27 days; what is the mean time for the payment of the whole?

Ans. 63 days very nearly.

§ 13. Guaging.

GUAGING is taking the dimensions of a cask in inches to find its contents in gallons by the following

METHOD.

1. Add two thirds of the difference between the head and bung diameters to the head diameter for the mean diameter; but if the staves be but little curving from the head to the bung, add only fix tenths of this difference.

2. Square the mean diameter, which multiplied by the length of the cask and the product divided by 294, for wine, or by 359 for ale, the quotient

will be the answer in gallons.

EXAMPLE.

1. How many ale or beer gallons will a cask hold, whose bung diameter is 31 inches, head diameter 25 inches, and whose length is 36 inches?

31 25	Bung diam. 2 Head diam.	5 head diam. 4 Two thirds diff.	
6	Difference. 29	– 9 Mean diam. 9	
, ;	26 58	i , `	
		– 1 Square of mean dian 6 Length.	1.
	504 2528	-	
9	· · · · · · · · · · · · · · · · · · ·	-	

359)30276(84 galls. $1+\frac{2}{5}$ gis.

Note. 1. In taking the length of the cask, an allowance must be made for the thickness for both heads of one inch, 1\frac{1}{3} inch, or 2 inches according to the size of the cask.

Note. 2. The head diameter must be taken close to the chimes, and for small casks, add 3 tenths of an inch; for casks of 40 or 50 gallons, 4 tenths, and for larger casks, 5 or 6 tenths, and the sum will be very nearly the head diameter within.

§ 14. Mechanical Powers.

1. OF THE LEVER.

To find what weight may be raifed or balanced by any given power, Say, as the distance between the body to be raised or balanced, and the fulcium or prop, is to the distance between the prop and the point where the power is applied; so is the power to the weight which it will balance or raise.

EXAMPLE.

If a man weighing 150/b. rest on the end of a lever 12 feet long, what weight will he balance on the other end, supposing the prop 1, foot from the weight?

12 feet the Lever.

1,5 distance of the weight from the fulcrum.

10,5 distance from the fulcrum to the man. Therefore, Feet. lb. Feet. As 1,5: 40,5:: 150: 1050 Ans.

2. OF THE WHEEL AND AXLE.

As the diameter of the axle is to the diameter of the wheel, so is the power applied to the wheel, to the weight suspended by the axle.

EXAMPLES.

1. A mechanic wishes to make a windlas in such a manner, as that 1 ib. applied to the wheel, should be equal to 12 suspended on the axle; now, suppoling the axle 4 inches diameter, required the diameter of the wheel?

lb. in.

As 1:4::12:48 Ans. or diameter of the wheel. 2. Suppose the diameter of the axle 6 inches and that of the wheel 60 inches, what power at the wheel will balance 10 lb. at the axle? Ans. 1lb.

3. OF THE SCREW.

The power is to the weight to be raifed as the distance between two threads of the screw is to the circumference of a circle described by the power applied at the end of the lever.

Note 1. To find the circumference of the circle described by the end of the lever, multiply the double of the lever by 3,14159, the product will be the circum-

ference.

Note 2. It is usual to abate ; of the effect of the machine for friction.

EXAMPLES.

There is a screw, whose threads are an inch asunder; the lever by which it is turned is 36 inches long, and the weight to be raifed a ton, or 2240lb. What power or force must be applied to the end of the lever sufficient to turn the screw, that is, to raise the weight?

The lever $36 \times 2 = 72 + 3,14159 = 226,194 + \text{the circumference.}$

e circumf. in. lb. Then, as 226,194:1::2240:9,903

PROBLEMS.

1. The diameter of a circle being given to find the circumference, multiply the diameter by 3,14159; the product will be the circumference.

2. To find the area of a circle, the diameter being given; multiply the

square of the diameter by ,785398; the product is the area.

3. To measure the folidity of any irregular body whose dimensions cannot be taken, put the body into some regular vessel and fill it with water, then taking out the body, measure the fall of water in the vessel; if the vessel be Iquare, multiply the fide by itself, and the product by the fall of water, which gives the forid contents of the irregular body.

SECTION IV.

xxx: :::xxx

MISCELLANEOUS QUESTIONS.

IN this Section there is nothing new to be proposed to the scholar. Enough of Arithmetic has been taught him for all ordinary occurrences in life. It only remains to lead him into some reflections on the foregoing rules. For this purpose the following questions are subjoined. They are lest without answers, that the scholar's only resource of knowledge for working them should be in his own mind. Masters having wrought out these questions at a leisure hour, may transcribe them with their answers into a manuscript for their private use, to which on any occasion, without any trouble or hindrance, they may readily advert to fatisfy the inquiries of their pupils.

1. The Northern Lights were first observed in London in 1560; how many years since?

2. What number multiplied by 43 produces 88150?

3. If a cannon may be discharged twice with 6lb. of powder, how many times will 7C. 3qrs. 17lbs. discharge the same piece?

Reduce 14 guineas and 475 13s. 63d. to Federal Money.
 What is the interest of \$79,49 one year and five months?

6. A owed B \$317,19, for which he gave his note, on interest, bearing date July 12th, 1797.

On the back of the note are these several endorsements, viz.

October 17, 1797, Received in cash, £61,10.

March 20th, 1798, Received 17 cwt. of Beef, at \$4,33 per cwt.

January 1st, 1800, Received in cash, 84 dollars.

What was there due from A to B, of principal and interest, Sept. 18th, 1801?

7. What cost 13½ yards of flannel at 1s. 8½ per yard?

8. What must I give for 3 cwt. 2 qrs. 13lb. of cheese at 7 cents per lb.?

9. What will 35 yards of broadcloth cost at 23s. 6d. per yard?

10. What will be the cost of a line of yeal, weighing 16¾b. at 2¼d. per bl.?
11. What will 87¼b. of tallow cost, at 9¼d. per bl.?

12. What will 196 yards of tape cost, at 3 farthings per yard?

13. What will 56 bushels of oats cost, at 3 farthings per yard:

14. At £3 7s. 6d. per cwt. for fugar, what is that per lb. }

15. How much in length of a board that is 10 inches wide will it require to make a square foot?

16. How many square feet in a board 1 foot, 3 inches wide, and 14 feet, inches long?

- 9 inches long?

 17. How much wood in a load 9 feet long, 3; feet wide, and 2 feet 9 inches high?
 - 18. At \$1,33 per yard for cloth, what must I give for 72 yards?
 - 19. If $2\frac{1}{4}$ cwt. of cotton wool cost £11 17s. 6d. what is that per lb.? 20. If $1832\frac{1}{2}$ gallons of wine cost £44 6s. what is that per gallon?

21. What will 53 lb. of beef colt at 5 cents 5 mills per lb.?

22. What will 50 bulkels of potatoes cost at 21 cents per bulkel?

23. At \$10,76 per cwt. for fugar, what is that per lb.?

24. What will be a man's wages for 6 months, at 43 cents per day, working 52 days per week?

25. What must I give for pasturing my horse 19 weeks, at 33 cents per

week?

26. How many revolutions does the moon perform in 144 years, 2 days, 10 hours; one revolution being in 27 days, 7 h. 43 m.?

27. What will 7 pieces of cloth, containing 27 yards each, come to, at 15s.

 $4^{1}_{2}d$. per yard?

- 28. A man spends 23 dollars 69 cents, 5 mills, in a year, what is that per day?
- 29. Suppose the Legislature of this State should grant a tax of 7 cents 3 mills on a dollar, what will a man's tax be, who is 142 dollars 40 cents on the list?
 - 30. A Bankrupt, whose effects are 3948 dollars, can pay his creditors but

28 cents 5 mills on the dollar; what does he owe?...

31. Suppose a cistern having a pipe that conveys 4 gallons, 2 qts. into it in an hour, has another that lets out 2 gallons, 1 qt. 1 pt. in an hour; if the cistern contains 84 gallons, in what time will it be filled?

32. If 80 dollars worth of provisions will serve 20 men 25 days, what

number of men will the fame provisions serve 10 days?

33. If 6 men spend 16 dollars 7 cents, in 40 days; how long will 135

men be in spending 100 dollars?

- 34. A bridge built across a river in 6 months, by 45 men, was washed away by the current; required the number of workmen sufficient to build another of twice as much worth in 4 months?
- 35. Four men, A, B, C, and D found a purse of money containing 12 dollars, they agree that A shall have one third, B one fourth, C one sixth, and D one eighth of it; what must each one have according to this agreement?
- 36. A certain usurer lent 90% for twelve months, and received principal and interest 95%. 8. I demand at what rate per cent. he received interest?
- 37. If a gentleman have an estate of 1000% per ann. how much may he spend per day to lay up three score guineas at the year's end?
 - 38. What is the length of a road, which being 33 feet wide contains an

acre?

39. Required a number from which if 7 be subtracted and the remainder be divided by 8, and the quotient be multiplied by 5, and 4 added to the product, the square root of the sum extracted, and three souths of that root cubed, the cube divided by 9, the last quotient may be 24?

40. If a quarter of wheat affords 60 ten penny loaves, how many eight

penny loaves may be obtained from it?

41. If the carriage of 7 cwt. 2qr. for 105 miles be 11. 5s. how far may 5 cwt. 1 qr. be carried for the fame money?

42. If 50 men confume 15 bushels of grain in 40 days, how much will

30 men confume in 60 days?

- 43. On the fame supposition, how long will 50 bushels maintain 64 men?
- 44. A gentleman having 50s. to pay among his laborers for a day's work, would give to every boy 6d. to every woman 8d. and to every man 16d. the number of boys, women and men, was the fame, I demand the number of each?
- 45. A gentleman had 7l. 17s. 6d. to pay among his laborers; to every boy he gave 6d. to every woman 8d. and to every man 16d. and there were for every boy three women, and for every woman two men; I demand the number of each?

- 46. Three Gardeners, A, B, and C, having bought a piece of ground, find the profits of it amount to 1201. per annum. Now the sum of money which they laid down was in such proportion, that as often as A paid 51. B paid 71. and as often as B paid 41. C paid 61. I demand how much each man must have per annum of the gain?
- 47. A young man received 2101. which was \(^2\) of his eldest brother's portion: now three times the eldest brother's portion was half the father's estate; I demand how much the estate was?

48. Two men depart both from one place, the one goes North and the other South; the one goes 7 miles a day, the other 11 miles a day; how far are they distant the 12th day after their departure?

49. Two men depart both from one place and both go the fame road; the one travels 12 miles every day, the other 17 miles every day; how far are

they distant the 10th day after their departure?

50. The river Po is 1000 feet broad, and 10 feet deep, and it runs at the rate of 4 miles an hour. In what time will it discharge a cubic mile of water (reckoning 5000 feet to the mile) into the sea?

- 51. If the country which supplies the river Po with water be 380 miles long and 120 broad, and the whole land upon the surface of the earth be 62,700,000 square miles, and if the quantity of water discharged by the rivers into the sea be every where proportional to the extent of land by which the rivers are supplied; how many times greater than the Po will the whole amount of the rivers be?
- 52. Upon the same supposition, what quantity of water altogether will be discharged by all the rivers into the sea in a year?
- 53. If the proportion of the sea on the surface of the earth to that of land be as 10½ to 5, and the mean depth of the sea be a quarter of a mile; how many years would it take if the ocean were empty to fill it by the rivers running at the present rate?
- 54. If a cubic foot of water weigh 1000 oz. avoirdupois, and the weight of mercury be 13\frac{1}{3} times greater than of water, and the height of the mercury in the barometer (the weight of which is equal to the weight of a column of air on the same base, extending to the top of the atmosphere) be 30 inches; what will be the weight of the air upon a square foot? a square mile? and what will be the whole weight of the atmosphere, supposing the size of the earth as in questions 51 and 53?
- 55. A began trade June 1, with 40 dollars, and took in B as a partner, Sept. 8, following, with 120 dollars; on Dec. 24, A put in 190 dollars more, and continued the whole in trade till May 5, following, when their whole gain was found to be 82 dollars; what is each partner's share?

56. If I give 80 bushels of potatoes, at 21 cents per bushel, and 240% of flax, at 15 cents per lb. for 64 bushels of salt, what is the salt per bushel?

57. What is the present worth of 482 dollars, payable 4 years hence, dis-

counting at the rate of 6 per cent?

58. I have owing to me as follows, viz. £18,73 in 8 months; £46,00 in 5 months; and £104,84 in 3 months; what is the mean time for the payment of the whole?

59. If I fell 500 deals at 15d. a piece, and lose £9 per cent. what do I lose

in the whole quantity?

60. If I buy 1000 Ells Flemish of linen for £99, what may I sell it per Ell in London, to gain £19, in the whole?

Pleasant and Diverting Questions.

1. THERE was a well 30 feet deep; a Frog at the bottom could jump up 3 feet every day, but he would fall back two feet every night. How many

days did it take the Frog to jump out?

2. Two men were driving sheep to market, says one to the other, give me one of yours and I shall have as many as you; the other says, give me one of yours and I shall have as many again as you. How many had each?

3. As I was a going to St. Ives, I met feven wives, Every wife had feven facks, Every fack had feven cats, Every cat had feven kits, Kits, cats, facks and wives, How many were going to St. Ives?

4. The account of a certain school is as follows, viz. 10 of the boys learn geometry, $\frac{1}{8}$ learn grammar, $\frac{3}{10}$ learn arithmetic, $\frac{3}{20}$ learn to write, and 9 learn

to read; I demand the number of each?

5 A man driving his geefe to market, was met by another, who faid, Good-morrow, master, with your hundred geese; says he I have not an hundred, but if I had half as many as I now have, and two geese and an half beside the number I now have already, I should have an hundred: How

many had he?

6. Three travellers met at a caravanfary, or inn, in Persia; and two of them brought their provisions along with them, according to the custom of the country; but the third not having provided any, proposed to the others that they should eat together, and he would pay the value of his proportion. This being agreed to, A produces 5 loaves, and B3 loaves, which the travellers eat together, and C paid 8 pieces of money as the value of his share, with which the others were fatisfied, but quarrelled about the dividing of it. Upon this the affair was referred to the judge, who decided the dispute by an impartial fentence. Required his decision?

7. Suppose the 9 Digits to be placed in a quadrangular form; I demand in what order they must stand, that any three figures in a right line, may

make just 15.

8. A countryman having a Fox, a Goose, and a peck of Corn, in his journey came to a river, where it so happened that he could carry but one over at a time. Now as no two were to be left together that might destroy each other; so he was at his wits end how to dispose of them: for, says he, the corn can't eat the goose, nor the goose eat the fox, yet the fox can eat the goose, and the goose eat the corn. The question is how he must carry them over, that they might not devour each other.

9. Three jealous husbands with their wives, being ready to pass by night over a river, do find at water fide a boat which can carry but two persons at once, and for want of a waterman they are necessitated to row themselves over the river at several times: The question is, how those 6 persons shall pass by 2 and 2, so that none of the three wives may be found in the compa-

ny of one or two men, unless her husband be present?

10. Two merry companions are to have equal shares of 8 gallons of wine, which are in a veffel containing exactly 8 gallons; now to divide it equally between them, they have only two other empty veffels, of which one contains 5 gallons, and the other 3; the question is, how they shall divide the said wine between them by the help of these three vessels, so that they may have 4 gallons a piece?

SECTION III.

Forms of Notes, Deeds, Bonds, and other Instruments of Writing.

§ 1. OF NOTES.

Overdean, Sept. 17, 1802. For value received I promise to pay to Oliver Bountiful, or order, fixty-three dollars, fifty-four cents, on demand, with interest after three months. William Trufty.

Attest, Timothy Testimony.

No. II.

Bilfort, Sept. 17, 1802. For value received, I promise to pay O. R. or -cents, three months after date.

Peter Pencil.

No. III.

BY TWO PERSONS.

Arian, Sept. 17, 1802. For value received we jointly and feverally promife to pay C. D. or order, — dollars — cents on demand, with interest. Attest, Alden Faithful. James Fairface.

Constance Adley.

OBSERVATIONS.

1. No note is negotiable unless the words, or order, otherwise, or bearer, be inserted in it.

2. If the note be written to pay him " ar order," (No. 1) then Oliver Bountiful may endorse this note, that is write his name on the back side and sell it to A, B, C, or whom he pleases. Then A, who buys the note, calls on William Trufly for payment, and if he neglects or is unable to pay, A may recover it of the endorser.

3. If a note be written, to pay him " or bearer," (No 2.) then any person

who holds the note may fue and recover the fame of Peter Pencil.

4. The rate of interest established by law being fix per cent. per annum, it becomes unnecessary, in writing notes to mention the rate of interest; it is sufficient to write them for the payment of fuch a fum, with interest, for it will be understood, legal interest, which is fix per cent.

5. All notes are either payable on demand, or at the expiration of a certain term of time agreed upon by the parties and mentioned in the note, as three

months, or a year, &c.

6. If a bond or note mention no time of payment, it is always on demand. whether the words " on demand" be expressed or not.

7. All notes payable at a certain time are on interest as foon as they be-

come due, though in fuch notes there be no mention made of interest.

This rule is founded on the principle, that every man ought to receive his money when due, and that the non payment of it at that time is an injury to him. The law, therefore, to do him justice, allows him interest from the time the money becomes due, as a compensation for the injury.

8. Upon the same principle a note payable on demand, without any mention mude of interest is on interest after a demand of payment, for upon demand

tuch notes immediately become due.

9. If a note be given for a specific article, as rye, payable in one, two or three months, or in any certain time, and the signer of such note suffers the time to elapse without delivering such article, the holder of the note will not be obliged to take the article afterwards, but may demand and recover the value of it in money.

§ 2. OF BONDS.

A Bond, with a condition from one to another.

The condition of this obligation is such, That if the above bound C. D. his heirs, executors or administrators, do and shall well and truly pay or cause to be paid, unto the above named E. F. his executors, administrators or assigns, the sull sum of two hundred dollars, with legal interest for the same, on or before the eleventh day of——next ensuing the date hereof: Then this ob-

ligation to be void, or otherwise to remain in full force and virtue.

Signed, &c.

A Condition of a Counter Bond, or Bond of Indemnity, where one man becomes bound for another.

THE condition of this obligation is such, That whereas the above named A. B. at the special instance and request, and for the only proper debt of the above bound C. D. together with the said C. D. is, in and by one bond or obligation bearing equal date with the obligation above written, held and firmly bound unto E. F. of, &c. in the penal such of dollars, conditioned for the payment of the sum of, &c. with legal interest for the same, on the day of next ensuing the date of the said in part recited obligation, as in and by the said in part recited bond, with the condition thereunder written may more fully appear: If therefore the said C. D. his heirs, executors or administrators, do and shall well and truly pay or cause to be paid unto the said E. F. his executors, administrators, or assigns, the said sum of, &c. with legal interest for the same, on the said day of, &c. next ensuing the date of the said in part recited obligation, according to the true intent and meaning, and in full discharge and satisfaction of the said in part recited bond or obligation: Then, &c. Otherwise, &c.

Note. The principal difference between a note and a bond is that the latter is an inftrument of more folemnity, being given under feal. Also, a note may be controlled by a special agreement, different from the note, whereas, in case of a bond, no special agreement can in the least controll what appears to have been the intention of the parties as expressed by the words in the condition of the bond.

§ 3. OF RECEIPTS.

No. I.

Sitgrieves, Sept. 19, 1802. Received from Mr. Durance Adley, ten dollars in full of all accounts.

Orvand Constance.

No. II.

Sitgrieves, Sept. 19, 1802. Received from Mr. Orvand Constance, five dollars in full of all accounts.

Durance Adley.

No. III.

A Receipt for an endorsement on a Note.

Sitgrieves, Sept. 19, 1802. Received from Mr. Simpson Easley, (by the hand of Mr. Titus Trusty,) fixteen dollars twenty five cents, which is endorsed on his note of June 3, 1802.

Peter Cheerful.

No. IV.

A Receipt for money received on Account.

Sitgrieves, Sept. 19, 1802. Received of Mr. Orand Landlike, fifty dollars on account.

Eldro Slackley.

No. V.

A Receipt for interest due on a Bond.

Received this—day of—of Mr. A. B. the sum of five pounds, in full of one year's interest of 100l. due to me on the—day of—last, on bond from the said A. B. I say received.

By me, C. D.

OBSERVATIONS.

1. There is a distinction between receipts given in full of all accounts, and others in full of all demands. The former cut off accounts only; the latter cut

off not only accounts, but all obligations and right of action.

2. When any two persons make a settlement and pass receipts (No. I. and No. II.) each receipt must specify a particular sum, received, less or more. It is not necessary that the sum specified in the receipt, be the exact sum received.

§ 4. OF ORDERS.

No. 1.

Mr. Stephen Burgefs.

SIR,

For value received, pay to A. B. Ten Dollars, and place the same to my account.

Samuel Skinner.

Archdale, Sept. 9, 1802.

No. II.

Bofton, Sept. 9, 1802.

SIR

For value received, pay G. R. eighty fix cents, and this, with his receipt, shall be your discharge from me.

Nicholas Reubens.

To Mr. James Robottom.

§ 5. OF DEEDS.

No. I.

A Warranty Deed.

Know all Men by these presents, That I, Peter Careful, of Leominster, in the County of Worcester and Commonwealth of Massachusetts, gentleman, for and in consideration of one hundred sifty dollars, and forty sive cents paid to me by Samuel Pendleton, of Ashby, in the County of Middlesex, and Commonwealth of Massachusetts, yeoman, the receipt whereof I do hereby acknowledge, do hereby give, grant, sell and convey to the said Samuel Pendleton, his heirs and assigns, a certain tract and parcel of land, bounded as follows, viz.

[Here infert the bounds, together with all the privileges and appurtenances thereum.

to belonging.]

To have and to hold the same unto the said Samuel Pendleton, his heirs and assigns to his and their use and behoof forever. And I do covenant with the said Peter Pendleton, his heirs and assigns, That I am lawfully seized in see of the premises, that they are free of all incumbrances, and that I will warrant and defend the same to the said Peter Pendleton, his heirs and assigns forever, against the lawful claims and demands of all persons.

In witness whereof I hereunto set my hand and seal, this day of

in the year of our Lord one thousand eight hundred and two.

Signed, fealed and delipered in presence of

Peter Careful. O

L. Ř. F. G.

No. II.

Quitclaim Deed.

Know all Men by These presents, That I, A. B. of, &c. in consideration of the sum of—to be paid by C. D. of, &c. the receipt whereof I do hereby acknowledge, have remissed, released, and forever quit-claimed, and do by these presents remiss, release, and forever quit-claim unto the said C. D. his heirs and assigns forever. (Here insert the premises.) To have and to hold the same, together with all the privileges and appurtenances thereunto belonging, to him the said C. D. his heirs and assigns forever.—In witness, &c.

No III. A Mortgage Deed.

KNOW ALL MEN BY THESE PRESENTS, That I, Simpson Easley, ofthe county of _____in the state of _____, Blacksmith, in consideration Dollars—Cents, paid by Elvin Fairface, of—in the county of _____in the state of _____, Shoemaker, the Receipt whereof I do hereby acknowledge, do hereby give, grant, fell and convey unto the faid Elvin Fairface, his heirs and affigns, a certain tract and parcel of land, bounded as follows, viz. (Here infert the bounds together with all the privileges and appurtenances thereunto belonging.) To have and to hold the afore-granted Premises to the faid Elvin Fairface, his heirs and affigns, to his and their use and behoof And I do covenant with the faid Elvin Fairface, his heirs and affigns, That I am lawfully feized in fee of the afore-granted premifes: That they are free of all incumbrances: That I have good right to fell and convey the same to the said Elvin Fairface. And that I will warrant and defend the same premises to the said Elvin, his heirs and assigns screver, against the lawful claims and demands of all persons. Provided nevertheless, That if I the faid Simpson Easley, my heirs, executors, or administrators, shall well and truly pay the faid Elvin Fairface, his heirs, executors, administrators or affigns, the full and just sum of-dollars-cents on or before theday of---which will be in the year of our Lord Eighteen Hundred andwith lawful interest for the same until paid, then this deed, as also a certain bond [or note as the case may be] bearing date with these presents given by me to the faid Fairface, conditioned to pay the fame fum and interest at the time aforesaid shall be void; otherwise to remain in full force and virtue. In witness whereof, I the said Simpson and Abigail my wife, in testimony that she relinquishes all her right to dower or alimony in and to the above described premises, hereunto set our hands and seals this -- day of -- in the year of our Lord one thousand eight hundred and five.

Signed, fealed and delivered in prefence of L. N.

v. x.

Simpson Fasley. O
Abigail Easley. O

§ 6. OF AN INDENTURE.

A common Indenture to bind an Apprentice.

This Indenture witneffeth, That A. B. of, &c. hath put and placed, and by these presents doth put and bind out his son C. D. and the said C. D. doth hereby put, place and bind out himself, as an apprentice to R. P. to learn the art, trade or mystery of-- The faid C. D. after the manner of an apprentice, to dwell with and ferve the faid R. P.—from the day of the date hereof, until the—day of—which will be in the year of our Lord one thousand eight hundred and—at which time the said apprentice, if he should be living, will be twenty-one years of age: During which time or term the faid apprentice his faid mafter well and faithfully shall serve; his fecrets keep, and his lawful commands every where at all times readily obey, he shall do no damage to his faid master, nor wilfully suffer any to be done by others; and if any to his knowledge be intended, he shall give his master feafonable notice thereof. He shall not waste the goods of his said master nor lend them unlawfully to any; at cards, dice, or any unlawful game he shall not play; fornication he shall not commit, nor matrimony contract during the faid term; taverns, ale-houses, or places of gaming he shall not haunt or frequent: From the fervice of his faid master, he shall not absent himself; but in all things and at all times he shall carry and behave himself as a good and faithful apprentice ought, during the whole time or term aforefaid.

And the faid R. P. on his part, doth hereby promise, covenant and agree to teach and instruct the said apprentice, or cause him to be taught and inftructed, in the art, trade, or calling of a-by the best way or means he can, and also to teach and instruct the said apprentice, or cause him to be taught and instructed, to read and write, and cypher as far as the Rule of Three, if the faid apprentice be capable to learn, and shall well and faithfully find and provide for the faid apprentice, good and fufficient meat, drink, clothing, lodging and other necessaries fit and convenient for such an apprentice, during the term aforefaid, and at the expiration thereof, shall give unto the faid apprentice, two fuits of wearing apparel, one fuitable for the Lord's day, and the other for working days.

In testimony whereof, the faid parties hereunto interchangeably set their hands and feals, the—day of—in the year of our Lord one thousand eight hundred and-

Signed, scaled and deliver-Seal) (Seal)

§ 7. OF A WILL.

The form of a Will, with a devise of a Real Estate, Leasehold, &c.

In the name of GOD, Amen, I, A. B. of, &c. being weak in body, but of found and perfect mind and memory (or you may fay thus, confidering the uncertainty of this mortal life, and being of found, &c.) bleffed be Almighty God for the same, do make and publish this my last Will and Testament, in manner and form following (that is to fay) First, I give and bequeath unto my beloved wife J. B. the fum of——I do also give and bequeath unto my eldest fon, G. B. the sum of-I do also give and bequeath unto my two younger fons, J. B. and F. B. the fum of——a piece. I also give and bequeath to my daughter-in-law, S. H. fingle woman, the fum of---which faid several legacies or sums of money I will and order shall be paid to the faid respective legatees, within fix months after my decease.—I further give and devise to my faid eldest son G. B. his heirs and assigns, All that my mesfuage or tenament, fituate, lying and being in, &c. together with all my other freehold estate whatsoever, to hold to him the said G. B. his heirs and asfigns forever. And I hereby give and bequeath to my faid younger fons, J. B. and F. B. all my leasehold estate of and in all those messuages or tenaments, with the appurtenances, fituate, &c. equally to be divided between them. And lastly, as to all the rest, residue and remainder of my personal estate, goods and chattels, of what kind and nature soever, I give and bequeath the same to my said beloved wife, J. B. whom I hereby appoint sole executrix of this my last Will and Testament; and hereby revoking all former wills by me made.

In suitness whereof I hereunto set my hand and seal, the day of in the year of our Lord-

Signed, fealed, published and declared by the above named A. B. to be his last will and testament, in

the presence of us, who hereunto subscribe our names as witnesses, in the presence of the testator.

R. S. W. T. T. W.

William Hoopen

A. B. (Seal.)

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